Package 'EQUIVNONINF'

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Description

Making available in R the complete set of programs accompanying S. Wellek's (2010) monograph "Testing Statistical Hypotheses of Equivalence and Noninferiority. Second Edition" (Chapman&Hall/CRC).

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EQUIVNONINF-package
bilst
bi2aeq1
bi2aeq2
bi2aeq3
bi2by_ni_del
bi2by_ni_OR 10
bi2diffac
bi2dipow 12
bi2rlv1
bi2rlv2
bi2st
bi2ste1

bi2ste2	18
bi2ste3	19
bi2wld_ni_del	21
cf_reh_exact	22
cf_reh_midp	23
exp1st	25
fstretch	26
gofhwex	28
gofhwex_1s	29
	30
gofsimpt	31
mawi	33
mcnasc_ni	34
mcnby_ni	35
mcnby_ni_pp	37
menemase	38
mcnempow	39
mwtie_fr	40
mwtie_xy	42
postmys	43
powsign	45
pow_abe	46
po_pbibe	47
sgnrk	48
srktie_d	50
srktie_m	51
tt1st	53
tt2st	54
	56

Index

EQUIVNONINF-package Testing for equivalence and noninferiority

Description

The package makes available in R the complete set of programs accompanying S. Wellek's (2010) monograph "Testing Statistical Hypotheses of Equivalence and Noninferiority. Second Edition" (Chapman&Hall/CRC).

Note

In order to keep execution time of all examples below the limit set by the CRAN administration, in a number of cases the function calls shown in the documentation contain specifications which are insufficient for real applications. This holds in particular true for the width sw of search grids, which should be chosen to be .001 or smaller. Similarly, the maximum number of interval halving steps to be carried out in finding maximally admissible significance levels should be set to values ≥ 10 .

bi1st

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2015.

Examples

bi2ste1(397,397,0.0,0.025,0.511,0.384) bi2ste2(0.0,0.025,0.95,0.8,0.80,1.0)

Critical constants and power of the UMP test for equivalence of a single binomial proportion to some given reference value

Description

The function computes the critical constants defining the uniformly most powerful (randomized) test for the problem $p \le p_1$ or $p \ge p_2$ versus $p_1 , with p denoting the parameter of a binomial distribution from which a single sample of size n is available. In the output, one also finds the power against the alternative that the true value of p falls on the midpoint of the hypothetical equivalence interval <math>(p_1, p_2)$.

Usage

bi1st(alpha,n,P1,P2)

Arguments

alpha	significance level
n	sample size
P1	lower limit of the hypothetical equivalence range for the binomial parameter p
P2	upper limit of the hypothetical equivalence range for p

alpha	significance level
n	sample size
P1	lower limit of the hypothetical equivalence range for the binomial parameter \boldsymbol{p}
P2	upper limit of the hypothetical equivalence range for p

C1	left-hand limit of the critical interval for the observed number X of successes
C2	right-hand limit of the critical interval for X
GAM1	probability of rejecting the null hypothesis when it turns out that $X = C_1$
GAM2	probability of rejecting the null hypothesis for $X = C_2$
POWNONRD	Power of the nonrandomized version of the test against the alternative $p = (p_1 + p_2)/2$
POW	Power of the randomized UMP test against the alternative $p = (p_1 + p_2)/2$

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 4.3.

Examples

bi1st(.05,273,.65,.75)

bi2aeq1

Power of the exact Fisher type test for equivalence

Description

The function computes exact values of the power of the randomized UMPU test for equivalence in the strict (i.e. two-sided) sense of two binomial distributions and the conservative nonrandomized version of that test. It is assumed that the samples being available from both distributions are independent.

Usage

```
bi2aeq1(m,n,rho1,rho2,alpha,p1,p2)
```

Arguments

size of Sample 1
size of Sample 2
lower limit of the hypothetical equivalence range for the odds ratio
upper limit of the hypothetical equivalence range for the odds ratio
significance level
true success rate in Population 1
true success rate in Population 2

bi2aeq2

Value

m	size of Sample 1
n	size of Sample 2
rho1	lower limit of the hypothetical equivalence range for the odds ratio
rho2	upper limit of the hypothetical equivalence range for the odds ratio
alpha	significance level
p1	true success rate in Population 1
p2	true success rate in Population 2
POWNR	Power of the nonrandomized version of the test
POW	Power of the randomized UMPU test

Author(s)

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 6.6.4.

Examples

bi2aeq1(302,302,0.6667,1.5,0.05,0.5,0.5)

bi2aeq2

Sample sizes for the exact Fisher type test for equivalence

Description

The function computes minimum sample sizes required in the randomized UMPU test for equivalence of two binomial distributions with respect to the odds ratio. Computation is done under the side condition that the ratio m/n has some predefined value λ .

Usage

bi2aeq2(rho1,rho2,alpha,p1,p2,beta,qlambd)

Arguments

rho1	lower limit of the hypothetical equivalence range for the odds ratio
rho2	upper limit of the hypothetical equivalence range for the odds ratio
alpha	significance level
p1	true success rate in Population 1
p2	true success rate in Population 2
beta	target value of power
qlambd	sample size ratio m/n

Value

rho1	lower limit of the hypothetical equivalence range for the odds ratio
rho2	upper limit of the hypothetical equivalence range for the odds ratio
alpha	significance level
p1	true success rate in Population 1
p2	true success rate in Population 2
beta	target value of power
qlambd	sample size ratio m/n
М	minimum size of Sample 1
Ν	minimum size of Sample 2
POW	Power of the randomized UMPU test attained with the computed values of m,n

Author(s)

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 6.6.4.

Examples

bi2aeq2(0.5,2.0,0.05,0.5,0.5,0.60,1.0)

bi2aeq3

Determination of a maximally raised nominal significance level for the nonrandomized version of the exact Fisher type test for equivalence

Description

The objective is to raise the nominal significance level as far as possible without exceeding the target significance level in the nonrandomized version of the test. The approach goes back to R.D. Boschloo (1970) who used the same technique for reducing the conservatism of the traditional nonrandomized Fisher test for superiority.

Usage

bi2aeq3(m,n,rho1,rho2,alpha,sw,tolrd,tol,maxh)

Arguments

m	size of Sample 1
n	size of Sample 2
rho1	lower limit of the hypothetical equivalence range for the odds ratio
rho2	upper limit of the hypothetical equivalence range for the odds ratio
alpha	significance level
SW	width of the search grid for determining the maximum of the rejection probabil- ity on the common boundary of the hypotheses
tolrd	horizontal distance from 0 and 1, respectively of the left- and right-most bound- ary point to be included in the search grid
tol	upper bound to the absolute difference between size and target level below which the search for a corrected nominal level terminates
maxh	maximum number of interval halving steps to be carried out in finding the max- imally raised nominal level

Details

It should be noted that, as the function of the nominal level, the size of the nonrandomized test is piecewise constant. Accordingly, there is a nondegenerate interval of "candidate" nominal levels serving the purpose. The limits of such an interval can be read from the output. In terms of execution time, bi2aeq3 is the most demanding program of the whole package.

m	size of Sample 1
n	size of Sample 2
rho1	lower limit of the hypothetical equivalence range for the odds ratio
rho2	upper limit of the hypothetical equivalence range for the odds ratio

alpha	significance level
SW	width of the search grid for determining the maximum of the rejection probabil- ity on the common boundary of the hypotheses
tolrd	horizontal distance from 0 and 1, respectively of the left- and right-most bound- ary point to be included in the search grid
tol	upper bound to the absolute difference between size and target level below which the search for a corrected nominal level terminates
maxh	maximum number of interval halving steps to be carried out in finding the max- imally raised nominal level
ALPH_0	current trial value of the raised nominal level searched for
NHST	number of interval-halving steps performed up to now
SIZE	size of the critical region corresponding to α_0

Author(s)

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References

Boschloo RD: Raised conditional level of significance for the 2 x 2- table when testing the equality of two probabilities. Statistica Neerlandica 24 (1970), 1-35.

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 6.6.5.

Examples

bi2aeq3(50,50,0.6667,1.5000,0.05,0.01,0.000001,0.0001,5)

bi2by_ni_del Objective Bayesian test for noninferiority in the two-sample setti with binary data and the difference of the two proportions as the p rameter of interest	with binary data and the difference of the two proportions	1 0
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Description

Implementation of the construction described on pp. 185-6 of Wellek S (2010) Testing statistical hypotheses of equivalence and noninferiority. Second edition.

Usage

bi2by_ni_del(N1,N2,EPS,SW,NSUB,ALPHA,MAXH)

bi2by_ni_del

Arguments

N1	size of Sample 1
N2	size of sample 2
EPS	noninferiority margin to the difference of success probabilities
SW	width of the search grid for determining the maximum of the rejection probabil- ity on the common boundary of the hypotheses
NSUB	number of subintervals for partitioning the range of integration
ALPHA	target significance level
MAXH	maximum number of interval halving steps to be carried out in finding the max- imally admissible nominal level

Details

The program uses 96-point Gauss-Legendre quadrature on each of the NSUB intervals into which the range of integration is partitioned.

Value

N1	size of Sample 1
N2	size of sample 2
EPS	noninferiority margin to the difference of success probabilities
NSUB	number of subintervals for partitioning the range of integration
SW	width of the search grid for determining the maximum of the rejection probabil- ity on the common boundary of the hypotheses
ALPHA0	result of the search for the largest admissible nominal level
SIZEØ	size of the critical region corresponding to α_0
SIZE_UNC	size of the critical region of the test at uncorrected nominal level

Author(s)

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References

Wellek S: Statistical methods for the analysis of two-armed non-inferiority trials with binary outcomes. Biometrical Journal 47 (2005), 48–61.

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 6.6.3.

Examples

bi2by_ni_del(20,20,.10,.01,10,.05,5)

bi2by_ni_OR

Description

Implementation of the construction described on pp. 179–181 of Wellek S (2010) Testing statistical hypotheses of equivalence and noninferiority. Second edition.

Usage

bi2by_ni_OR(N1,N2,EPS,SW,NSUB,ALPHA,MAXH)

Arguments

N1	size of sample 1
N2	size of sample 2
EPS	noninferiority margin to the deviation of the odds ratio from unity
SW	width of the search grid for determining the maximum of the rejection probabil- ity on the common boundary of the hypotheses
NSUB	number of subintervals for partitioning the range of integration
ALPHA	target significance level
MAXH	maximum number of interval halving steps to be carried out in finding the max- imally admissible nominal level

Details

The program uses 96-point Gauss-Legendre quadrature on each of the NSUB intervals into which the range of integration is partitioned.

N1	size of sample 1
N2	size of sample 2
EPS	noninferiority margin to the deviation of the odds ratio from unity
NSUB	number of subintervals for partitioning the range of integration
SW	width of the search grid for determining the maximum of the rejection probabil- ity on the common boundary of the hypotheses
ALPHA0	result of the search for the largest admissible nominal level
SIZEØ	size of the critical region corresponding to α_0
SIZE_UNC	size of the critical region of the test at uncorrected nominal level

bi2diffac

Author(s)

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References

Wellek S: Statistical methods for the analysis of two-arm non-inferiority trials with binary outcomes. Biometrical Journal 47 (2005), 48–61.

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 6.6.2.

Examples

bi2by_ni_OR(10,10,1/3,.0005,10,.05,12)

bi2diffac	Determination of a corrected nominal significance level for the asymp-
	totic test for equivalence of two unrelated binomial proportions with
	respect to the difference δ of their population counterparts

Description

The program computes the largest nominal significance level which can be substituted for the target level α without making the exact size of the asymptotic testing procedure larger than α .

Usage

bi2diffac(alpha,m,n,del1,del2,sw,tolrd,tol,maxh)

Arguments

alpha	significance level
m	size of Sample 1
n	size of Sample 2
del1	absolute value of the lower limit of the hypothetical equivalence range for $p_1 - p_2$
del2	upper limit of the hypothetical equivalence range for $p_1 - p_2$
SW	width of the search grid for determining the maximum of the rejection probabil- ity on the common boundary of the hypotheses
tolrd	horizontal distance of the left- and right-most boundary point to be included in the search grid
tol	upper bound to the absolute difference between size and target level below which the search for a corrected nominal level terminates
maxh	maximum number of interval halving steps to be carried out in finding the max- imally raised nominal level

Value

alpha	significance level
m	size of Sample 1
n	size of Sample 2
del1	absolute value of the lower limit of the hypothetical equivalence range for p_1-p_2
del2	upper limit of the hypothetical equivalence range for $p_1 - p_2$
SW	width of the search grid for determining the maximum of the rejection probabil- ity on the common boundary of the hypotheses
tolrd	horizontal distance of the left- and right-most boundary point to be included in the search grid
tol	upper bound to the absolute difference between size and target level below which the search for a corrected nominal level terminates
maxh	maximum number of interval halving steps to be carried out in finding the max- imally raised nominal level
NH	number of interval-halving steps actually performed
ALPH_0	value of the raised nominal level obtained after NH steps
SIZE0	size of the critical region corresponding to α_0
ERROR	error indicator answering the question of whether or not the sufficient condition for the correctness of the result output by the program, was satisfied

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 6.6.6.

Examples

bi2diffac(0.05,20,20,0.40,0.40,0.1,1e-6,1e-4,3)

bi2dipow	Exact rejection probability of the asymptotic test for equivalence of two unrelated binomial proportions with respect to the difference of their expectations at any nominal level under an arbitrary parameter configuration

Description

The program computes exact values of the rejection probability of the asymptotic test for equivalence in the sense of $-\delta_1 < p_1 - p_2 < \delta_2$, at any nominal level α_0 . [The largest α_0 for which the test is valid in terms of the significance level, can be computed by means of the program bi2diffac.]

bi2dipow

Usage

bi2dipow(alpha0,m,n,del1,del2,p1,p2)

Arguments

alpha0	nominal significance level
m	size of Sample 1
n	size of Sample 2
del1	absolute value of the lower limit of the hypothetical equivalence range for $p_1 - p_2$
del2	upper limit of the hypothetical equivalence range for $p_1 - p_2$
p1	true value of the success probability in Population 1
p2	true value of the success probability in Population 2

Value

alpha0	nominal significance level
m	size of Sample 1
n	size of Sample 2
del1	absolute value of the lower limit of the hypothetical equivalence range for $p_1 - p_2$
del2	upper limit of the hypothetical equivalence range for $p_1 - p_2$
p1	true value of the success probability in Population 1
p2	true value of the success probability in Population 2
POWEXØ	exact rejection probability under (p_1, p_2) of the test at nominal level α_0 for equivalence of two binomial distributions with respect to the difference of the success probabilities
ERROR	error indicator answering the question of whether or not the sufficient condition for the correctness of the result output by the program, was satisfied

Author(s)

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 6.6.6.

Examples

bi2dipow(0.0228,50,50,0.20,0.20,0.50,0.50)

bi2rlv1

Description

The function computes exact values of the power of the randomized UMPU test for relevant differences between two binomial distributions and the conservative nonrandomized version of that test. It is assumed that the samples being available from both distributions are independent.

Usage

bi2rlv1(m,n,rho1,rho2,alpha,p1,p2)

Arguments

m	size of Sample 1
n	size of Sample 2
rho1	lower limit of the hypothetical equivalence range for the odds ratio
rho2	upper limit of the hypothetical equivalence range for the odds ratio
alpha	significance level
p1	true success rate in Population 1
p2	true success rate in Population 2

Value

m	size of Sample 1
n	size of Sample 2
rho1	lower limit of the hypothetical equivalence range for the odds ratio
rho2	upper limit of the hypothetical equivalence range for the odds ratio
alpha	significance level
p1	true success rate in Population 1
p2	true success rate in Population 2
POWNR	power of the nonrandomized version of the test
POW	power of the randomized UMPU test

Author(s)

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 11.3.3.

bi2rlv2

Examples

bi2rlv1(200,300,.6667,1.5,.05,.25,.10)

bi2rlv2

Sample sizes for the exact Fisher type test for relevant differences

Description

The function computes minimum sample sizes required in the randomized UMPU test for relevant differences between two binomial distributions with respect to the odds ratio. Computation is done under the side condition that the ratio m/n has some predefined value λ .

Usage

bi2rlv2(rho1,rho2,alpha,p1,p2,beta,qlambd)

Arguments

rho1	lower limit of the hypothetical equivalence range for the odds ratio
rho2	upper limit of the hypothetical equivalence range for the odds ratio
alpha	significance level
p1	true success rate in Population 1
p2	true success rate in Population 2
beta	target value of power
qlambd	sample size ratio m/n

Value

rho1	lower limit of the hypothetical equivalence range for the odds ratio
rho2	upper limit of the hypothetical equivalence range for the odds ratio
alpha	significance level
p1	true success rate in Population 1
p2	true success rate in Population 2
beta	target value of power
qlambd	sample size ratio m/n
М	minimum size of Sample 1
Ν	minimum size of Sample 2
POW	power of the randomized UMPU test attained with the computed values of m, n

Author(s)

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 11.3.3.

Examples

bi2rlv2(.6667,1.5,.05,.70,.50,.50,2.0)

bi2st	Critical constants for the exact Fisher type UMPU test for equivalence
	of two binomial distributions with respect to the odds ratio

Description

The function computes the critical constants defining the uniformly most powerful unbiased test for equivalence of two binomial distributions with parameters p_1 and p_2 in terms of the odds ratio. Like the ordinary Fisher type test of the null hypothesis $p_1 = p_2$, the test is conditional on the total number S of successes in the pooled sample.

Usage

bi2st(alpha,m,n,s,rho1,rho2)

Arguments

alpha	significance level
m	size of Sample 1
n	size of Sample 2
S	observed total count of successes
rho1	lower limit of the hypothetical equivalence range for the odds ratio $\rho = \frac{p_1(1-p_2)}{p_2(1-p_1)}$
rho2	upper limit of the hypothetical equivalence range for ρ

alpha	significance level
m	size of Sample 1
n	size of Sample 2
S	observed total count of successes
rho1	lower limit of the hypothetical equivalence range for the odds ratio $\rho = \frac{p_1(1-p_2)}{p_2(1-p_1)}$
rho2	upper limit of the hypothetical equivalence range for ρ
C1	left-hand limit of the critical interval for the number X of successes observed in Sample 1
C2	right-hand limit of the critical interval for X
GAM1	probability of rejecting the null hypothesis when it turns out that $X = C_1$
GAM2	probability of rejecting the null hypothesis for $X = C_2$

bi2ste1

Author(s)

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 6.6.4.

Examples

bi2st(.05,225,119,171, 2/3, 3/2)

bi2ste1

Power of the exact Fisher type test for noninferiority

Description

The function computes exact values of the power of the randomized UMPU test for one-sided equivalence of two binomial distributions and its conservative nonrandomized version. It is assumed that the samples being available from both distributions are independent.

Usage

bi2ste1(m, n, eps, alpha, p1, p2)

Arguments

m	size of Sample 1
n	size of Sample 2
eps	noninferiority margin to the odds ratio ρ , defined to be the maximum acceptable deviation of the true value of ρ from unity
alpha	significance level
p1	success rate in Population 1
p2	success rate in Population 2

m	size of Sample 1
n	size of Sample 2
eps	noninferiority margin to the odds ratio ρ , defined to be the maximum acceptable deviation of the true value of ρ from unity
alpha	significance level
р1	success rate in Population 1
p2	success rate in Population 2
POWNR	power of the nonrandomized version of the test
POW	power of the randomized UMPU test

Author(s)

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, 6.6.1.

Examples

bi2ste1(106,107,0.5,0.05,0.9245,0.9065)

bi2ste2

Sample sizes for the exact Fisher type test for noninferiority

Description

Sample sizes for the exact Fisher type test for noninferiority

Usage

bi2ste2(eps, alpha, p1, p2, bet, qlambd)

Arguments

eps	noninferiority margin to the odds ratio
alpha	significance level
p1	success rate in Population 1
p2	success rate in Population 2
bet	target power value
qlambd	sample size ratio m/n

Details

The program computes the smallest sample sizes m,n satisfying $m/n = \lambda$ required for ensuring that the power of the randomized UMPU test does not fall below β .

eps	noninferiority margin to the odds ratio
alpha	significance level
p1	success rate in Population 1
p2	success rate in Population 2
bet	target power value

bi2ste3

qlambd	sample size ratio m/n
Μ	minimum size of Sample 1
Ν	minimum size of Sample 2
POW	power of the randomized UMPU test attained with the computed values of m, n

Author(s)

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, 6.6.1.

Examples

bi2ste2(0.5,0.05,0.9245,0.9065,0.80,1.00)

bi2ste3	Determination of a maximally raised nominal significance level for the
	nonrandomized version of the exact Fisher type test for noninferiority

Description

The objective is to raise the nominal significance level as far as possible without exceeding the target significance level in the nonrandomized version of the test. The approach goes back to R.D. Boschloo (1970) who used the same technique for reducing the conservatism of the traditional nonrandomized Fisher test for superiority.

Usage

bi2ste3(m, n, eps, alpha, sw, tolrd, tol, maxh)

Arguments

m	size of Sample 1
n	size of Sample 2
eps	noninferiority margin to the odds ratio ρ , defined to be the maximum acceptable deviation of the true value of ρ from unity
alpha	target significance level
SW	width of the search grid for determining the maximum of the rejection probabil- ity on the common boundary of the hypotheses
tolrd	horizontal distance from 0 and 1, respectively, of the left- and right-most bound- ary point to be included in the search grid

bi2ste3

tol	upper bound to the absolute difference between size and target level below which the search for a corrected nominal level terminates
maxh	maximum number of interval-halving steps to be carried out in finding the max- imally raised nominal level

Details

It should be noted that, as the function of the nominal level, the size of the nonrandomized test is piecewise constant. Accordingly, there is a nondegenerate interval of "candidate" nominal levels serving the purpose. The limits of such an interval can be read from the output.

Value

m	size of Sample 1
n	size of Sample 2
eps	noninferiority margin to the odds ratio ρ , defined to be the maximum acceptable deviation of the true value of ρ from unity
alpha	target significance level
SW	width of the search grid for determining the maximum of the rejection probabil- ity on the common boundary of the hypotheses
tolrd	horizontal distance from 0 and 1, respectively, of the left- and right-most bound- ary point to be included in the search grid
tol	upper bound to the absolute difference between size and target level below which the search for a corrected nominal level terminates
maxh	maximum number of interval-halving steps to be carried out in finding the max- imally raised nominal level
ALPH_0	current trial value of the raised nominal level searched for
NHST	number of interval-halving steps performed up to now
SIZE	size of the critical region corresponding to α_0

Author(s)

Stefan Wellek <stefan.wellek@zi-mannheim.de> Peter Ziegler <peter.ziegler@zi-mannheim.de>

References

Boschloo RD: Raised conditional level of significance for the 2 x 2- table when testing the equality of two probabilities. Statistica Neerlandica 24 (1970), 1-35.

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, §6.6.2.

Examples

bi2ste3(50, 50, 1/3, 0.05, 0.05, 1e-10, 1e-8, 10)

bi2wld_ni_del	Function to compute corrected nominal levels for the Wald type
	(asymptotic) test for one-sided equivalence of two binomial distribu-
	tions with respect to the difference of success rates

Description

Implementation of the construction described on pp. 183-5 of Wellek S (2010) Testing statistical hypotheses of equivalence and noninferiority. Second edition.

Usage

bi2wld_ni_del(N1,N2,EPS,SW,ALPHA,MAXH)

Arguments

N1	size of Sample 1
N2	size of Sample 2
EPS	noninferiority margin to the difference of success probabilities
SW	width of the search grid for determining the maximum of the rejection probabil- ity on the common boundary of the hypotheses
ALPHA	target significance level
MAXH	maximum number of interval-halving steps

Details

The program computes the largest nominal significance level to be used for determining the critical lower bound to the Wald-type statistic for the problem of testing $H : p_1 \le p_2 - \varepsilon$ versus $K : p_1 < p_2 - \varepsilon$.

N1	size of Sample 1
N2	size of Sample 2
EPS	noninferiority margin to the difference of success probabilities
SW	width of the search grid for determining the maximum of the rejection probabil- ity on the common boundary of the hypotheses
ALPHA	target significance level
MAXH	maximum number of interval-halving steps
ALPHA0	corrected nominal level
SIZE0	size of the critical region of the test at nominal level ALPHA0
SIZE_UNC	size of the test at uncorrected nominal level ALPHA
ERR_IND	indicator taking value 1 when it occurs that the sufficient condition allowing one to restrict the search for the maximum of the rejection probability under the null hypothesis to its boundary, fails to be satisfied; otherwise the indicator retains its default value 0.

Author(s)

Stefan Wellek <stefan.wellek@zi-mannheim.de> Peter Ziegler <peter.ziegler@zi-mannheim.de>

References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 6.6.3.

Examples

bi2wld_ni_del(25,25,.10,.01,.05,10)

cf_reh_exact	Exact confidence bounds to the relative excess heterozygosity (REH)
	exhibited by a SNP genotype distribution

Description

Implementation of the interval estimation procedure described on pp. 305-6 of Wellek S (2010) Testing statistical hypotheses of equivalence and noninferiority. Second edition.

Usage

cf_reh_exact(X1,X2,X3,alpha,SW,TOL,ITMAX)

Arguments

X1	count of homozygotes of the first kind [\leftrightarrow genotype AA]
X2	count of heterozygotes [\leftrightarrow genotype AB]
Х3	count of homozygotes of the second kind [\leftrightarrow genotype BB]
alpha	1 - confidence level
SW	width of the search grid for determining an interval covering the parameter point at which the conditional distribution function takes value α and $1 - \alpha$, respectively
TOL	numerical tolerance to the deviation between the computed confidence limits and their exact values
ITMAX	maximum number of interval-halving steps

Details

The program exploits the structure of the family of all genotype distributions, which is 2-parameter exponential with $\log(REH)$ as one of these parameters.

cf_reh_midp

Value

X1	count of homozygotes of the first kind [\leftrightarrow genotype AA]
X2	count of heterozygotes [\leftrightarrow genotype AB]
Х3	count of homozygotes of the second kind [\leftrightarrow genotype BB]
alpha	1 - confidence level
SW	width of the search grid for determining an interval covering the parameter point at which the conditional distribution function takes value α and $1 - \alpha$, respectively
TOL	numerical tolerance to the deviation between the computed confidence limits and their exact values
ITMAX	maximum number of interval-halving steps
C_l_exact	exact conditional lower $(1 - \alpha)$ -confidence bound to REH
C_r_exact	exact conditional upper $(1 - \alpha)$ -confidence bound to REH

Author(s)

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References

Wellek S, Goddard KAB, Ziegler A: A confidence-limit-based approach to the assessment of Hardy-Weinberg equilibrium. Biometrical Journal 52 (2010), 253-270.

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 9.4.3.

Examples

cf_reh_exact(34,118,96,.05,.1,1E-4,25)

cf_reh_midp Mid-p-value - based confidence bounds to the relative excess heterozygosity (REH) exhibited by a SNP genotype distribution

Description

Implementation of the interval estimation procedure described on pp. 306-7 of Wellek S (2010) Testing statistical hypotheses of equivalence and noninferiority. Second edition.

Usage

cf_reh_midp(X1,X2,X3,alpha,SW,TOL,ITMAX)

Arguments

X1	count of homozygotes of the first kind [\leftrightarrow genotype AA]
X2	count of heterozygotes [\leftrightarrow genotype AB]
Х3	count of homozygotes of the second kind [\leftrightarrow genotype BB]
alpha	1 - confidence level
SW	width of the search grid for determining an interval covering the parameter point at which the conditional distribution function takes value α and $1 - \alpha$, respectively
TOL	numerical tolerance to the deviation between the computed confidence limits and their exact values
ITMAX	maximum number of interval-halving steps

Details

The mid-p algorithm serves as a device for reducing the conservatism inherent in exact confidence estimation procedures for parameters of discrete distributions.

Value

X1	count of homozygotes of the first kind [\leftrightarrow genotype AA]
X2	count of heterozygotes [\leftrightarrow genotype AB]
Х3	count of homozygotes of the second kind [\leftrightarrow genotype BB]
alpha	1 - confidence level
SW	width of the search grid for determining an interval covering the parameter point at which the conditional distribution function takes value α and $1 - \alpha$, respectively
TOL	numerical tolerance to the deviation between the computed confidence limits and their exact values
ITMAX	maximum number of interval-halving steps
C_l_midp	lower $(1 - \alpha)$ -confidence bound to REH based on conditional mid-p-values
C_r_midp	upper $(1 - \alpha)$ -confidence bound to REH based on conditional mid-p-values

Author(s)

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References

Agresti A: Categorical data Analysis (2nd edn). Hoboken, NJ: Wiley, Inc., 2002, Section 1.4.5.

Wellek S, Goddard KAB, Ziegler A: A confidence-limit-based approach to the assessment of Hardy-Weinberg equilibrium. Biometrical Journal 52 (2010), 253-270.

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 9.4.3.

exp1st

Examples

cf_reh_midp(137,34,8,.05,.1,1E-4,25)

exp1st	Critical constants and power against the null alternative of the UMP
	test for equivalence of the hazard rate of a single exponential distribu-
	tion to some given reference value

Description

The function computes the critical constants defining the uniformly most powerful test for the problem $\sigma \leq 1/(1 + \varepsilon)$ or $\sigma \geq (1 + \varepsilon)$ versus $1/(1 + \varepsilon) < \sigma < (1 + \varepsilon)$, with σ denoting the scale parameter [\equiv reciprocal hazard rate] of an exponential distribution.

Usage

exp1st(alpha,tol,itmax,n,eps)

Arguments

alpha	significance level
tol	tolerable deviation from α of the rejection probability at either boundary of the hypothetical equivalence interval
itmax	maximum number of iteration steps
n	sample size
eps	margin determining the hypothetical equivalence range symmetrically on the log-scale

alpha	significance level
tol	tolerable deviation from α of the rejection probability at either boundary of the hypothetical equivalence interval
itmax	maximum number of iteration steps
n	sample size
eps	margin determining the hypothetical equivalence range symmetrically on the log-scale
IT	number of iteration steps performed until reaching the stopping criterion corresponding to TOL
C1	left-hand limit of the critical interval for $T = \sum_{i=1}^{n} X_i$
C2	right-hand limit of the critical interval for $T = \sum_{i=1}^{n} X_i$
ERR1	deviation of the rejection probability from α under $\sigma=1/(1+\varepsilon)$
POWØ	power of the randomized UMP test against the alternative $\sigma = 1$

Author(s)

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 4.2.

Examples

exp1st(0.05,1.0e-10,100,80,0.3)

fstretch	Critical constants and power of the UMPI (uniformly most powerful invariant) test for dispersion equivalence of two Gaussian distribu- tions

Description

The function computes the critical constants defining the optimal test for the problem $\sigma^2/\tau^2 \leq \varrho_1$ or $\sigma^2/\tau^2 \geq \varrho_2$ versus $\varrho_1 < \sigma^2/\tau^2 < \varrho_2$, with (ϱ_1, ϱ_2) as a fixed nonempty interval around unity.

Usage

fstretch(alpha,tol,itmax,ny1,ny2,rho1,rho2)

Arguments

alpha	significance level
tol	tolerable deviation from α of the rejection probability at either boundary of the hypothetical equivalence interval
itmax	maximum number of iteration steps
ny1	number of degrees of freedom of the estimator of σ^2
ny2	number of degrees of freedom of the estimator of $ au^2$
rho1	lower equivalence limit to σ^2/τ^2
rho2	upper equivalence limit to σ^2/τ^2

alpha	significance level
tol	tolerable deviation from α of the rejection probability at either boundary of the hypothetical equivalence interval
itmax	maximum number of iteration steps
ny1	number of degrees of freedom of the estimator of σ^2

ny2	number of degrees of freedom of the estimator of τ^2
rho1	lower equivalence limit to σ^2/τ^2
rho2	upper equivalence limit to σ^2/τ^2
IT	number of iteration steps performed until reaching the stopping criterion corresponding to TOL
C1	left-hand limit of the critical interval for

$$T = \frac{n-1}{m-1} \sum_{i=1}^{m} (X_i - \overline{X})^2 / \sum_{j=1}^{n-1} (Y_j - \overline{Y})^2$$

C2 right-hand limit of the critical interval for

$$T = \frac{n-1}{m-1} \sum_{i=1}^{m} (X_i - \overline{X})^2 / \sum_{j=1}^{n-1} (Y_j - \overline{Y})^2$$

ERR	deviation of the rejection probability from α under $\sigma^2/\tau^2 = \varrho_1$
POWØ	power of the UMPI test against the alternative $\sigma^2/ au^2=1$

Note

If the two independent samples under analysis are from exponential rather than Gaussian distributions, the critical constants computed by means of fstretch with $\nu_1 = 2m$, $\nu_2 = 2n$, can be used for testing for equivalence with respect to the ratio of hazard rates. The only difference is that the ratio of sample means rather than variances has to be used as the test statistic then.

Author(s)

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 6.5.

Examples

fstretch(0.05, 1.0e-10, 50,40,45,0.5625,1.7689)

gofhwex

Critical constants of the exact UMPU test for approximate compatibility of a SNP genotype distribution with the Hardy-Weinberg model

Description

The function computes the critical constants defining the uniformly most powerful unbiased test for equivalence of the population distribution of the three genotypes distinguishable in terms of a single nucleotide polymorphism (SNP), to a distribution being in Hardy-Weinberg equilibrium (HWE). The test is conditional on the total count S of alleles of the kind of interest, and the parameter θ , in terms of which equivalence shall be established, is defined by $\theta = \frac{\pi_2^2}{\pi_1(1-\pi_1-\pi_2)}$, with π_1 and π_2 denoting the population frequence of homozygotes of the 1st kind and heterozygotes, respectively.

Usage

gofhwex(alpha,n,s,del1,del2)

Arguments

alpha	significance level
n	number of genotyped individuals
S	observed count of alleles of the kind of interest
del1	absolute value of the lower equivalence limit to $\theta/4-1$
del2	upper equivalence limit to $\theta/4-1$

Value

alpha	significance level
n	number of genotyped individuals
S	observed count of alleles of the kind of interest
del1	absolute value of the lower equivalence limit to $\theta/4-1$
del2	upper equivalence limit to $\theta/4 - 1$
C1	left-hand limit of the critical interval for the observed number X_2 of heterozygotes
C2	right-hand limit of the critical interval for the observed number X_2
GAM1	probability of rejecting the null hypothesis when it turns out that $X_2 = C_1$
GAM2	probability of rejecting the null hypothesis for $X_2 = C_2$

Author(s)

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gofhwex_1s

References

Wellek S: Tests for establishing compatibility of an observed genotype distribution with Hardy-Weinberg equilibrium in the case of a biallelic locus. Biometrics 60 (2004), 694-703.

Goddard KAB, Ziegler A, Wellek S: Adapting the logical basis of tests for Hardy-Weinberg equilibrium to the real needs of association studies in human and medical genetics. Genetic Epidemiology 33 (2009), 569-580.

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 9.4.2.

Examples

gofhwex(0.05,475,429,1-1/1.96,0.96)

gofhwex_1s Critical constants of the exact UMPU test for absence of a substantial deficit of heterozygotes as compared with a HWE-compliant SNP genotype distribution [noninferiority version of the test implemented by means of gofhwex]

Description

The function computes the critical constants defining the UMPU test for one-sided equivalence of the population distribution of a SNP, to a distribution being in Hardy-Weinberg equilibrium (HWE). A substantial deficit of heterozygotes is defined to occur when the true value of the parametric function $\omega = \frac{\pi_2/2}{\sqrt{\pi_1\pi_3}}$ [called relative excess heterozygosity (REH)] falls below unity by more than some given margin δ_0 .

Like its two-sided counterpart [see the description of the R function gofhwex], the test is conditional on the total count S of alleles of the kind of interest.

Usage

gofhwex_1s(alpha,n,s,del0)

Arguments

alpha	significance level
n	number of genotyped individuals
S	observed count of alleles of the kind of interest
del0	noninferiority margin for ω , which has to satisfy $\omega > 1 - \delta_0$ under the alternative hypothesis to be established

Value

alpha	significance level
n	number of genotyped individuals
S	observed count of alleles of the kind of interest
del0	noninferiority margin for ω , which has to satisfy $\omega > 1 - \delta_0$ under the alternative hypothesis to be established
С	left-hand limit of the critical interval for the observed number X_2 of heterozy- gotes
GAM	probability of rejecting the null hypothesis when it turns out that $X_2 = C$

Author(s)

Stefan Wellek <stefan.wellek@zi-mannheim.de> Peter Ziegler <peter.ziegler@zi-mannheim.de>

References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, pp. 300-302.

Examples

```
gofhwex_1s(0.05,133,65,1-1/1.96)
```

gofind_t	Establishing approximate independence in a two-way contingency ta-
	ble: Test statistic and critical bound

Description

The function computes all quantities required for carrying out the asymptotic test for approximate independence of two categorial variables derived in \S 9.2 of Wellek S (2010) Testing statistical hypotheses of equivalence and noninferiority. Second edition.

Usage

```
gofind_t(alpha,r,s,eps,xv)
```

Arguments

alpha	significance level
r	number of rows of the contingency table under analysis
S	number of columns of the contingency table under analysis
eps	margin to the Euclidean distance between the vector π of true cell probabilities and the associated vector of products of marginal totals
xv	row vector of length $r \cdot s$ whose $(i - 1)s + j$ -th component is the entry in cell (i, j) of the $r \times s$ contingency table under analysis $i = 1,, r, j = 1,, s$.

gofsimpt

Value

n	size of the sample to which the input table relates
alpha	significance level
r	number of rows of the contingency table under analysis
S	number of columns of the contingency table under analysis
eps	margin to the Euclidean distance between the vector π of true cell probabilities and the associated vector of products of marginal totals
X(r,s)	observed cell counts
DSQ_OBS	observed value of the squared Euclidean distance
VN	square root of the estimated asymtotic variance of $\sqrt{n}DSQ_OBS$
CRIT	upper critical bound to $\sqrt{n}DSQ_OBS$
REJ	indicator of a positive [=1] vs negative [=0] rejection decision to be taken with the data under analysis

Author(s)

Stefan Wellek <stefan.wellek@zi-mannheim.de> Peter Ziegler <peter.ziegler@zi-mannheim.de>

References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 9.2.

Examples

xv <- c(8, 13, 15, 6, 19, 21, 31, 7)
gofind_t(0.05,2,4,0.15,xv)</pre>

gofsimpt

Establishing goodness of fit of an observed to a fully specified multinomial distribution: test statistic and critical bound

Description

The function computes all quantities required for carrying out the asymptotic test for goodness rather than lack of fit of an observed to a fully specified multinomial distribution derived in \S 9.1 of Wellek S (2010) Testing statistical hypotheses of equivalence and noninferiority. Second edition.

Usage

```
gofsimpt(alpha,n,k,eps,x,pio)
```

gofsimpt

Arguments

alpha	significance level
n	sample size
k	number of categories
eps	margin to the Euclidean distance between the vectors π and π_0 of true and hypothesized cell probabilities
x	vector of length k with the observed cell counts as components
pio	prespecified vector of cell probabilities

Value

alpha	significance level
n	sample size
k	number of categories
eps	margin to the Euclidean distance between the vectors π and π_0 of true and hypothesized cell probabilities
X(1,K)	observed cell counts
PI0(1,K)	hypothecized cell probabilities
DSQPIH_0	observed value of the squared Euclidean distance
VN_N	square root of the estimated asymtotic variance of $\sqrt{n}DSQPIH_0$
CRIT	upper critical bound to $\sqrt{n}DSQPIH_0$
REJ	indicator of a positive [=1] vs negative [=0] rejection decision to be taken with the data under analysis

Author(s)

Stefan Wellek <stefan.wellek@zi-mannheim.de> Peter Ziegler <peter.ziegler@zi-mannheim.de>

References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 9.1.

Examples

```
x<- c(17,16,25,9,16,17)
pio <- rep(1,6)/6
gofsimpt(0.05,100,6,0.15,x,pio)</pre>
```

mawi

Mann-Whitney test for equivalence of two continuous distributions of arbitrary shape: test statistic and critical upper bound

Description

Implementation of the asymptotically distribution-free test for equivalence of two continuous distributions in terms of the Mann-Whitney-Wilcoxon functional. For details see Wellek S (2010) Testing statistical hypotheses of equivalence and noninferiority. Second edition, \S 6.2.

Usage

mawi(alpha,m,n,eps1_,eps2_,x,y)

Arguments

alpha	significance level
m	size of Sample 1
n	size of Sample 2
eps1_	absolute value of the left-hand limit of the hypothetical equivalence range for $\pi_+ - 1/2$
eps2_	right-hand limit of the hypothetical equivalence range for $\pi_+ - 1/2$
х	row vector with the m observations making up Sample1 as components
У	row vector with the n observations making up Sample2 as components

Details

Notation: π_+ stands for the Mann-Whitney functional defined by $\pi_+ = P[X > Y]$, with $X \sim F \equiv$ cdf of Population 1 being independent of $Y \sim G \equiv$ cdf of Population 2.

alpha	significance level
m	size of Sample 1
n	size of Sample 2
eps1_	absolute value of the left-hand limit of the hypothetical equivalence range for $\pi_+ - 1/2$
eps2_	right-hand limit of the hypothetical equivalence range for $\pi_+ - 1/2$
W+	observed value of the U-statistics estimator of π_+
SIGMAH	square root of the estimated asymtotic variance of W_+
CRIT	upper critical bound to $ W_+ - 1/2 - (arepsilon_2' - arepsilon_1')/2 /\hat{\sigma}$
REJ	indicator of a positive [=1] vs negative [=0] rejection decision to be taken with the data under analysis

Author(s)

Stefan Wellek <stefan.wellek@zi-mannheim.de> Peter Ziegler <peter.ziegler@zi-mannheim.de>

References

Wellek S: A new approach to equivalence assessment in standard comparative bioavailability trials by means of the Mann-Whitney statistic. Biometrical Journal 38 (1996), 695-710.

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 6.2.

Examples

```
x <- c(10.3,11.3,2.0,-6.1,6.2,6.8,3.7,-3.3,-3.6,-3.5,13.7,12.6)
y <- c(3.3,17.7,6.7,11.1,-5.8,6.9,5.8,3.0,6.0,3.5,18.7,9.6)
mawi(0.05,12,12,0.1382,0.2602,x,y)
```

mcnasc_ni	Determination of a corrected nominal significance level for the asymp-
	totic test for noninferiority in the McNemar setting

Description

The program computes the largest nominal significance level which can be substituted for the target level α without making the exact size of the asymptotic testing procedure larger than α .

Usage

```
mcnasc_ni(alpha,n,del0,sw,tol,maxh)
```

Arguments

alpha	significance level
n	sample size
del0	absolute value of the noninferiority margin for $\delta := p_{10} - p_{01}$, with p_{10} and p_{01} denoting the probabilities of discordant pairs of both kinds
SW	width of the search grid for determining the maximum of the rejection probabil- ity on the common boundary of the hypotheses
tol	upper bound to the absolute difference between size and target level below which the search for a corrected nominal level terminates
maxh	maximum number of interval halving steps to be carried out in finding the max- imally raised nominal level

mcnby_ni

Value

alpha	significance level
n	sample size
del0	absolute value of the noninferiority margin for $\delta := p_{10} - p_{01}$, with p_{10} and p_{01} denoting the probabilities of discordant pairs of both kinds
SW	width of the search grid for determining the maximum of the rejection probabil- ity on the common boundary of the hypotheses
ALPH_0	value of the corrected nominal level obtained after nh steps
SIZE_UNC	exact size of the rejection region of the test at uncorrected nominal level α
SIZEØ	exact size of the rejection region of the test at nominal level α_0
NH	number of interval-halving steps actually performed

Author(s)

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 5.2.3.

Examples

mcnasc_ni(0.05,50,0.05,0.05,0.0001,5)

mcnby_ni

Bayesian test for noninferiority in the McNemar setting with the difference of proportions as the parameter of interest

Description

The program determines through iteration the largest nominal level α_0 such that comparing the posterior probability of the alternative hypothesis $K_1: \delta > -\delta_0$ to the lower bound $1-\alpha_0$ generates a critical region whose size does not exceed the target significance level α . In addition, exact values of the power against specific parameter configurations with $\delta = 0$ are output.

Usage

mcnby_ni(N,DEL0,K1,K2,K3,NSUB,SW,ALPHA,MAXH)

Arguments

Ν	sample size
DELØ	noninferiority margin to the difference of the parameters of the marginal bino- mial distributions under comparison
K1	Parameter 1 of the Dirichlet prior for the family of trinomial distributions
K2	Parameter 2 of the Dirichlet prior for the family of trinomial distributions
К3	Parameter 3 of the Dirichlet prior for the family of trinomial distributions
NSUB	number of subintervals for partitioning the range of integration
SW	width of the search grid for determining the maximum of the rejection probabil- ity on the common boundary of the hypotheses
ALPHA	target significance level
МАХН	maximum number of interval halving steps to be carried out in finding the max- imally raised nominal level

Details

The program uses 96-point Gauss-Legendre quadrature on each of the NSUB intervals into which the range of integration is partitioned.

Value

Ν	sample size
DEL0	noninferiority margin to the difference of the parameters of the marginal bino- mial distributions under comparison
К1	Parameter 1 of the Dirichlet prior for the family of trinomial distributions
К2	Parameter 2 of the Dirichlet prior for the family of trinomial distributions
К3	Parameter 3 of the Dirichlet prior for the family of trinomial distributions
NSUB	number of subintervals for partitioning the range of integration
SW	width of the search grid for determining the maximum of the rejection probabil- ity on the common boundary of the hypotheses
ALPHA	target significance level
MAXH	maximum number of interval halving steps to be carried out in finding the max- imally raised nominal level
ALPHA0	result of the search for the largest admissible nominal level
SIZEØ	size of the critical region corresponding to α_0
SIZE_UNC	size of the critical region of test at uncorrected nominal level α
POW	power against 7 different parameter configurations with $\delta = 0$

Author(s)

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mcnby_ni_pp

References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 5.2.3.

Examples

mcnby_ni(25,.10,.5,.5,.5,10,.05,.05,5)

<pre>mcnby_ni_pp</pre>	Computation of the posterior probability of the alternative hypothesis	
	of noninferiority in the McNemar setting, given a specific point in the	
	sample space	

Description

Evaluation of the integral on the right-hand side of Equation (5.24) on p. 88 of Wellek S (2010) Testing statistical hypotheses of equivalence and noninferiority. Second edition.

Usage

mcnby_ni_pp(N,DEL0,N10,N01)

Arguments

Ν	sample size
DEL0	noninferiority margin to the difference of the parameters of the marginal bino- mial distributions under comparison
N10	count of pairs with $(X, Y) = (1, 0)$
N01	count of pairs with $(X, Y) = (0, 1)$

Details

The program uses 96-point Gauss-Legendre quadrature on each of 10 subintervals into which the range of integration is partitioned.

Value

Ν	sample size
DEL0	noninferiority margin to the difference of the parameters of the marginal bino- mial distributions under comparison
N10	count of pairs with $(X, Y) = (1, 0)$
NØ1	count of pairs with $(X, Y) = (0, 1)$
PPOST	posterior probability of the alternative hypothesis $K_1: \delta > -\delta_0$ with respect to the noninformative prior determined according to Jeffrey's rule

38

Note

The program uses Equation (5.24) of Wellek S (2010) corrected for a typo in the middle line which must read $(1+\delta_0)/2$

$$\int_{\delta_0}^{(1+\delta_0)/2} \left[B(n_{01}+1/2, n-n_{01}+1) \ p_{01}^{n_{01}-1/2} (1-p_{01})^{n-n_{01}} \right]$$

Author(s)

•

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 5.2.3.

Examples

mcnby_ni_pp(72,0.05,4,5)

mcnemasc	Determination of a corrected nominal significance level for the asymp-	
	totic test for equivalence of two paired binomial proportions with re-	
	spect to the difference of their expectations (McNemar setting)	

Description

The program computes the largest nominal significance level which can be substituted for the target level α without making the exact size of the asymptotic testing procedure larger than α .

Usage

mcnemasc(alpha,n,del0,sw,tol,maxh)

Arguments

alpha	significance level
n	sample size
del0	upper limit set to $ p_{10} - p_{01} $ under the alternative hypothesis of equivalence, with p_{10} and p_{01} denoting the probabilities of discordant pairs of both kinds
SW	width of the search grid for determining the maximum of the rejection probabil- ity on the common boundary of the hypotheses
tol	upper bound to the absolute difference between size and target level below which the search for a corrected nominal level terminates
maxh	maximum number of interval halving steps to be carried out in finding the max- imally raised nominal level

mcnempow

Value

alpha	significance level
n	sample size
del0	upper limit set to $ p_{10} - p_{01} $ under the alternative hypothesis of equivalence, with p_{10} and p_{01} denoting the probabilities of discordant pairs of both kinds
SW	width of the search grid for determining the maximum of the rejection probabil- ity on the common boundary of the hypotheses
ALPH_0	value of the corrected nominal level obtained after nh steps
NH	number of interval-halving steps actually performed
ERROR	error indicator messaging "!!!!!" if the sufficient condition for the correctness of the result output by the program was found violated

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 5.2.2.

Examples

mcnemasc(0.05,50,0.20,0.05,0.0005,5)

mcnempow	Exact rejection probability of the asymptotic test for equivalence of
	two paired binomial proportions with respect to the difference of their
	expectations (McNemar setting)

Description

The program computes exact values of the rejection probability of the asymptotic test for equivalence in the sense of $-\delta_0 < p_{10} - p_{01} < \delta_0$, at any nominal level α . [The largest α for which the test is valid in terms of the significance level, can be computed by means of the program mcnemasc.]

Usage

```
mcnempow(alpha,n,del0,p10,p01)
```

mwtie_fr

Arguments

alpha	nominal significance level
n	sample size
del0	upper limit set to $ \delta $ under the alternative hypothesis of equivalence
p10	true value of $P[X = 1, Y = 0]$
p01	true value of $P[X = 0, Y = 1]$

Value

alpha	nominal significance level
n	sample size
del0	upper limit set to $ \delta $ under the alternative hypothesis of equivalence
p10	true value of $P[X = 1, Y = 0]$
p01	true value of $P[X = 0, Y = 1]$
POW	exact rejection probability of the asymptotic McNemar test for equivalence at nominal level α
ERROR	error indicator messaging "!!!!!" if the sufficient condition for the correctness of the result output by the program was found violated

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, p.84.

Examples

mcnempow(0.024902,50,0.20,0.30,0.30)

mwt	

Analogue of mwtie_xy for settings with grouped data

Description

Implementation of the asymptotically distribution-free test for equivalence of discrete distributions from which grouped data are obtained. Hypothesis formulation is in terms of the Mann-Whitney-Wilcoxon functional generalized to the case that ties between observations from different distributions may occur with positive probability. For details see Wellek S (2010) Testing statistical hypotheses of equivalence and noninferiority. Second edition, p.155.

mwtie_fr

Usage

mwtie_fr(k,alpha,m,n,eps1_,eps2_,x,y)

Arguments

k	total number of grouped values which can be distinguished in the pooled sample
alpha	significance level
m	size of Sample 1
n	size of Sample 2
eps1_	absolute value of the left-hand limit of the hypothetical equivalence range for $\pi_+/(1-\pi_0)-1/2$
eps2_	right-hand limit of the hypothetical equivalence range for $\pi_+/(1-\pi_0)-1/2$
х	row vector with the m observations making up Sample1 as components
У	row vector with the n observations making up Sample2 as components

Details

Notation: π_+ and π_0 stands for the functional defined by $\pi_+ = P[X > Y]$ and $\pi_0 = P[X = Y]$, respectively, with $X \sim F \equiv \text{cdf}$ of Population 1 being independent of $Y \sim G \equiv \text{cdf}$ of Population 2.

Value

alpha	significance level
m	size of Sample 1
n	size of Sample 2
eps1_	absolute value of the left-hand limit of the hypothetical equivalence range for $\pi_+/(1-\pi_0)-1/2$
eps2_	right-hand limit of the hypothetical equivalence range for $\pi_+/(1-\pi_0)-1/2$
WXY_TIE	observed value of the U-statistics – based estimator of $\pi_+/(1-\pi_0)$
SIGMAH	square root of the estimated asymtotic variance of $W_+/(1-W_0)$
CRIT	upper critical bound to $ W_+/(1-W_0)-1/2-(arepsilon_2'-arepsilon_1')/2 /\hat{\sigma}$
REJ	indicator of a positive [=1] vs negative [=0] rejection decision to be taken with the data under analysis

Author(s)

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References

Wellek S, Hampel B: A distribution-free two-sample equivalence test allowing for tied observations. Biometrical Journal 41 (1999), 171-186.

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 6.4.

Examples

```
mwtie_xy
```

Distribution-free two-sample equivalence test for tied data: test statistic and critical upper bound

Description

Implementation of the asymptotically distribution-free test for equivalence of discrete distributions in terms of the Mann-Whitney-Wilcoxon functional generalized to the case that ties between observations from different distributions may occur with positive probability. For details see Wellek S (2010) Testing statistical hypotheses of equivalence and noninferiority. Second edition, § 6.4.

Usage

```
mwtie_xy(alpha,m,n,eps1_,eps2_,x,y)
```

Arguments

alpha	significance level
m	size of Sample 1
n	size of Sample 2
eps1_	absolute value of the left-hand limit of the hypothetical equivalence range for $\pi_+/(1-\pi_0)-1/2$
eps2_	right-hand limit of the hypothetical equivalence range for $\pi_+/(1-\pi_0)-1/2$
x	row vector with the m observations making up Sample1 as components
У	row vector with the n observations making up Sample2 as components

Details

Notation: π_+ and π_0 stands for the functional defined by $\pi_+ = P[X > Y]$ and $\pi_0 = P[X = Y]$, respectively, with $X \sim F \equiv \text{cdf}$ of Population 1 being independent of $Y \sim G \equiv \text{cdf}$ of Population 2.

postmys

Value

alpha	significance level
m	size of Sample 1
n	size of Sample 2
eps1_	absolute value of the left-hand limit of the hypothetical equivalence range for $\pi_+/(1-\pi_0)-1/2$
eps2_	right-hand limit of the hypothetical equivalence range for $\pi_+/(1-\pi_0)-1/2$
WXY_TIE	observed value of the U-statistics – based estimator of $\pi_+/(1-\pi_0)$
SIGMAH	square root of the estimated asymtotic variance of $W_+/(1-W_0)$
CRIT	upper critical bound to $ W_+/(1-W_0)-1/2-(arepsilon_2'-arepsilon_1')/2 /\hat{\sigma}$
REJ	indicator of a positive [=1] vs negative [=0] rejection decision to be taken with the data under analysis

Author(s)

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References

Wellek S, Hampel B: A distribution-free two-sample equivalence test allowing for tied observations. Biometrical Journal 41 (1999), 171-186.

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 6.4.

Examples

x <- c(1,1,3,2,2,3,1,1,1,2)
y <- c(2,1,2,2,1,1,2,2,2,1,1,2)
mwtie_xy(0.05,10,12,0.10,0.10,x,y)</pre>

postmys

Bayesian posterior probability of the alternative hypothesis in the setting of the one-sample t-test for equivalence

Description

Evaluation of the integral appearing on the right-hand side of equation (3.6) on p. 38 of Wellek S (2010) Testing statistical hypotheses of equivalence and noninferiority. Second edition

Usage

postmys(n,dq,sd,eps1,eps2,tol)

Arguments

n	sample size
dq	mean within-pair difference observed in the sample under analysis
sd	square root of the sample variance of the within-pair differences
eps1	absolute value of the left-hand limit of the hypothetical equivalence range for δ/σ_D
eps2	right-hand limit of the hypothetical equivalence range for δ/σ_D
tol	tolerance for the error induced through truncating the range of integration on the right

Details

The program uses 96-point Gauss-Legendre quadrature.

Value

n	sample size
dq	mean within-pair difference observed in the sample under analysis
sd	square root of the sample variance of the within-pair differences
eps1	absolute value of the left-hand limit of the hypothetical equivalence range for δ/σ_D
eps2	right-hand limit of the hypothetical equivalence range for δ/σ_D
tol	tolerance for the error induced through truncating the range of integration on the right
PPOST	posterior probability of the set of all (δ, σ_D) such that $-\varepsilon_1 < \delta/\sigma_D < \varepsilon_2$

Author(s)

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 3.2.

Examples

postmys(23,0.16,3.99,0.5,0.5,1e-6)

powsign

Nonconditional power of the UMPU sign test for equivalence and its nonrandomized counterpart

Description

The program computes for each possible value of the number n_0 of zero observations the power conditional on $N_0 = n_0$ and averages these conditional power values with respect to the distribution of N_0 . Equivalence is defined in terms of the logarithm of the ratio p_+/p_- , where p_+ and p_- denotes the probability of obtaining a positive and negative sign, respectively.

Usage

powsign(alpha,n,eps1,eps2,poa)

Arguments

alpha	significance level
n	sample size
eps1	absolute value of the lower limit of the hypothetical equivalence range for $\log(p_+/p)$.
eps2	upper limit of the hypothetical equivalence range for $\log(p_+/p)$.
роа	probability of a tie under the alternative of interest

Value

alpha	significance level
n	sample size
eps1	absolute value of the lower limit of the hypothetical equivalence range for $\log(p_+/p)$.
eps2	upper limit of the hypothetical equivalence range for $\log(p_+/p)$.
роа	probability of a tie under the alternative of interest
POWNONRD	power of the nonrandomized version of the test against the alternative $p_+ = p = (1-p_\circ)/2$
POW	power of the randomized UMPU test against the alternative $p_+ = p = (1 - p_\circ)/2$

Note

A special case of the test whose power is computed by this program, is the exact conditional equivalence test for the McNemar setting (cf. Wellek 2010, pp. 76-77).

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 5.1.

Examples

powsign(0.06580,50,0.847298,0.847298,0.26)

pow_abe	Confidence innterval inclusion test for average bioequivalence: exact
	power against an arbitrary specific alternative

Description

Evaluation of the integral on the right-hand side of equation (10.11) of p. 317 of Wellek S (2010) Testing statistical hypotheses of equivalence and noninferiority. Second edition

Usage

pow_abe(m,n,alpha,del_0,del,sig)

Arguments

m	sample size in sequence group T(est)/R(eference)
n	sample size in sequence group R(eference)/T(est)
alpha	significance level
del_0	equivalence margin to the absolute value of the log-ratio μ_T^* and μ_R^* of the formulation effects
del	assumed true value of $ \log(\mu_T^*/\mu_R^*) $, with $0 \le \delta < \delta_0$
sig	theoretical standard deviation of the log within-subject bioavailability ratios in each sequence group

Details

The program uses 96-point Gauss-Legendre quadrature.

Value

m	sample size in sequence group T(est)/R(eference)
n	sample size in sequence group R(eference)/T(est)
alpha	significance level
del_0	equivalence margin to the absolute value of the log-ratio μ_T^* and μ_R^* of the formulation effects
del	assumed true value of $ \log(\mu_T^*/\mu_R^*) $, with $0 \le \delta < \delta_0$
POW_ABE	power of the interval inclusion test for average bioequivalence against the specific alternative given by (δ,σ)

po_pbibe

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 10.2.1.

Examples

pow_abe(12,13,0.05,log(1.25),log(1.25)/2,0.175624)

po_pbibe	Bayesian	posterior	probability	of	the	alternative	hypothesis	of
	probabilit	y-based ind	lividual bioe	quiv	alen	ce (PBIBE)		

Description

Implementation of the algorithm presented in \S 10.3.3 of Wellek S (2010) Testing statistical hypotheses of equivalence and noninferiority. Second edition.

Usage

po_pbibe(n,eps,pio,zq,s,tol,sw,ihmax)

Arguments

n	sample size
eps	equivalence margin to an individual log-bioavailability ratio
pio	prespecified lower bound to the probability of obtaining an individual log-bioavailability ratio falling in the equivalence range $(-\varepsilon, \varepsilon)$
zq	mean log-bioavailability ratio observed in the sample under analysis
S	square root of the sample variance of the log-bioavailability ratios
tol	maximum numerical error allowed for transforming the hypothesis of PBIBE into a region in the parameter space of the log-normal distribution assumed to underlie the given sample of individual bioavailability ratios
SW	step width used in the numerical procedure yielding results at a level of accuracy specified by the value chosen for tol
ihmax	maximum number of interval halving steps to be carried out in finding the region specified in the parameter space according to the criterion of PBIBE

Details

The program uses 96-point Gauss-Legendre quadrature.

Value

n	sample size
eps	equivalence margin to an individual log-bioavailability ratio
pio	prespecified lower bound to the probability of obtaining an individual log-bioavailability ratio falling in the equivalence range $(-\varepsilon,\varepsilon)$
zq	mean log-bioavailability ratio observed in the sample under analysis
S	square root of the sample variance of the log-bioavailability ratios
tol	maximum numerical error allowed for transforming the hypothesis of PBIBE into a region in the parameter space of the log-normal distribution assumed to underlie the given sample of individual bioavailability ratios
SW	step width used in the numerical procedure yielding results at a level of accuracy specified by the value chosen for tol
ihmax	maximum number of interval halving steps to be carried out in finding the region specified in the parameter space according to the criterion of PBIBE
PO_PBIBE	posterior probability of the alternative hypothesis of PBIBE

Author(s)

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References

Wellek S: Bayesian construction of an improved parametric test for probability-based individual bioequivalence. Biometrical Journal 42 (2000), 1039-52.

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 10.3.3.

Examples

po_pbibe(20,0.25,0.75,0.17451,0.04169, 10e-10,0.01,100)

sgnrk	Signed rank test for equivalence of an arbitrary continuous distribu- tion of the intraindividual differences in terms of the probability of a positive sign of a Walsh average: test statistic and critical upper bound

Description

Implementation of the paired-data analogue of the Mann-Whitney-Wilcoxon test for equivalence of continuous distributions. The continuity assumption relates to the intraindividual differences D_i . For details see Wellek S (2010) Testing statistical hypotheses of equivalence and noninferiority. Second edition, § 5.4.

sgnrk

Usage

sgnrk(alpha,n,qpl1,qpl2,d)

Arguments

alpha	significance level
n	sample size
qpl1	lower equivalence limit q'_+ to the target functional q_+
qpl2	upper equivalence limit q_+'' to the target functional q_+
d	row vector with the intraindividual differences for all n pairs as components

Details

 q_+ is the probability of getting a positive sign of the so-called Walsh-average of a pair of withinsubject differences and can be viewed as a natural paired-observations analogue of the Mann-Whitney functional $\pi_+ = P[X > Y]$.

Value

alpha	significance level
n	sample size
qpl1	lower equivalence limit q'_+ to the target functional q_+
qpl2	upper equivalence limit q_{+}'' to the target functional q_{+}
U_pl	observed value of the U-statistics estimator of q_+
SIGMAH	square root of the estimated asymtotic variance of U_+
CRIT	upper critical bound to $\left U_+ - \left(q'_+ + q''_+ ight)/2 ight /\hat{\sigma}$
REJ	indicator of a positive [=1] vs negative [=0] rejection decision to be taken with the data under analysis

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 5.4.

Examples

srktie_d

Generalized signed rank test for equivalence for tied data: test statistic and critical upper bound

Description

Implementation of a generalized version of the signed-rank test for equivalence allowing for arbitrary patterns of ties between the within-subject differences. For details see Wellek S (2010) Testing statistical hypotheses of equivalence and noninferiority. Second edition, \S 5.5.

Usage

srktie_d(n,alpha,eps1,eps2,d)

Arguments

n	sample size
alpha	significance level
eps1	absolute value of the left-hand limit of the hypothetical equivalence range for $q_+/(1-q_0)-1/2$
eps2	right-hand limit of the hypothetical equivalence range for $q_+/(1-q_0) - 1/2$
d	row vector with the intraindividual differences for all n pairs as components

Details

Notation: q_+ and q_0 stands for the functional defined by $q_+ = P[D_i + D_j > 0]$ and $q_0 = P[D_i + D_j = 0]$, respectively, with D_i and D_j as the intraindividual differences observed in two individuals independently selected from the underlying bivariate population.

Value

n	sample size
alpha	significance level
eps1	absolute value of the left-hand limit of the hypothetical equivalence range for $q_+/(1-q_0)-1/2$
eps2	right-hand limit of the hypothetical equivalence range for $q_+/(1-q_0) - 1/2$
U_pl	observed value of the U-statistics estimator of q_+
U_0	observed value of the U-statistics estimator of q_0
UAS_PL	observed value of $U_+/(1-U_0)$
TAUHAS	square root of the estimated asymtotic variance of $\sqrt{n}U_+/(1-U_0)$
CRIT	upper critical bound to $\sqrt{n} U_+/(1-U_0)-1/2-(arepsilon_2-arepsilon_1)/2 /\hat{ au}$
REJ	indicator of a positive [=1] vs negative [=0] rejection decision to be taken with the data under analysis

srktie_m

Note

The function srktie_d can be viewed as the paired-data analogue of mwtie_xy

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 5.5.

Examples

srktie_m	Analogue of srktie_d for settings where the distribution of intraindi-
	vidual differences is concentrated on a finite lattice

Description

Analogue of the function srktie_d tailored for settings where the distribution of the within-subject differences is concentrated on a finite lattice. For details see Wellek S (2010) Testing statistical hypotheses of equivalence and noninferiority. Second edition, pp.112-3.

Usage

```
srktie_m(n,alpha,eps1,eps2,w,d)
```

Arguments

n	sample size
alpha	significance level
eps1	absolute value of the left-hand limit of the hypothetical equivalence range for $q_{+}/(1-q_{0})-1/2$
eps2	right-hand limit of the hypothetical equivalence range for $q_+/(1-q_0) - 1/2$
W	span of the lattice in which the intraindividual differences take their values
d	row vector with the intraindividual differences for all n pairs as components

Details

Notation: q_+ and q_0 stands for the functional defined by $q_+ = P[D_i + D_j > 0]$ and $q_0 = P[D_i + D_j = 0]$, respectively, with D_i and D_j as the intraindividual differences observed in two individuals independently selected from the underlying bivariate population.

Value

n	sample size
alpha	significance level
eps1	absolute value of the left-hand limit of the hypothetical equivalence range for $q_+/(1-q_0)-1/2$
eps2	right-hand limit of the hypothetical equivalence range for $q_+/(1-q_0)-1/2$
W	span of the lattice in which the intraindividual differences take their values
U_pl	observed value of the U-statistics estimator of q_+
U_0	observed value of the U-statistics estimator of q_0
UAS_PL	observed value of $U_+/(1-U_0)$
TAUHAS	square root of the estimated asymtotic variance of $\sqrt{n}U_+/(1-U_0)$
CRIT	upper critical bound to $\sqrt{n} U_+/(1-U_0)-1/2-(arepsilon_2-arepsilon_1)/2 /\hat{ au}$
REJ	indicator of a positive [=1] vs negative [=0] rejection decision to be taken with the data under analysis

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, pp. 112-114.

Examples

tt1st

Critical constants and power against the null alternative of the onesample t-test for equivalence with an arbitrary, maybe nonsymmetric choice of the limits of the equivalence range

Description

The function computes the critical constants defining the uniformly most powerful invariant test for the problem $\delta/\sigma_D \leq \theta_1$ or $\delta/\sigma_D \geq \theta_2$ versus $\theta_1 < \delta/\sigma_D < \theta_2$, with (θ_1, θ_2) as a fixed nondegenerate interval on the real line. In addition, tt1st outputs the power against the null alternative $\delta = 0$.

Usage

tt1st(n,alpha,theta1,theta2,tol,itmax)

Arguments

n	sample size
alpha	significance level
theta1	lower equivalence limit to δ/σ_D
theta2	upper equivalence limit to δ/σ_D
tol	tolerable deviation from α of the rejection probability at either boundary of the hypothetical equivalence interval
itmax	maximum number of iteration steps

Value

n	sample size
alpha	significance level
theta1	lower equivalence limit to δ/σ_D
theta2	upper equivalence limit to δ/σ_D
IT	number of iteration steps performed until reaching the stopping criterion corresponding to TOL
C1	left-hand limit of the critical interval for the one-sample t-statistic
C2	right-hand limit of the critical interval for the one-sample t-statistic
ERR1	deviation of the rejection probability from α under $\delta/\sigma_D = \theta_1$
ERR2	deviation of the rejection probability from α under $\delta/\sigma_D = \theta_2$
POWØ	power of the UMPI test against the alternative $\delta = 0$

Note

If the output value of ERR2 is NA, the deviation of the rejection probability at the right-hand boundary of the hypothetical equivalence interval from α is smaller than the smallest real number representable in R.

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 5.3.

Examples

tt1st(36,0.05, -0.4716,0.3853,1e-10,50)

tt2	2st
-----	-----

Critical constants and power against the null alternative of the twosample t-test for equivalence with an arbitrary, maybe nonsymmetric choice of the limits of the equivalence range

Description

The function computes the critical constants defining the uniformly most powerful invariant test for the problem $(\xi - \eta)/\sigma \leq -\varepsilon_1$ or $(\xi - \eta)/\sigma \geq \varepsilon_2$ versus $-\varepsilon_1 < (\xi - \eta)/\sigma < \varepsilon_2$, with ξ and η denoting the expected values of two normal distributions with common variance σ^2 from which independent samples are taken. In addition, tt2st outputs the power against the null alternative $\xi = \eta$.

Usage

tt2st(m,n,alpha,eps1,eps2,tol,itmax)

Arguments

m	size of the sample from $\mathcal{N}(\xi, \sigma^2)$
n	size of the sample from $\mathcal{N}(\eta,\sigma^2)$
alpha	significance level
eps1	absolute value of the lower equivalence limit to $(\xi - \eta)/\sigma$
eps2	upper equivalence limit to $(\xi - \eta)/\sigma$
tol	tolerable deviation from α of the rejection probability at either boundary of the hypothetical equivalence interval
itmax	maximum number of iteration steps

Value

m	size of the sample from $\mathcal{N}(\xi,\sigma^2)$
n	size of the sample from $\mathcal{N}(\eta,\sigma^2)$
alpha	significance level
eps1	absolute value of the lower equivalence limit to $(\xi - \eta)/\sigma$
eps2	upper equivalence limit to $(\xi - \eta)/\sigma$
IT	number of iteration steps performed until reaching the stopping criterion corresponding to TOL
C1	left-hand limit of the critical interval for the two-sample t-statistic
C2	right-hand limit of the critical interval for the two-sample t -statistic
ERR1	deviation of the rejection probability from α under $(\xi - \eta)/\sigma = -\varepsilon_1$
ERR2	deviation of the rejection probability from α under $(\xi - \eta)/\sigma = \varepsilon_2$
POWØ	power of the UMPI test against the alternative $\xi = \eta$

Note

If the output value of ERR2 is NA, the deviation of the rejection probability at the right-hand boundary of the hypothetical equivalence interval from α is smaller than the smallest real number representable in R.

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References

Wellek S: Testing statistical hypotheses of equivalence and noninferiority. Second edition. Boca Raton: Chapman & Hall/CRC Press, 2010, \S 6.1.

Examples

tt2st(12,12,0.05,0.50,1.00,1e-10,50)

Index

* 2x2 contingency table gofind_t, 30 * Bayesian test bi2by_ni_del, 8 bi2by_ni_OR, 10 mcnby_ni, 35 po_pbibe, 47 postmys, 43 * Dirichlet prior mcnby_ni, 35 mcnby_ni_pp, 37 * Euclidean distance statistic gofind_t, 30 gofsimpt, 31 * Gauss-Legendre quadrature bi2by_ni_del, 8 bi2by_ni_OR, 10 mcnby_ni, 35 mcnby_ni_pp, 37 po_pbibe, 47 postmys, 43 * Gaussian data fstretch, 26 * Hardy-Weinberg equilibrium (HWE) gofhwex, 28 gofhwex_1s, 29 * Hardy-Weinberg equilibrium cf_reh_exact, 22 cf_reh_midp, 23 * Jeffrey's rule mcnby_ni_pp, 37 * Jeffreys prior postmys, 43 * Mann-Whitney functional mawi, 33 mwtie_fr, 40 mwtie_xy, 42 * McNemar setting mcnasc_ni, 34

mcnby_ni_pp, 37 mcnemasc, 38 mcnempow, 39 powsign, 45 * U-statistics estimators mwtie_fr, 40 mwtie_xy, 42 srktie_d, 50 srktie_m, 51 * UMP test for equivalence exp1st, 25 * UMP test bi1st, 3 * UMPU test bi2st. 16 powsign, 45 * Wald-type bi2wld_ni_del, 21 * Walsh averages sgnrk, 48 srktie_d, 50 srktie_m, 51 * asymptotic normality gofind_t, 30 gofsimpt, 31mawi, 33 mwtie_fr, 40 mwtie_xy, 42 sgnrk, 48 srktie_d, 50 srktie_m, 51 * asymptotic test for equivalence mcnempow, 39 * asymptotic test bi2diffac, 11 bi2dipow, 12 mcnasc_ni, 34 mcnemasc, 38 * average bioequivalence

INDEX

pow_abe, 46 * binary observations mcnasc_ni, 34 mcnemasc, 38 powsign, 45 * binomial one-sample problem bi1st.3 * binomial two-sample problem bi2aeq1,4 bi2aeq2, 5 bi2aeq3,7 bi2diffac, 11 bi2dipow, 12 bi2rlv1, 14 bi2rlv2, 15 bi2st. 16 bi2ste1, 17 bi2ste2, 18 bi2ste3, 19 * conditional test bi2st. 16 * confidence interval inclusion test pow_abe, 46 * confidence interval inclusion cf_reh_exact, 22 cf reh midp. 23 * continuous observations mawi, 33 sgnrk, 48 * corrected nominal level bi2diffac. 11 mcnasc_ni, 34 mcnemasc, 38 * difference between response probabilities mcnby_ni_pp, 37 * difference of proportions bi2by_ni_del, 8 mcnby_ni, 35 * difference of success probabilities bi2diffac, 11 bi2dipow, 12 * dispersion equivalence fstretch, 26 * equivalence test cf_reh_exact, 22 cf_reh_midp, 23 * equivalence bi1st, 3

bi2aeq1,4 bi2aeq2, 5 bi2aeq3.7 bi2diffac, 11 bi2dipow, 12 bi2st, 16 mcnemasc, 38 powsign, 45 * establishing approximate independence of two categorical variables gofind_t, 30 * exact Fisher-type test nonrandomized version bi2aeq3,7 bi2ste3, 19 * exact Fisher-type test bi2aeq1,4 bi2aeq2,5 bi2rlv1, 14 bi2rlv2, 15 bi2st. 16 bi2ste1, 17 bi2ste2.18 * exact conditional confidence limit cf_reh_exact, 22 * exact conditional test powsign, 45 * exact power bi2dipow, 12 mcnempow, 39 * exponential distribution exp1st, 25 * finite lattice srktie_m, 51 * fully specified multinomial distribution gofsimpt, 31 * genetic association study cf_reh_exact, 22 cf_reh_midp, 23 * goodness of fit cf_reh_exact, 22 cf_reh_midp, 23 * homoskedasticity tt2st, 54 * individual bioequivalence po_pbibe, 47 * lognormal distribution po_pbibe, 47

pow_abe, 46 * matched-pair design with binary data mcnby_ni, 35 * maximally raised nominal level bi2aeq3,7 bi2ste3, 19 * mid-p value cf_reh_midp, 23 * model validation gofhwex, 28 * model verification gofsimpt, 31 * nominal level bi2wld_ni_del, 21 * noncentral t-distribution tt1st. 53 tt2st, 54 * noninferiority bi2by_ni_del, 8 bi2by_ni_OR, 10 bi2ste1.17 bi2ste2, 18 bi2ste3, 19 gofhwex_1s, 29 mcnasc_ni, 34 mcnby_ni, 35 mcnby_ni_pp, 37 * nonparametric paired-sample equivalence test sgnrk, 48 srktie_d, 50 srktie_m, 51 * nonparametric two-sample equivalence test mawi.33 mwtie_fr, 40 mwtie_xy, 42 * normal distribution postmys, 43 * odds ratio bi2aeq1,4 bi2aeq2, 5 bi2aeq3,7 bi2by_ni_OR, 10 bi2rlv1, 14 bi2rlv2, 15 bi2st, 16 bi2ste1, 17

bi2ste2, 18 bi2ste3, 19 * one-dimensional contingency table gofsimpt, 31 * one-sample problem exp1st, 25 * package EQUIVNONINF-package, 2 * paired data postmys, 43 * paired samples mcnasc_ni, 34 mcnemasc. 38 powsign, 45 * paired t-test for equivalence tt1st. 53 * parallel-group design with binary data bi2by_ni_del, 8 bi2by_ni_OR, 10 * posterior probability of the alternative hypothesis mcnby_ni_pp, 37 * power bi1st, 3 bi2aeq1,4 bi2rlv1.14 bi2ste1, 17 exp1st, 25 fstretch, 26 tt1st, 53 tt2st. 54 * product of Jeffrey's priors bi2by_ni_del, 8 bi2by_ni_OR, 10 * randomized test bi1st.3 bi2st, 16 * relative excess heterozygosity (REH) gofhwex_1s, 29 * relative excess heterozygosity cf_reh_exact, 22 cf_reh_midp, 23 * relevant differences bi2rlv1, 14 bi2rlv2, 15 * sample size bi2aeq2, 5 bi2rlv2, 15

INDEX

bi2ste2, 18 fstretch, 26 * single nucleotide polymorphism (SNP) gofhwex, 28gofhwex, 28gofhwex_1s, 29 gofhwex_1s, 29 gofind_t, 30 * standardized difference of means gofsimpt, 31 postmys, 43 tt1st, 53 mawi, 33 tt2st, 54 mcnasc_ni, 34 * tied observations mcnby_ni, 35 mwtie_fr, 40 mcnby_ni_pp, 37 mwtie_xy, 42 mcnemasc, 38 srktie_d, 50 mcnempow, 39 srktie_m, 51 mwtie_fr, 40 * two-period crossover mwtie_xy, 42 pow_abe, 46 * two-sample problem po_pbibe, 47 fstretch, 26 postmys, 43* two-sample t-test for equivalence pow_abe, 46 tt2st, <mark>54</mark> powsign, 45 * uniformly most powerful invariant test fstretch, 26 sgnrk, 48 tt1st, 53 srktie_d, 50 tt2st, 54 srktie_m, 51 * uniformly most powerful unbiased test gofhwex, 28 tt1st, 53 gofhwex_1s, 29 tt2st, 54 bi1st.3 bi2aeq1,4 bi2aeq2, 5 bi2aeq3,7 bi2by_ni_del, 8 bi2by_ni_OR, 10 bi2diffac, 11 bi2dipow, 12 bi2rlv1, 14 bi2rlv2, 15 bi2st, 16 bi2ste1, 17 bi2ste2, 18 bi2ste3, 19 bi2wld_ni_del, 21 cf_reh_exact, 22 cf_reh_midp, 23 EQUIVNONINF (EQUIVNONINF-package), 2 EQUIVNONINF-package, 2exp1st, 25