# Package 'BiplotML' 

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Description Logistic Biplot is a method that allows representing multivariate binary data on a subspace of low dimension, where each individual is represented by a point and each variable as vectors directed through the origin. The orthogonal projection of individuals onto these vectors predicts the expected probability that the characteristic occurs. The package contains new techniques to estimate the model parameters and con-
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bootBLB Fitting a Binary Logistic Biplot using bootstrap methodology

## Description

This function estimates the vector $\mu$, matrix A and matrix B using the optimization algorithm chosen by the user and applies a bootstrap methodology to determine the confidence ellipses.

## Usage

bootBLB(
x,
$\mathrm{k}=2$,
$\mathrm{L}=0$,
method = "CG",
type = 1,
plot = TRUE,
sup = TRUE,
ellipses = FALSE,
maxit = NULL,
resamples = 100,
conf $=0.9$,
col.ind $=$ NULL
)

## Arguments

| x | Binary matrix. |
| :--- | :--- |
| k | Dimensions number. By default $\mathrm{k}=2$. |
| L | Penalization parameter. By default $\mathrm{L}=0$. |
| method | Method to be used to estimate the parameters. By default method="CG" |
| type | For the conjugate-gradients method. Takes value 1 for the Fletcher-Reeves up- <br> date, 2 for Polak-Ribiere and 3 for Beale-Sorenson. |
| plot | Plot the Bootstrap Logistic Biplot. |


| sup | Boolean, if TRUE, rows that are not selected in each resample are treated as <br> supplementary individuals. See details. |
| :--- | :--- |
| ellipses | Draw confidence ellipses. By default is FALSE. <br> maxit |
| The maximum number of iterations. Defaults to 100 for the gradient methods, <br> and 500 without gradient. |  |
| resamples | Number of iterations in the bootstrap process. By default 100. |
| conf | Level confidence in the ellipses. By default conf $=0.90$ <br> col.ind |
| Color for the rows. |  |

## Details

Fitting when sup=TRUE ... whereas sup=FALSE ...

## Value

Coordenates of the matrix A and B in resamples and Biplot

## Author(s)

Giovany Babativa < gbabativam@gmail.com>

## References

John C. Nash (2011). Unifying Optimization Algorithms to Aid Software System Users:optimx for R. Journal of Statistical Software. 43(9). 1-14.

John C. Nash (2014). On Best Practice Optimization Methods in R. Journal of Statistical Software. 60(2). 1-14.
Milan, L., \& Whittaker, J. (1995). Application of the parametric bootstrap to models that incorporate a singular value decomposition. Applied Statistics, 44, 31-49.
Vicente-Villardon, J.L. and Galindo, M. Purificacion (2006), Multiple Correspondence Analysis and related Methods. Chapter: Logistic Biplots. Chapman-Hall

## See Also

plotBLB, performanceBLB

## Examples

```
data("Methylation")
set.seed(02052020)
out.sup <- bootBLB(x = Methylation, ellipses = FALSE)
out <- bootBLB(x = Methylation, sup = FALSE, ellipses = TRUE)
```

```
cv_LogBip Cross-Validation for logistic biplot
```


## Description

This function run cross-validation for logistic biplot

## Usage

cv_LogBip(
data,
$\mathrm{k}=0: 5$,
K = 7,
method = "MM",
type = NULL,
plot = TRUE,
maxit = NULL
)

## Arguments

| data | Binary matrix. |
| :--- | :--- |
| k | Dimensions to analyze. By default $\mathrm{k}=1: 3$. |
| K | folds. By default $\mathrm{K}=7$. |
| method | Method to be used to estimate the parameters. By default method="MM" |
| type | For the conjugate-gradients method. Takes value 1 for the Fletcher-Reeves up- <br> date, 2 for Polak-Ribiere and 3 for Beale-Sorenson. |
| plot | draw the graph. By default plot=TRUE |
| maxit | The maximum number of iterations. Defaults to 100 for the gradient methods, <br> and 2000 for MM algorithm. |

## Value

Training error and generalization error for a logistic biplot model.

## Author(s)

Giovany Babativa [gbabativam@gmail.com](mailto:gbabativam@gmail.com)

## References

Bro R and Kjeldahl K and Smilde AK. (2008). Cross-validation of component models: a critical look at current methods. Analytical and bioanalytical chemistry. 390(5):1241-1251
Wold S. (1978). Cross-validatory estimation of the number of components in factor and principal components models. Technometrics. 20(4):397-405.

## See Also

```
LogBip,pred_LB,fitted_LB,simBin
```


## Examples

```
set.seed(1234)
x <- simBin(n = 100, p = 50, k = 3, D = 0.5, C = 20)
# cross-validation with coordinate descendent MM algorithm
cv_MM <- cv_LogBip(data = x$X, k=0:5, method = "MM", maxit = 1000)
# cross-validation with CG Fletcher-Reeves algorithm
cv_CG <- cv_LogBip(data = x$X, k=0:5, method = "CG", type = 1)
# cross-validation with projection data and block coordinate descending algorithm
cv_PB <- cv_LogBip(data = x$X, k=0:5, method = "PDLB", maxit = 1000)
```

fitted_LB Fitted values using Logistic Biplot

## Description

Compute the predicted matrix or log-odds for a logistic biplot model

## Usage

fitted_LB(object, type = c("link", "response"))

## Arguments

object BiplotML object
type the type of fitting required. type = "link" gives output on the logit scale and type $=$ "response" gives output on the probability scale

## Value

This function returns the predicted matrix or the log-odds of a binary logistic biplot model.

## Author(s)

Giovany Babativa [gbabativam@gmail.com](mailto:gbabativam@gmail.com)

## Examples

```
data("Methylation")
LB <- LogBip(Methylation, plot = FALSE)
Theta <- fitted_LB(LB, type = "link")
Pi <- fitted_LB(LB, type = "response")
```

```
    gradientDesc Gradient function for Binary Logistic Biplot
```


## Description

This function computes the parameters of A and B in Binary Logistic Biplot under algorithm of Descendent Gradient.

## Usage

gradientDesc ( x,
k = 2,
rate $=0.001$,
converg $=0.001$,
max_iter,
plot $=$ FALSE,
)

## Arguments

| x | Binary matrix. |
| :--- | :--- |
| k | Dimensions number. By default $\mathrm{k}=2$. |
| rate | The value of the rate of descent $\alpha$ in the algorithm of descending gradient. By <br> default $\alpha=0.001$. |
| converg | Tolerance limit to achieve convergence. By default converg $=0.001$ |
| max_iter | Maximum iterations number. |
| plot | Plot the Logistic Biplot. |
| $\ldots$ | other arguments |

## Details

We note that the Binary Logistic Biplot is defined as:

$$
\operatorname{logit}\left(\pi_{i j}\right)=\log \left(\frac{\pi_{i j}}{1-\pi_{i j}}\right)=\mu_{j}+\sum_{s=1}^{k} b_{j s} a_{i s}=\mu_{j}+\mathbf{a}_{\mathbf{i}}^{\mathbf{T}} \mathbf{b}_{\mathbf{j}}
$$

Also, note that the gradient is:

$$
\nabla \ell=\left(\frac{\partial \ell}{\partial \mu}, \frac{\partial \ell}{\partial \mathbf{A}}, \frac{\partial \ell}{\partial \mathbf{B}}\right)==\left((\Pi-\mathbf{X})^{T},(\Pi-\mathbf{X}) \mathbf{B},(\Pi-\mathbf{X})^{T} A\right)
$$

## Value

The coefficients of A and B matrix.

## Author(s)

Giovany Babativa < gbabativam@gmail.com>

## References

Vicente-Villardon, J.L. and Galindo, M. Purificacion (2006), Multiple Correspondence Analysis and related Methods. Chapter: Logistic Biplots. Chapman-Hall

## See Also

```
plotBLB,performanceBLB
```


## Examples

```
data('Methylation')
set.seed(02052020)
MatGD <- gradientDesc(x = Methylation, k=2, max_iter=10000)
outGD <- gradientDesc(x = Methylation, k=2, max_iter=10000, plot = TRUE)
```

LogBip

Fitting a Binary Logistic Biplot using optimization methods

## Description

This function estimates the vector $\mu$, matrix A and matrix B using the optimization algorithm chosen by the user. The PDLB method allows to enter a binary matrix with missing data

## Usage

```
LogBip(
    x,
    k = 2,
    method = "MM",
    type = NULL,
    plot = TRUE,
    maxit = NULL,
    endsegm = 0.9,
    label.ind = FALSE,
    col.ind = NULL,
```

```
    draw = c("biplot", "ind", "var"),
    random_start = FALSE,
    L = 0,
    cv_LogBip = FALSE
)
```


## Arguments

x
k
method Method to be used to estimate the parameters. By default method="CG"
type For the conjugate-gradients method. Takes value 1 for the Fletcher-Reeves update, 2 for Polak-Ribiere and 3 for Beale-Sorenson.
plot Plot the Bootstrap Logistic Biplot.
maxit The maximum number of iterations. Defaults to 100 for the gradient methods, and 500 without gradient.
endsegm The segment starts at 0.5 and ends at this value. By default endsegm $=0.90$.
label.ind By default the row points are not labelled.
col.ind Color for the rows marks.
draw The graph to draw ("ind" for the individuals, "var" for the variables and "biplot" for the row and columns coordinates in the same graph)
random_start Logical value; whether to randomly inititalize the parameters. If FALSE, algorithm will use an SVD as starting value.
$L \quad$ Penalization parameter. By default $L=0$.
cv_LogBip Indicates if the procedure is being used for cross validation.

## Details

The methods that can be used to estimate the parameters of a logistic biplot

- For methods based on the conjugate gradient use method = "CG" and
type $=1$ for the Fletcher Reeves; type $=2$ for Polak Ribiere; type $=3$ for Hestenes Stiefel and type $=4$ for Dai Yuan.
- To use the iterative coordinate descendent MM algorithm then method = "MM".
- If the binary matrix X has missing data, use method $=$ "PDLB". In case it's required to estimate the row coordinates of other individuals, this method is also the most appropriate. For more details see the paper "Logistic biplot with missing data".
- To use the BFGS formula, method = "BFGS".


## Value

Coordenates of the matrix A and B , threshold for classification rule. Furthemore, for the PDLB method, the imputed matrix is returned.

## Author(s)

Giovany Babativa [gbabativam@gmail.com](mailto:gbabativam@gmail.com)

## References

Babativa-Marquez, J. G., \& Vicente-Villardon, J. L. (2022). Logistic biplot with missing data. In Process.
Babativa-Marquez, J. G., \& Vicente-Villardon, J. L. (2021). Logistic Biplot by Conjugate Gradient Algorithms and Iterated SVD. Mathematics, 9(16).
John C. Nash (2011). Unifying Optimization Algorithms to Aid Software System Users:optimx for R. Journal of Statistical Software. 43(9). 1-14.

John C. Nash (2014). On Best Practice Optimization Methods in R. Journal of Statistical Software. 60(2). 1-14.

Nocedal, J.;Wright, S. (2006). Numerical optimization; Springer Science \& Business Media.
Vicente-Villardon, J.L. and Galindo, M. Purificacion (2006), Multiple Correspondence Analysis and related Methods. Chapter: Logistic Biplots. Chapman-Hall

## See Also

```
plotBLB,pred_LB,fitted_LB
```


## Examples

```
data("Methylation")
# If the binary matrix has no missing data and does not require the projection
# of supplementary individuals, you can use an coordinate descendent MM algorithm
res_MM <- LogBip(x = Methylation, method = "MM", maxit = 1000)
# If the binary matrix has missing data or requires the projection of supplementary
#individuals, use a method based on data projection with a block coordinate descent algorithm
data("Methylation")
set.seed(12345)
n <- nrow(Methylation)
p <- ncol(Methylation)
miss <- matrix(rbinom(n*p, 1, 0.2), n, p) #I simulate some missing data
miss <- ifelse(miss == 1, NA, miss)
x <- Methylation + miss #Matrix containing missing data
out <- LogBip(x, method = "PDLB", maxit = 1000)
```

Methylation Binary data set of 48 human cell lines.

## Description

A dataset containing the BRCA (breast invasive carcinoma) for 48 human cell lines, where each variable is a likely cancer driver or suppressor gene. A gene is labeled as ' 1 ' when it is classified as mutated in a sample and as ' 0 ' when classified as wild type.

## Usage

Methylation

## Format

A data frame with 48 rows and 9 variables:
GSTM1 Glutathione S-Transferase Mu 1, is a Protein Coding gene
C1orf70 Chromosome 1 Open Reading Frame 70, Transmembrane Protein
DNM3 Dynamin 3, is a Protein Coding gene
THY1 Thy-1 Cell Surface Antigen, is a Protein Coding gene
ADCY4 Adenylate Cyclase 4, is a Protein Coding gene
GSTT1 Glutathione S-Transferase Theta 1, is a Protein Coding gen
FILIP1L Filamin A Interacting Protein 1 Like, is a Protein Coding gene
DUSP22 Dual Specificity Phosphatase 22, is a Protein Coding gene
NAPRT1 Nicotinic Acid Phosphoribosyltransferase

## Source

https://www.cancerrxgene.org
performanceBLB Performance comparison of severals estimation algorithms

## Description

This function computes the estimates of A and B matrix with severals algorithms.

## Usage

performanceBLB(xi, $k=2, L=0$, method $=N U L L$, maxit $=$ NULL)

## Arguments

xi Binary matrix.
$\mathrm{k} \quad$ Dimensions number. By default $\mathrm{k}=2$.
$\mathrm{L} \quad$ Penalization parameter. By default $\mathrm{L}=0$.
method use value 1 for algorithms without gradient, 2 with gradient, 3 quasi-newton methods or 4 for all methods. By default method $=2$.
maxit The maximum number of iterations. Defaults to 100 for the gradient methods, and 500 without gradient.

## Details

This function compare the process time and convergence of different algorithms without gradient, with gradient or quasi-newton method for estimating the parameters in a Binary Logistic Biplot

## Value

data frame with method, time of process, convergence and number of evaluations

## Author(s)

Giovany Babativa [gbabativam@gmail.com](mailto:gbabativam@gmail.com)

## References

John C. Nash (2011). Unifying Optimization Algorithms to Aid Software System Users:optimx for R. Journal of Statistical Software. 43(9). 1-14.

John C. Nash (2014). On Best Practice Optimization Methods in R. Journal of Statistical Software. 60(2). 1-14.
Vicente-Villardon, J.L. and Galindo, M. Purificacion (2006), Multiple Correspondence Analysis and related Methods. Chapter: Logistic Biplots. Chapman-Hall

## See Also

gradientDesc

## Examples

```
data('Methylation')
set.seed(123456)
########### Gradient Methods
performanceBLB(xi = Methylation)
performanceBLB(xi = Methylation, maxit = 150)
########### Without Gradient Methods
performanceBLB(xi = Methylation, method = 1)
performanceBLB(xi = Methylation, method = 1, maxit = 100)
############ Quasi-Newton Methods
performanceBLB(xi = Methylation, method = 3)
performanceBLB(xi = Methylation, method = 3, maxit = 100)
############ All methods
performanceBLB(x = Methylation, method = 4)
```

```
plotBLB Plot a Binary Logistic Biplot using a BiplotML object
```


## Description

Plot the bootstrap binary logistic biplot and draw confidence ellipses on the individuals of an object BiplotML.

```
Usage
    plotBLB(
        x,
        dim = c(1, 2),
        col.ind = NULL,
        col.var = "#0E185F",
        label.ind = FALSE,
        draw = c("biplot", "ind", "var"),
        titles = NULL,
        ellipses = FALSE,
        endsegm = 0.75,
        repel = FALSE,
        xylim = NULL
    )
```


## Arguments

| x | Object class BiplotML. |
| :--- | :--- |
| dim | Dimensions plot. By default Dim1 and Dim2. |
| col.ind | Color for the individuals. |
| col.var | Color for the variables. |
| label.ind | By default the row points are not labelled. |
| draw | The graph to draw ("ind" for the individuals, "var" for the variables and "biplot" <br> for the row and columns coordinates in the same graph) |
| titles | Title for the Biplot |
| ellipses | If ellipses=TRUE, draw confidence ellipses around the rows. <br> endsegm |
| Represents where the segment of a variable ends on the logit probability scale. <br> By default endsegm=0.75 |  |
| repel | Repel overlapping text labels. <br> vector specifying the minimum and maximum of the x-axis and y-axis. For <br> example, you can use xylim=c(-10, 10). |

## Details

If draw = "ind", then the biplot is plotted only for individuals and if draw = "var" then is plotted only for the variables.

## Value

Returns the Biplot of the individuals and variables.

## Author(s)

Giovany Babativa [gbabativam@gmail.com](mailto:gbabativam@gmail.com)

## References

Meulman, J. J., \& Heiser, W. J. (1983). The display of bootstrap solutions in multidimensional scaling. Murray Hill, NJ: Bell Laboratories. (Technical memorandum)
Vicente-Villardon, J.L. and Galindo, M. Purificacion (2006), Multiple Correspondence Analysis and related Methods. Chapter: Logistic Biplots. Chapman-Hall

## See Also

```
bootBLB
```


## Examples

```
data("Methylation")
set.seed(123456)
outBLB <- bootBLB(x = Methylation, sup = TRUE, plot=FALSE)
plotBLB(x = outBLB, titles = "Methylation Logistic Biplot", ellipses = FALSE)
plotBLB(x = outBLB, titles = "Methylation LogBiplot", endsegm = 0.95)
plotBLB(x = outBLB, label.ind = TRUE, titles = "Methylation LogBiplot")
```

```
pred_LB Predict logistic biplot and thresholds by variable
```


## Description

Predicts the binary matrix and calculates the optimal thresholds per variable that minimize the Balanced Accuracy (BACC)

## Usage

pred_LB(object, $x$, ncuts $=100$ )

## Arguments

object BiplotML object
$x \quad$ Binary matrix.
ncuts $\quad$ Number of equidistant cuts between 0 and 1 that will be evaluated. By default ncuts $=100$

## Details

The threshold for each variable is lowered to minimize the Balanced Accuracy (BACC).

$$
B A C C=\frac{1}{2}\left(\frac{T P}{T P+F N}+\frac{T N}{T N+F P}\right)
$$

where TP is the number of true positives, TN is the number of true negatives, FP is the number of false positives and FN is the number of false negatives

## Value

This function returns the thresholds per variable, the predicted matrix, the confusion matrix and the BACC.

## Examples

```
data("Methylation")
LB <- LogBip(Methylation, plot = FALSE)
out <- pred_LB(LB, Methylation)
```

proj_LogBip

Fitting a Binary Logistic Biplot with Missing Data Using Data Projection and a Block Coordinate Descending Algorithm

## Description

This function impute the missing values of a binary dataset $X$, and estimates the vector $\mu$, matrix A and matrix B using data projection model with a block coordinate descending algorithm.

## Usage

proj_LogBip(x, k = 2, max_iters = 1000, random_start $=$ FALSE, epsilon $=1 \mathrm{e}-05$ )

## Arguments

| x | binary matrix. |
| :--- | :--- |
| k | dimensions number. By default $\mathrm{k}=2$. |
| max_iters | maximum iterations. |
| random_start | random initialization |
| epsilon | convergence criteria |

## Value

Imputed $X$ matrix and coordenates of the matrix $\mathbf{A}$ and $\mathbf{B}$, and $\mu$

## Author(s)

Giovany Babativa < gbabativam@gmail.com>

## References

Babativa-Marquez, J. G., \& Vicente-Villardon, J. L. (2022). Logistic biplot with missing data. Babativa-Marquez, J. G., \& Vicente-Villardon, J. L. (2021). Logistic Biplot by Conjugate Gradient Algorithms and Iterated SVD. Mathematics, 9(16). Vicente-Villardon, J.L. and Galindo, M. Purificacion (2006), Multiple Correspondence Analysis and related Methods. Chapter: Logistic Biplots. Chapman-Hall

## See Also

cv_LogBip

## Examples

```
data("Methylation")
set.seed(12345)
n <- nrow(Methylation)
p <- ncol(Methylation)
miss <- matrix(rbinom(n*p, 1, 0.2), n, p) #I simulate some missing data
miss <- ifelse(miss == 1, NA, miss)
x <- Methylation + miss #Matrix containing missing data
out <- LogBip(x, method = "PDLB", maxit = 1000)
```

```
sdv_MM
```

Fitting a Binary Logistic Biplot using coordinate descendent MM algorithm

## Description

This function estimates the vector $\mu$, matrix A and matrix B using coordinate descendent MM algorithm.

```
Usage
    sdv_MM(
        x,
        k = 2,
        iterations = 1000,
        truncated = TRUE,
        random = FALSE,
        epsilon = 1e-04
    )
```


## Arguments

| x | binary matrix. |
| :--- | :--- |
| k | dimensions number. By default $\mathrm{k}=2$. |
| iterations | maximum iterations. |
| truncated | if TRUE, find the k largest singular values and vectors of a matrix. |
| random | random initialization |
| epsilon | convergence criteria |

## Value

Coordenates of the matrix A and B , and $\mu$

## Author(s)

Giovany Babativa [gbabativam@gmail.com](mailto:gbabativam@gmail.com)

## References

Babativa-Marquez, J. G., \& Vicente-Villardon, J. L. (2021). Logistic Biplot by Conjugate Gradient Algorithms and Iterated SVD. Mathematics, 9(16).
Vicente-Villardon, J.L. and Galindo, M. Purificacion (2006), Multiple Correspondence Analysis and related Methods. Chapter: Logistic Biplots. Chapman-Hall

## See Also

cv_LogBip

## Examples

```
data("Methylation")
out <- sdv_MM(x = Methylation)
```

simBin Multivariate binary data

## Description

Simulate a binary data matrix based on a latent variables model

## Usage

$\operatorname{simBin}(\mathrm{n}, \mathrm{p}, \mathrm{k}, \mathrm{D}, \mathrm{C}=1)$

## Arguments

n
$p$ number of columns
k number of underlying dimensions in the model
D sparsity control
C variance control

## Value

X: binary matrix, P: predicted matrix, Theta: matrix of natural parameters, A: row markers, B: column markers, mu: offset term, D: sparsity level, n: number of rows, $p$ : number of columns

## Author(s)

Giovany Babativa [gbabativam@gmail.com](mailto:gbabativam@gmail.com)

## See Also

cv_LogBip

## Examples

$x<-\operatorname{simBin}(n=100, p=50, k=3, D=0.5)$

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