Package 'IsoCheck'

March 25, 2020

Title Isomorphism Check for Multi-Stage Factorial Designs with

Randomization Restrictions

Version 0.1.0
Date 2020-03-20
Author Neil Spencer [aut, cre], Pritam Ranjan [aut,cre], Franklin Mendivil [ctb]
Maintainer Pritam Ranjan <pritam.ranjan@gmail.com></pritam.ranjan@gmail.com>
Description Contains functions to check the isomorphism of multi-stage factorial designs with randomisation restrictions based on balanced spreads and balanced covering stars of PG(n-1,2) as described in Spencer, Ranjan and Mendivil (2019) <doi:10.1007 s42519-019-0064-5="">.</doi:10.1007>
License GPL-2
Imports gtools, dplyr, plyr
NeedsCompilation no
Repository CRAN
Date/Publication 2020-03-25 15:40:02 UTC
R topics documented:
applyCollineation checkSpreadEquivalence checkSpreadIsomorphism checkStarEquivalence checkStarIsomorphism getBitstrings is.spread is.spread is.spread is.star spreadn4t2a spreadn4t2b

 spreadn6t2a
 15

 spreadn6t2b
 16

 spreadn6t2c
 17

 spreadn6t3a
 18

 spreadn6t3b
 19

2 applyCollineation

apply		R	ela	ıb	el	a	Sp	re	aa	l o	rS	Sta	ır	wi	th	a	C	oli	lin	ea	tic	n	M	ati	rix	c							
Index																																	28
	vectortostring							•									•					•	•			•				•		•	26
	stringtovector																																
	star_to_spread																																24
	starn8t5b																																23
	starn8t5a																																22
	starn5t3b																																
	starn5t3a																																

Description

This function relabels a balanced (t-1)-spread or a covering star $St(n, \mu, t, t_0)$ of PG(n-1,2) according to the specified collineation matrix.

Usage

```
applyCollineation(C, spr)
```

Arguments

С A binary n by n matrix representing a collineation of PG(n-1, 2).

A balanced spread or star of PG(n-1,2) stored as a three dimensional binary spr

array (see Details and Examples of checkSpreadEquivalence).

Details

This code applies the relabelling corresponding to a collineation matrix C to any given balanced spread or star of PG(n-1, 2). The spread should be formatted as a 3-dimensional array with spr[i,j,k] indicating whether or not the ith basic factor is present in the jth effect of the kth flat of spr. The collineation is applied via a matrix multiplication modulo 2 (i.e., the calculations are done over GF(2)). See Spencer et al. (2019) for details.

Value

A spread or star of the same dimensions as spr.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2ⁿ Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

checkSpreadIsomorphism for checking the isomorphism of balanced spreads. checkStarIsomorphism for checking the isomorphism of balanced covering stars.

Examples

```
## Example 1: relabelling a 1-spread of PG(3,2)
data(spreadn4t2a)
Collin <- cbind(c(1,0,0,1), c(0,0,1,1), c(1,1,1,1), c(0,1,1,1))
# Collin is the collineation matrix corresponding to
# A -> AD, B -> CD, C -> ABCD, D -> BCD
applyCollineation(Collin, spreadn4t2a)

## Example 2: Relabelling a star of PG(4,2) consisting of 4-flats.
data(starn5t3a)
Collin2 <- cbind(c(0,0,0,0,1), c(1,0,0,0,0), c(0,1,0,0,0), c(0,0,0,1,0), c(0,0,1,0,0))
# Collin2 is the collineation matrix corresponding to
# A -> E, B -> A, C -> B, D -> D, E -> C
applyCollineation(Collin2, starn5t3a)
```

checkSpreadEquivalence

Checking the Equivalence of Two Spreads

Description

This function checks the equivalence of two (t-1)-spreads of PG(n-1,2) by comparing their sorted bitstring representations.

Usage

checkSpreadEquivalence(spread1, spread2)

Arguments

spread1 A (t-1)-spread of PG(n-1,2) stored as a three dimensional binary array (see

Details and Examples).

spread2 A (t-1)-spread of PG(n-1,2) stored as a three dimensional binary array (see

Details and Examples).

Details

This code checks if two (t-1)-spreads of PG(n-1,2) are equivalent using the bitstring representation of Spencer et al. (2019). Both input spreads should be formatted as 3-dimensional arrays, for example, spread1[i,j,k] indicates whether or not the ith basic factor is present in the jth effect of the kth flat of spread1.

Value

A Boolean indicating whether or not the two spreads are equivalent.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2^n Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

checkSpreadIsomorphism for checking the isomorphism of spreads. checkStarEquivalence for checking the equivalence of two stars.

Examples

```
## Example 1: two non-equivalent 1-spreads of PG(3,2)
data(spreadn4t2a)
data(spreadn4t2b)
# test their equivalence
(test1 <- checkSpreadEquivalence(spreadn4t2a, spreadn4t2b))</pre>
# direct instantiation of a spread
spreadn4t2c <- array(NA, c(4,3,5))
spreadn4t2c[,1,1] <- c(0, 0, 0, 1)
spreadn4t2c[,2,1] \leftarrow c(0, 1, 1, 0)
spreadn4t2c[,3,1] <- c(0, 1, 1, 1)
spreadn4t2c[,1,2] \leftarrow c(0, 0, 1, 0)
spreadn4t2c[,2,2] <- c(1, 1, 0, 0)
spreadn4t2c[,3,2] \leftarrow c(1, 1, 1, 0)
spreadn4t2c[,1,3] \leftarrow c(0, 1, 0, 0)
spreadn4t2c[,2,3] <- c(1, 0, 1, 1)
spreadn4t2c[,3,3] <- c(1, 1, 1, 1)
spreadn4t2c[,1,4] <- c(1, 0, 0, 0)
spreadn4t2c[,2,4] \leftarrow c(0, 1, 0, 1)
spreadn4t2c[,3,4] <- c(1, 1, 0, 1)
spreadn4t2c[,1,5] <- c(0, 0, 1, 1)
spreadn4t2c[,2,5] <- c(1, 0, 1, 0)
spreadn4t2c[,3,5] <- c(1, 0, 0, 1)
(test2 <- checkSpreadEquivalence(spreadn4t2a, spreadn4t2c))</pre>
```

```
## Example 2: two equivalent 2-spreads of PG(5,2)
data(spreadn6t3a)

# permute the flats and flat order of spreadn6t3a to create a
# second equivalent spread equiv_spreadn6t3a.

equiv_spreadn6t3a <- spreadn6t3a
dims <- dim(equiv_spreadn6t3a)
for(i in 1:(dims[3])){
    equiv_spreadn6t3a[,,i] <- equiv_spreadn6t3a[,sample(1:dims[2], dims[2]),i]
} equiv_spreadn6t3a <- equiv_spreadn6t3a[,,sample(1:dims[3], dims[3])]

(test3 <- checkSpreadEquivalence(spreadn6t3a, equiv_spreadn6t3a))</pre>
```

checkSpreadIsomorphism

Checking the Isomorphism of Two Spreads

Description

This function checks the isomorphism of two (t-1)-spreads of PG(n-1,2). If they are isomorphic, it returns the list of isomorphism establishing collineations (IECs). The option is provided to enumerate all IECs or to terminate after the first one is found.

Usage

checkSpreadIsomorphism(spread1, spread2, returnfirstIEC = FALSE, printstatement = TRUE)

Arguments

spread1	A (t-1)-spread of PG(n-1,2) stored as a three dimensional binary array (see Details and Examples of checkSpreadEquivalence).
spread2	A (t-1)-spread of PG(n-1,2) stored as a three dimensional binary array (see Details and Examples of checkSpreadEquivalence).
returnfirstIEC	An indicator to indicate whether all isomorphism establishing collineations should be returned (default), or terminate only after the first one is found.
printstatement	If set to true (default), running the function also prints a sentence declaring the isomorphism of the spreads.

Details

This code considers all possible collineations of PG(n-1,2) to search for isomorphism establishing collineations (IECs) from spread1 to spread2. The search is conducted over the reduced space described in Algorithm 1 of Spencer et al. (2019). Equivalence is assessed using the bitstring comparison method described in Spencer et al. (2019).

Both input spreads should be formatted as 3-dimensional arrays with spread1[i,j,k] indicating whether or not the ith basic factor is present in the jth effect of the kth flat of spread1.

Value

A list containing two objects. The first object is a Boolean indicating whether or not spread1 is isomorphic to spread2. If isomorphic, the second object is a list of isomorphism establishing collineation matrices. If not isomorphic, the second object is NA.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2ⁿ Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

checkStarIsomorphism for checking the isomorphism of balanced covering stars. checkSpreadEquivalence for checking the equivalence of balanced spreads.

Examples

```
## Example 1: two 1-spreads of PG(3,2)
data(spreadn4t2a)
data(spreadn4t2b)
# test their isomorphism
test1 <- checkSpreadIsomorphism(spreadn4t2a, spreadn4t2b)</pre>
test1$result # the test indicates that they are isomorphic
(IEC1 <- (test1$IECs)[[1]])
# we store the first isomorphism establishing collineation as IEC1
## Example 2: two 2-spreads of PG(5,2) using returnfirstIEC to cut down on runtime
data(spreadn6t3a)
data(spreadn6t3b)
test2 <- checkSpreadIsomorphism(spreadn6t3a, spreadn6t3b, returnfirstIEC = TRUE)</pre>
test2$result # the test indicates that they are isomorphic
## Example 3: non-isomorphic 1-spreads of PG(5,2)
data(spreadn6t2a)
data(spreadn6t2c)
# A bit slow for official example
```

checkStarEquivalence 7

```
# test3 <- checkSpreadIsomorphism(spreadn6t2a, spreadn6t2c, returnfirstIE#C = TRUE)
# test3$result

## Example 4: isomorphic 1-spreads of PG(5,2)
data(spreadn6t2a)
data(spreadn6t2b)
test4 <- checkSpreadIsomorphism(spreadn6t2a, spreadn6t2b, returnfirstIEC = TRUE)
test4$result # the test indicates that they are isomorphic</pre>
```

checkStarEquivalence Checking the Equivalence of Two Stars

Description

This function checks the equivalence of two balanced covering stars of PG(n-1,2) by comparing sorted bitstring representations.

Usage

checkStarEquivalence(star1, star2)

Arguments

star1	A star of PG(n-1,2) stored as a three dimensional binary array (see Details and Examples of checkSpreadEquivalence).
star2	A star of PG(n-1,2) stored as a three dimensional binary array (see Details and Examples of checkSpreadEquivalence).

Details

This code checks if two stars of PG(n-1,2) are equivalent using the bitstring representation of Spencer et al. (2019). Both input stars should be formatted as 3-dimensional arrays with spread1[i,j,k] indicating whether or not the ith basic factor is present in the jth effect of the kth flat of spread1.

Value

A Boolean indicating whether or not the two stars are equivalent.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2ⁿ Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

checkStarIsomorphism for checking the isomorphism of stars. checkSpreadEquivalence for checking the equivalence of spreads.

Examples

```
## Example 1: two non-equivalent stars of PG(4,2)
data(starn5t3a)
data(starn5t3b)

# test their equivalence
(test1 <- checkStarEquivalence(starn5t3a, starn5t3b))

## Example 2: two equivalent stars of PG(7,2) consisting of 6-flats
data(starn8t5a)

#permute the flats and flat order of starn8t5a to create a second equivalent spread equiv_starn8t5a.
equiv_starn8t5a <- starn8t5a
dims <- dim(equiv_starn8t5a)
for(i in 1:(dims[3])){
    equiv_starn8t5a[,,i] <- equiv_starn8t5a[,sample(1:dims[2], dims[2]),i]
} equiv_starn8t5a <- starn8t5a[,,sample(1:dims[3], dims[3])]
(test2 <- checkStarEquivalence(starn8t5a, equiv_starn8t5a))</pre>
```

 ${\it checkStarIsomorphism} \quad {\it Checking the Isomorphism of Two Stars}$

Description

This function checks the isomorphism of two balanced covering stars of PG(n-1,2). If they are isomorphic, it returns the list of isomorphism establishing collineations. The option is provided to enumerate all isomorphism establishing collineations or to terminate after the first one is found.

Usage

```
checkStarIsomorphism(star1, star2, returnfirstIEC = FALSE)
```

Arguments

star1	A star of PG(n-1,2) stored as a three dimensional binary array (see Details and Examples of checkSpreadEquivalence).
star2	A star of PG(n-1,2) stored as a three dimensional binary array (see Details and Examples of checkSpreadEquivalence).

returnfirstIEC An indicator of whether all isomorphism establishing collineations (IECs) should be returned (default), or terminate only after the first one is found.

Details

This code considers all possible collineations of PG(n-1,2) to search for isomorphism establishing collineations from star1 to star2. The search is conducted by first projecting onto a lower dimensional space described as Algorithm 2 in Spencer et al. (2019). Equivalence is assessed using the bitstring comparison method described in Spencer et al. (2019). Both input stars should be formatted as 3-dimensional arrays with star1[i,j,k] indicating whether or not the ith basic factor is present in the jth effect of the kth flat of star1.

Value

A list containing two objects. The first object is a Boolean indicating whether or not star1 is isomorphic to star2. If isomorphic, the second object is a list of isomorphism establishing collineation matrices. If not isomorphic, the second object is NA.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2^n Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

checkSpreadIsomorphism for checking the isomorphism of spreads. checkStarEquivalence for checking the equivalence of stars.

Examples

```
## Example 1: Two stars of PG(4,2) consisting of 4-flats
data(starn5t3a)
data(starn5t3b)
test1 <- checkStarIsomorphism(starn5t3a, starn5t3b, returnfirstIEC = TRUE)
test1$result # the test indicates that they are isomorphic
(IECstar <- test1$IECs[[1]]) # the first IEC

## Example 2: Two stars of PG(7,2) consisting of 6-flats
data(starn8t5a)
data(starn8t5b)
test2 <- checkStarIsomorphism(starn8t5a, starn8t5b, returnfirstIEC = TRUE)
test2$result</pre>
```

10 getBitstrings

getBitstrings

Bitstring Representation of a Spread or Star

Description

This function computes a bitstring representation for a spread or star of PG(n-1, 2)

Usage

```
getBitstrings(spr)
```

Arguments

spr

A spread or star of PG(n-1,2) stored as a three dimensional binary array (see Details and Examples of checkSpreadEquivalence).

Details

This code obtains the bitstring representation (as described in Spencer et al. 2019) for any given spread or star of PG(n-1,2). The spread should be formatted as a 3-dimensional array with spr[i,j,k] indicating whether or not the ith basic factor is present in the jth effect of the kth flat of spr. This representation facilitates fast equivalence checking for spreads or stars.

Value

A matrix with each row characterizing the elements of a distinct flat in spr.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2^n Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

checkSpreadEquivalence for checking equivalence of spreads. checkStarEquivalence for checking equivalence of spreads.

is.spread 11

Examples

```
## Example 1: The bitstring representation of a 1-spread of PG(3,2)
data(spreadn4t2a)
getBitstrings(spreadn4t2a)

## Example 2: The bitstring representation of a star of PG(4,2) consisting of 4-flats.
data(starn5t3a)
getBitstrings(starn5t3a)
```

is.spread

Boolean check for a proper Spread

Description

Checks whether or not the input is a proper balanced (t-1)-spread of PG(n-1, 2).

Usage

```
is.spread(spr, printstatements = TRUE)
```

Arguments

spr

A balanced spread of PG(n-1,2) stored as a three dimensional binary array (see Details and Examples of checkSpreadEquivalence).

printstatements

A Boolean indicating whether or not to print possible reasons for not being a spread if the input is not a spread.

Details

Checks whether or not the input is a proper balanced (t-1)-spread of PG(n-1,2). The spread should be formatted as a 3-dimensional array with spr[i,j,k] indicating whether or not the ith basic factor is present in the jth effect of the kth flat of spr. See Spencer et al. (2019) for details.

Value

A Boolean indicating whether or not the input is a spread.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2ⁿ Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

is.star

See Also

is.star for checking if the input is a balanced covering star. checkSpreadIsomorphism for checking the isomorphism of balanced spreads. checkStarIsomorphism for checking the isomorphism of balanced covering stars.

Examples

```
## Example 1: checking whether "spreadn4t2a" is a proper spread
data(spreadn4t2a)
is.spread(spreadn4t2a)

## Example 2: checking whether "starn5t3a" is a proper spread
data(starn5t3a)
is.spread(starn5t3a)
```

is.star

Boolean check for a proper Star

Description

Checks whether or not the input is a proper balanced covering star of PG(n-1, 2).

Usage

```
is.star(star, printstatements = TRUE)
```

Arguments

star

A balanced covering star of PG(n-1,2) stored as a three dimensional binary array (see Details and Examples of checkSpreadEquivalence).

printstatements

A Boolean indicating whether or not to print possible reasons for not being a star if the input is not a balanced covering star.

Details

Checks whether or not the input is a proper balanced covering star of PG(n-1,2). The star should be formatted as a 3-dimensional array with star[i,j,k] indicating whether or not the ith basic factor is present in the jth effect of the kth flat of star. See Spencer et al. (2019) for details.

Value

A Boolean indicating whether or not the input is a star.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

spreadn4t2a 13

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2ⁿ Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

is.spread for checking if the input is a balanced spread. checkSpreadIsomorphism for checking the isomorphism of balanced spreads. checkStarIsomorphism for checking the isomorphism of balanced covering stars.

Examples

```
## Example 1: checking whether "spreadn4t2a" is a proper star
data(spreadn4t2a)
is.star(spreadn4t2a)

## Example 2: checking whether "starn5t3a" is a proper star
data(starn5t3a)
is.star(starn5t3a)
```

spreadn4t2a

Data: A cyclic 1-spread of PG(3,2)

Description

A balanced 1-spread of PG(3,2) obtained via cyclic construction

Usage

```
data(spreadn4t2a)
```

Format

The spread is formatted as a 3-dimensional array, where the [i,j,k]-th element indicates whether or not the ith basic factor is present in the jth effect of the kth flat of the spread.

Details

```
The spread consists of five subspaces f_1, f_2, f_3, f_4, f_5 given by f_1 = (D, BC, BCD), f_2 = (C, AB, ABC), f_3 = (B, ACD, ABCD), f_4 = (A, BD, ABD) and f_5 = (CD, AC, AD).
```

Note

In R, the data must be loaded using the data function.

14 spreadn4t2b

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2ⁿ Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

checkSpreadIsomorphism for checking the isomorphism of balanced spreads.
checkStarIsomorphism for checking the isomorphism of balanced covering stars.

spreadn4t2b

Data: A cyclic 1-spread of PG(3,2)

Description

A balanced 1-spread of PG(3,2) obtained via cyclic construction

Usage

data(spreadn4t2b)

Format

The spread is formatted as a 3-dimensional array, where the [i,j,k]-th element indicates whether or not the ith basic factor is present in the jth effect of the kth flat of the spread.

Details

```
The spread consists of five subspaces f_1, f_2, f_3, f_4, f_5 given by f_1 = (A, CD, ACD), f_2 = (C, ABCD, ABD), f_3 = (D, B, BD), f_4 = (ABC, AD, BCD) and f_5 = (AC, AB, BC).
```

Note

In R, the data must be loaded using the data function.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2ⁿ Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

spreadn6t2a 15

See Also

checkSpreadIsomorphism for checking the isomorphism of balanced spreads. checkStarIsomorphism for checking the isomorphism of balanced covering stars.

spreadn6t2a

Data: A cyclic 1-spread of PG(5,2)

Description

A balanced 1-spread of PG(5,2) obtained via cyclic construction

Usage

data(spreadn6t2a)

Format

The spread is formatted as a 3-dimensional array, where the [i,j,k]-th element indicates whether or not the ith basic factor is present in the jth effect of the kth flat of the spread.

Details

```
The spread consists of 21 subspaces f_1, f_2, ..., f_{21} given by f_1 = (F, ABCEF, ABCE), f_2 = (E, ABDF, ABDEF), f_3 = (D, ACF, ACDF), f_4 = (C, BF, BCF), f_5 = (B, AE, ABE), f_6 = (A, DEF, ADEF), f_7 = (EF, CDE, CDF), f_8 = (DE, BCD, BCE), f_9 = (CD, ABC, ABD), f_{10} = (BC, ABEF, ACEF), f_{11} = (AB, ADF, BDF), f_{12} = (DF, BE, BDEF), f_{13} = (CE, AD, ACDE), f_{14} = (AC, BDE, ABCDE), f_{15} = (BEF, ACD, ABCDEF), f_{16} = (ADE, BCEF, ABCDF), f_{17} = (CDEF, ABDE, ABCF), f_{18} = (BCDE, ACDEF, ABF), f_{19} = (ABCD, BCDF, AF), f_{20} = (AEF, CF, ACE), and f_{21} = (BD, CEF, BCDEF).
```

Note

In R, the data must be loaded using the data function.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2^n Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

16 spreadn6t2b

spreadn6t2b

Data: A cyclic 1-spread of PG(5,2)

Description

A balanced 1-spread of PG(5,2) obtained via cyclic construction

Usage

data(spreadn6t2b)

Format

The spread is formatted as a 3-dimensional array, where the [i,j,k]-th element indicates whether or not the ith basic factor is present in the jth effect of the kth flat of the spread.

Details

```
The spread consists of 21 subspaces f_1, f_2, ..., f_{21} given by f_1 = (EF, BCD, BCDEF), f_2 = (A, ACF, CF), f_3 = (B, ABCDE, ACDE), f_4 = (DF, F, D), f_5 = (E, BC, BCE), f_6 = (ABC, ABEF, CEF), f_7 = (AEF, ABDF, BDE), f_8 = (AB, BDEF, ADEF), f_9 = (BDF, ABCDEF, ACE), f_{10} = (DEF, BCF, BCDE), f_{11} = (ABCE, ACEF, BF), f_{12} = (BEF, AE, ABF), f_{13} = (ADF, AC, CDF), f_{14} = (ABCDF, ABE, CDEF), f_{15} = (AF, ACDF, CD), f_{16} = (C, AD, ACD), f_{17} = (ABDE, CE, ABCD), f_{18} = (ABDEF, CDE, ABCF), f_{19} = (ACDEF, BD, ABCEF), f_{20} = (BCEF, DE, BCDF), and f_{21} = (BE, ADE, ABD).
```

Note

In R, the data must be loaded using the data function.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2^n Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

spreadn6t2c 17

spreadn6t2c

Data: A cyclic 1-spread of PG(5,2)

Description

A balanced 1-spread of PG(5,2) obtained via cyclic construction

Usage

data(spreadn6t2c)

Format

The spread is formatted as a 3-dimensional array, where the [i,j,k]-th element indicates whether or not the ith basic factor is present in the jth effect of the kth flat of the spread.

Details

```
The spread consists of 21 subspaces f_1, f_2, ..., f_{21} given by f_1 = (F, ABCEF, ABCE), f_2 = (E, ABDF, ABDEF), f_3 = (D, ACF, ACDF), f_4 = (C, BF, BCF), f_5 = (B, AE, ABE), f_6 = (A, DEF, ADEF), f_7 = (EF, CDE, CDF), f_8 = (DE, BCD, BCE), f_9 = (CD, ABC, ABD), f_{10} = (BC, ABEF, ACEF), f_{11} = (AB, ADF, BDF), f_{12} = (DF, BE, BDEF), f_{13} = (CE, AD, ACDE), f_{14} = (AC, BDE, ABCDE), f_{15} = (BEF, ACD, ABCDEF), f_{16} = (ADE, BCEF, ABCDF), f_{17} = (CDEF, ABDE, ABCF), f_{18} = (BCDE, ACDEF, ABF), f_{19} = (ACE, AF, CEF), f_{20} = (CF, BD, BCDF), and f_{21} = (ABCD, AEF, BCDEF).
```

Note

In R, the data must be loaded using the data function.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2^n Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

18 spreadn6t3a

spreadn6t3a

Data: A cyclic 2-spread of PG(5,2)

Description

A balanced 2-spread of PG(5,2) obtained via cyclic construction

Usage

data(spreadn6t3a)

Format

The spread is formatted as a 3-dimensional array, where the [i,j,k]-th element indicates whether or not the ith basic factor is present in the jth effect of the kth flat of the spread.

Details

```
The spread consists of 9 subspaces f_1, f_2, ..., f_9 each of size 7. The subspaces are f_1 = (A, EF, AEF, BCE, ABCE, BCF, ABCF), f_2 = (B, AF, ABF, CDF, BCDF, ACD, ABCD), f_3 = (C, AB, ABC, ADE, ACDE, BDE, BCDE), f_4 = (D, BC, BCD, BEF, BDEF, CEF, CDEF), f_5 = (E, CD, CDE, ACF, ACEF, ADF, ADEF), f_6 = (F, DE, DEF, ABD, ABDF, ABE, ABEF), f_7 = (BD, BF, DF, ACE, ABCDE, ABCEF, ACDEF), f_8 = (AC, CE, AE, BDF, ABCDF, BCDEF, ABDEF) and f_9 = (AD, BE, ABDE, CF, ACDF, BCEF, ABCDEF).
```

Note

In R, the data must be loaded using the data function.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2^n Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

spreadn6t3b

spreadn6t3b

Data: A cyclic 2-spread of PG(5,2)

Description

A balanced 2-spread of PG(5,2) obtained via cyclic construction

Usage

data(spreadn6t3b)

Format

The spread is formatted as a 3-dimensional array, where the [i,j,k]-th element indicates whether or not the ith basic factor is present in the jth effect of the kth flat of the spread.

Details

```
The spread consists of 9 subspaces f_1, f_2, ..., f_9 each of size 7. The subspaces are f_1 = (ABC, AEF, BCEF, ADEF, BCDEF, D, ABCD), f_2 = (E, ABCEF, ABCF, BDE, BD, ACDF, ACDEF), f_3 = (DF, ABCE, ABCDEF, C, CDF, ABE, ABDEF), f_4 = (B, DEF, BDEF, AF, ABF, ADE, ABDE), f_5 = (A, BDF, ABDF, ABCDE, BCDE, ACEF, CEF), f_6 = (EF, AB, ABEF, ACE, ACF, BCE, BCF), f_7 = (BE, F, BEF, BCDF, CDEF, BCD, CDE), f_8 = (ABCDF, ADF, BC, BF, ACD, ABD, CF) and f_9 = (AC, AE, CE, DE, ACDE, AD, CD).
```

Note

In R, the data must be loaded using the data function.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2^n Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

20 starn5t3a

starn5t3a

Data: A 2-star of PG(4,2)

Description

A balanced 2-star of PG(4,2)

Usage

data(starn5t3a)

Format

The star is formatted as a 3-dimensional array, where the [i,j,k]-th element indicates whether or not the ith basic factor is present in the jth effect of the kth flat of the star.

Details

```
The star consists of five subspaces f_1, f_2, f_3, f_4, f_5 given by f_1 = (A, E, CDE, AE, ACD, ACDE, CD), f_2 = (D, BC, BCD, AD, ABC, ABCD, A), f_3 = (C, BDE, BCDE, AC, ABDE, ABCDE, A), f_4 = (B, BCE, CE, AB, ACE, A, ABCE) and f_5 = (DE, BD, BE, A, ABD, ABE, ADE).
```

Note

In R, the data must be loaded using the data function.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2^n Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

starn5t3b 21

starn5t3b

Data: A 2-star of PG(4,2)

Description

A balanced 2-star of PG(4,2)

Usage

data(starn5t3b)

Format

The star is formatted as a 3-dimensional array, where the [i,j,k]-th element indicates whether or not the ith basic factor is present in the jth effect of the kth flat of the star.

Details

```
The star consists of five subspaces f_1, f_2, f_3, f_4, f_5 given by f_1 = (ABC, AC, CDE, B, BCDE, ABDE, ADE), f_2 = (AE, DE, AD, BCE, ABCDE, BCD, ABC), f_3 = (D, C, CD, ABCD, AB, ABD, ABC), f_4 = (E, ACDE, ACD, ABCE, BD, ABC, BDE) and f_5 = (CE, A, ACE, ABC, BC, BE, ABE).
```

Note

In R, the data must be loaded using the data function.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2^n Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

22 starn8t5a

starn8t5a

Data: A 4-star of PG(7,2)

Description

A balanced 4-star of PG(7,2)

Usage

data(starn8t5a)

Format

The star is formatted as a 3-dimensional array, where the [i,j,k]-th element indicates whether or not the ith basic factor is present in the jth effect of the kth flat of the star.

Details

The star consists of nine subspaces $f_1, f_2, ..., f_9$ of size 31 each. Use vectortostring(starn8t5a) to see the elements of this star.

Note

In R, the data must be loaded using the data function.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2^n Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

starn8t5b 23

starn8t5b

Data: A 4-star of PG(7,2)

Description

A balanced 4-star of PG(7,2)

Usage

data(starn8t5b)

Format

The star is formatted as a 3-dimensional array, where the [i,j,k]-th element indicates whether or not the ith basic factor is present in the jth effect of the kth flat of the star.

Details

The star consists of nine subspaces $f_1, f_2, ..., f_9$ of size 31 each. Use vectortostring(starn8t5b) to see the elements of this star.

Note

In R, the data must be loaded using the data function.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2^n Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

24 star_to_spread

star_to_spread

Converts a star to its corresponding spread

Description

A function that converts a balanced covering star $St(n,mu,t,t_0)$ of PG(n-1,2) to its corresponding balanced $((t-t_0)-1)$ -spread of $PG((n-t_0)-1,2)$.

Usage

```
star_to_spread(star)
```

Arguments

star

A balanced covering star of PG(n-1,2) stored as a three dimensional binary array (see Details and Examples of checkSpreadEquivalence).

Details

Finds a balanced $((t-t_0)-1)$ -spread of PG $((n-t_0)-1,2)$ embedded in PG(n-1,2) as conformable with the geometry of a balanced covering star St (n,mu,t,t_0) of PG(n-1,2). The star should be formatted as a 3-dimensional array with star[i,j,k] indicating whether or not the ith basic factor is present in the jth effect of the kth flat of star. See Spencer et al. (2019) for details.

Value

```
A balanced ((t-t_0)-1)-spread of PG((n-t_0)-1,2)
```

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2^n Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

is.spread for checking if the input is a balanced spread. checkSpreadIsomorphism for checking the isomorphism of balanced spreads. checkStarIsomorphism for checking the isomorphism of balanced covering stars. stringtovector 25

Examples

```
## Example 1: checking whether "starn8t5a" is a proper star
data(starn8t5a)
star_to_spread(starn8t5a)

## Example 2: checking whether "starn5t3a" is a proper star
data(starn5t3a)
star_to_spread(starn5t3a)
```

stringtovector

Converts a character string representation of a factorial effect into the vector form

Description

Converts a character string representation of a factorial effect in PG(n-1,2) into a binary vector of length n.

Usage

```
stringtovector(string,n)
```

Arguments

string

a character string representation of a factorial effect in PG(n-1,2) (see Details

and Examples of checkSpreadEquivalence).

n

the number of basic factors, or equivalently, the dimension of PG(n-1, 2)

Details

Takes a character string representation of a factorial effect in PG(n-1,2), and returns a binary vector of length n. This can be used in defining a spread or a star. The spread/star should be formatted as a 3-dimensional array with spread[i,j,k]/star[i,j,k] indicating whether or not the ith basic factor is present in the jth effect of the kth flat of spread/star. See Spencer et al. (2019) for details.

Value

A binary vector of length n.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

26 vectortostring

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2ⁿ Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

checkSpreadIsomorphism for checking the isomorphism of balanced spreads. checkStarIsomorphism for checking the isomorphism of balanced covering stars.

Examples

```
## Example : Converts "AC" into a vector representation
stringtovector("AC",4)
stringtovector("AC",5)
stringtovector("CD",6)
```

vectortostring

Converts a binary vector to character strings

Description

Converts a binary vector or matrix in PG(n-1, 2) into string-vector/matrix.

Usage

```
vectortostring(arry)
```

Arguments

arry

A binary vector or a matrix of binary vectors representing a flat or spread/star in PG(n-1,2) (see Details and Examples of checkSpreadEquivalence).

Details

Takes an array (a binary vector or an array of binary vectors, upto three dimensions) and returns the character string representation of the vectors. This can be used for reporting spreads and stars in an easy-to-read format. Recall that a sprad/star should be formatted as a 3-dimensional array with star[i,j,k] indicating whether or not the ith basic factor is present in the jth effect of the kth flat of star. See Spencer et al. (2019) for details.

Value

Character string representation of the input arry.

Author(s)

Neil Spencer, Pritam Ranjan, Franklin Mendivil

vectortostring 27

References

Spencer, N.A., Ranjan, P., and Mendivil, F., (2019), "Isomorphism Check for 2ⁿ Factorial Designs with Randomization Restrictions", Journal of Statistical Theory and Practice, 13(60),1-24 [https://doi.org/10.1007/s42519-019-0064-5]

See Also

checkSpreadIsomorphism for checking the isomorphism of balanced spreads.
checkStarIsomorphism for checking the isomorphism of balanced covering stars.

Examples

```
## Example 1: converts c(0,1,1,0) into "BC"
vec = c(0,1,1,0)
vectortostring(vec)

## Example 2: converts "spreadn6t3a" into character string representation
data(spreadn6t3a)
vectortostring(spreadn6t3a)

## Example 3: converts "starn5t3a" into character string representation
data(starn5t3a)
vectortostring(starn5t3a)
```

Index

*Topic Collineation	data, <i>13–23</i>
applyCollineation, 2	
getBitstrings, 10	getBitstrings, 10
*Topic Datasets	i 11 12 2
spreadn4t2a, 13	is.spread, 11, 13, 24
spreadn4t2b, 14	is.star, <i>12</i> , 12
spreadn6t2a, 15	spreadn4t2a, 13
spreadn6t2b, 16	spreadn4t2b, 14
spreadn6t2c, 17	spreadn6t2a, 15
spreadn6t3a, 18	spreadn6t2b, 16
spreadn6t3b, 19	spreadn6t2c, 17
starn5t3a, 20	spreadn6t3a, 18
starn5t3b, 21	spreadn6t3b, 19
starn8t5a, 22	star_to_spread, 24
starn8t5b, 23	starn5t3a, 20
*Topic Miscellaneous	starn5t3b, 21
stringtovector, 25	starn8t5a, 22
vectortostring, 26	starn8t5b, 23
*Topic Spread Equivalence	stringtovector, 25
<pre>checkSpreadEquivalence, 3</pre>	Sti ingtovector, 25
<pre>checkStarEquivalence, 7</pre>	vectortostring, 26
*Topic Spread Isomorphism	8,
<pre>checkSpreadIsomorphism, 5</pre>	
*Topic Spread	
is.spread, 11	
*Topic Star Isomorphism	
<pre>checkStarIsomorphism, 8</pre>	
*Topic Star	
is.star, 12	
star_to_spread, 24	
applyCollineation, 2	
checkSpreadEquivalence, 2, 3, 5–8, 10–12, 24–26	
checkSpreadIsomorphism, 3, 4, 5, 9, 12-24, 26, 27	
checkStarEquivalence, 4, 7, 9, 10	
checkStarIsomorphism, 3 , 6 , 8 , 8 , $12-24$, 26 , 27	