## Package 'NBDesign'

September 10, 2020

Type Package

Version 2.0.0

Date 2020-09-09

Title Design and Monitoring of Clinical Trials with Negative Binomial Endpoint

**Description** Calculate various functions needed for design and monitoring clinical trials with negative binomial endpoint

with variable follow-

up. This version has a few changes compared to the previous version 1.0.0, including (1) correct a typo in Type 1 censoring, mtbnull=bnull and (2) restructure the code to account for shape parameter equal to zero, i.e. Poisson scenario.

**Depends** R (>= 3.1.2)

Imports stats, PWEALL, MASS

License GPL (>= 2)

RoxygenNote 5.0.1

LazyData true

NeedsCompilation no

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**Repository** CRAN

Date/Publication 2020-09-10 06:30:22 UTC

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NBDesign-package

#### Description

Calculate various functions needed for design and monitoring clinical trials with negative binomial endpoint with variable follow-up. This version has a few changes compared to the previous version 1.0.0, including (1) correct a typo in Type 1 censoring, mtbnull=bnull and (2) restructure the code to account for shape parameter equal to zero, i.e. Poisson scenario.

#### Details

The DESCRIPTION file:

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Туре. Раскаде	
Version: 2.0.0	
Date: 2020-09-09	
Title: Design and Monitoring of Clinical Trials with Negative Binomial Endpoint	
Description: Calculate various functions needed for design and monitoring clinical trials with negative binomial endp	point
Authors@R: c(person(given="Xiaodong", family="Luo", email = "Xiaodong.Luo@sanofi.com", role =c("aut", "cre"	)), pe
Depends: $R (>= 3.1.2)$	_
Imports: stats,PWEALL,MASS	
License: $GPL (\geq 2)$	
RoxygenNote: 5.0.1	
LazyData: true	
Author: Xiaodong Luo [aut, cre], Sanofi [cph]	
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	binomial distribution with variable follow-up
ynegbinomsize	Two-sample sample size calculation for negative
	binomial distribution with variable follow-up

#### Author(s)

NA

#### negint2

Maintainer: NA

negint2

A utility functon to calculate the mean exposure under different scenarios

#### Description

This will calculate the mean exposure under different scenarios: 2: fixed follow-up with drop-out, 3: variable follow-up with a maximum (maxfu), 4: variable follow-up with a maximum and drop-out

#### Usage

```
negint2(ux=0.5,fixedfu=1,type=2,u=c(0.5,0.5,1),ut=c(0.5,1.0,1.5),
    tfix=ut[length(ut)]+0.5,maxfu=10.0,tchange=c(0,0.5,1),
    ratec=c(0.15,0.15,0.15),eps=1.0e-03)
```

#### Arguments

ux	the parameter a in $(a^{*}t)/(1+a^{*}t)$
fixedfu	the minimum follow-up time
type	follow-up type, type=2: fixed fu with fu time fixedfu but subject to censoring; type=3: depending on entry time, minimum fu is fixedfu and maximum fu is maxfu; type=4: same as 3 but subject to censoring
u	recruitment rate
ut	recruitment interval, must have the same length as u
tfix	fixed study duration, often equals to recruitment time plus minimum follow-up
maxfu	maximum follow-up time, should not be greater than tfix
tchange	a strictly increasing sequence of time points starting from zero at which the drop-out rate changes. The first element of tchange must be zero. The above rates and tchange must have the same length.
ratec	piecewise constant drop-out rate
eps	error tolerance for the numerical intergration

#### Details

Let  $\tau_{min}$  and  $\tau_{max}$  correspond to the minimum follow-up time taumin and the maximum follow-up time taumax. Let  $T_f$ , C, E and R be the follow-up time, the drop-out time, the study entry time and the total recruitment period(R is the last element of ut). For type 2 follow-up  $T_f = min(C, \tau_{min})$ . For type 3 follow-up,  $T_f = min(R + \tau_{min} - E, \tau_{max})$ . For type 4 follow-up,  $T_f = min(R + \tau_{min} - E, \tau_{max})$ . For type 4 follow-up,  $T_f = min(R + \tau_{min} - E, \tau_{max})$ .

$$\int_0^\infty tf(t)dt$$
$$\int_0^\infty \frac{at}{1+at}f(t)dt$$

and

#### Value

mt	mean of $(a*t)/(1+a*t)$
tt	mean of t
vt	variance of t

#### Author(s)

Xiaodong Luo

#### Examples

```
##calculating the exposure for type 4 follow-up
exp4=negint2(ux=0.5,fixedfu=1,type=2,u=c(0.5,0.5,1),ut=c(0.5,1.0,1.5),
    tfix=2.0,maxfu=1.0,tchange=c(0,0.5,1),
    ratec=c(0.15,0.15,0.15),eps=1.0e-03)
#mean exposure
meanexp=exp4$tt
#var exposure
varexp=exp4$vt
c(meanexp,sqrt(varexp))
#mean of (ux*t)/(1+ux*t)
meanuxt=exp4$mt
```

```
ynegbinompower
```

*Two-sample sample size calculation for negative binomial distribution with variable follow-up* 

#### Description

This will calculate the power for the negative binomial distribution for the 2-sample case under different follow-up scenarios: 1: fixed follow-up, 2: fixed follow-up with drop-out, 3: variable follow-up with a minimum fu and a maximum fu, 4: variable follow-up with a minimum fu and a maximum fu and a maximum fu and drop-out.

#### Usage

#### Arguments

nsize	total number of subjects in two groups
r0	event rate for the control
r1	event rate for the treatment

shape0	dispersion parameter for the control
shape1	dispersion parameter for the treatment
pi1	allocation prob for the treatment
alpha	type-1 error
twosided	1: two-side, others: one-sided
fixedfu	fixed follow-up time for each patient
type	follow-up time type, type=1: fixed fu with fu time fixedfu; type=2: same as 1 but subject to censoring; type=3: depending on entry time, minimum fu is fixedfu and maximum fu is maxfu; type=4: same as 3 but subject to censoring
u	recruitment rate
ut	recruitment interval, must have the same length as u
tfix	fixed study duration, often equals to recruitment time plus minimum follow-up
maxfu	maximum follow-up time, should not be greater than tfix
tchange	a strictly increasing sequence of time points starting from zero at which the drop-out rate changes. The first element of tchange must be zero. The above rates and tchange must have the same length.
ratec1	piecewise constant drop-out rate for the treatment
ratec0	piecewise constant drop-out rate for the control
eps	error tolerance for the numerical intergration

#### Details

Let  $\tau_{min}$  and  $\tau_{max}$  correspond to the minimum follow-up time fixedfu and the maximum followup time maxfu. Let  $T_f$ , C, E and R be the follow-up time, the drop-out time, the study entry time and the total recruitment period(R is the last element of ut). For type 1 follow-up,  $T_f = \tau_{min}$ . For type 2 follow-up  $T_f = min(C, \tau_{min})$ . For type 3 follow-up,  $T_f = min(R + \tau_{min} - E, \tau_{max})$ . For type 4 follow-up,  $T_f = min(R + \tau_{min} - E, \tau_{max}, C)$ . Let f be the density of  $T_f$ . Suppose that  $Y_i$  is the number of event observed in follow-up time  $t_i$  for patient i with treatment assignment  $Z_i$ ,  $i = 1, \ldots, n$ . Suppose that  $Y_i$  follows a negative binomial distribution such that

$$P(Y_i = y \mid Z_i = j) = \frac{\Gamma(y + 1/k_j)}{\Gamma(y + 1)\Gamma(1/k_j)} \left(\frac{k_j u_i}{1 + k_j u_i}\right)^y \left(\frac{1}{1 + k_j u_i}\right)^{1/k_j},$$

where

$$\log(u_i) = \log(t_i) + \beta_0 + \beta_1 Z_i.$$

Let  $\hat{\beta}_0$  and  $\hat{\beta}_1$  be the MLE of  $\beta_0$  and  $\beta_1$ . The variance of  $\hat{\beta}_1$  is

$$\operatorname{var}(\hat{\beta}_1) = 1/\tilde{a}_0(r_0) + 1/\tilde{a}_1(r_1)$$

where

$$\tilde{a}_j(r) = \sum_{i=1}^n I(Z_i = j)k_j r t_i / (1 + k_j r t_i), \quad j = 0, 1,$$

and  $k_j$ , j = 0, 1 are the dispersion parameters for control j = 0 and treatment j = 1. Note that Zhu and Lakkis (2014) use

$$a_j(r) = \sum_{i=1}^n I(Z_i = j)k_j r E(t_i) / \{1 + k_j r E(t_i)\},\$$

to replace  $\tilde{a}_j(r)$ , j = 0, 1. Using Jensen's inequality, we can show  $a_j(r) \ge \tilde{a}_j(r)$ , which means Zhu and Lakkis's method will underestimate variance of  $\hat{\beta}_1$ , which leads to either smaller than required sample size or inflated power. For comparison, I provide sample sizes under both  $\tilde{a}_j(r)$  and  $a_j(r)$ .

Zhu and Lakkis (2014) discuss three types of the variance under the null. The first way is to set  $\tilde{r}_0 = \tilde{r}_1 = r_0$ , using event rate from the control group. The second way is to set  $\tilde{r}_0 = r_0$ ,  $\tilde{r}_1 = r_1$ , using true event rates. The third way is to set  $\tilde{r}_0 = \tilde{r}_1 = \tilde{r}$ , where  $\tilde{r} = \pi_1 r_1 + \pi_0 r_0$ , using maximum likelihood estimation.

Therefore, for each type of follow-up, there are 3 sample sizes calculated (because there are 3 varainces under the null) for with and without approximation of Zhu and Lakkis (2014).

Note that PASS14.0 provides 3 ways of null varaince with the default being the MLE. PASS does not allow different dispersion parameters between treatmetn and control. EAST only provides the second way of null varaince but allows for different dispersion parameters. Both of these softwares base on the approximatin method of Zhu and Lakkis (2014), which underestimate the required sample sizes.

#### Value

tildeXPWR	powers (in percentage) not based on current approach, i.e. not based on the Zhu and Lakkis's approximation
XPWR	powers (in percentage) based on on the Zhu and Lakkis's approximation
tildemineffsize	
	minimum detectable effect sizes not based on approximation
mineffsize	minimum detectable effect sizes based on approximation
Exposure	mean exposure under different follow-up types with element 1 for control, element 2 for treatment and element 3 for overall.
SDExp	Sd of the exposure under different follow-up types with element 1 for control, element 2 for treatment and column 3 for overall.

#### Author(s)

Xiaodong Luo

#### References

Zhu~H and Lakkis~H. Sample size calculation for comparing two negative binomial rates. Statistics in Medicine 2014, 33: 376-387.

#### ynegbinompowersim

#### Examples

ynegbinompowersim Two-sample sample size calculation for negative binomial distribution with variable follow-up

#### Description

This will calculate the power for the negative binomial distribution for the 2-sample case under different follow-up scenarios: 1: fixed follow-up, 2: fixed follow-up with drop-out, 3: variable follow-up with a minimum fu and a maximum fu, 4: variable follow-up with a minimum fu and a maximum fu and drop-out.

#### Usage

#### Arguments

nsize	total number of subjects in two groups
r0	event rate for the control
r1	event rate for the treatment
shape0	dispersion parameter for the control
shape1	dispersion parameter for the treatment
pi1	allocation prob for the treatment
alpha	type-1 error
twosided	1: two-side, others: one-sided
fixedfu	fixed follow-up time for each patient
type	follow-up time type, type=1: fixed fu with fu time fixedfu; type=2: same as 1 but subject to censoring; type=3: depending on entry time, minimum fu is fixedfu and maximum fu is maxfu; type=4: same as 3 but subject to censoring

u	recruitment rate
ut	recruitment interval, must have the same length as u
tfix	fixed study duration, often equals to recruitment time plus minimum follow-up
maxfu	maximum follow-up time, should not be greater than tfix
tchange	a strictly increasing sequence of time points starting from zero at which the drop-out rate changes. The first element of tchange must be zero. The above rates and tchange must have the same length.
ratec1	piecewise constant drop-out rate for the treatment
ratec0	piecewise constant drop-out rate for the control
rn	Number of repetitions

#### Details

Let  $\tau_{min}$  and  $\tau_{max}$  correspond to the minimum follow-up time fixedfu and the maximum followup time maxfu. Let  $T_f$ , C, E and R be the follow-up time, the drop-out time, the study entry time and the total recruitment period(R is the last element of ut). For type 1 follow-up,  $T_f = \tau_{min}$ . For type 2 follow-up  $T_f = min(C, \tau_{min})$ . For type 3 follow-up,  $T_f = min(R + \tau_{min} - E, \tau_{max})$ . For type 4 follow-up,  $T_f = min(R + \tau_{min} - E, \tau_{max}, C)$ . Let f be the density of  $T_f$ . Suppose that  $Y_i$  is the number of event observed in follow-up time  $t_i$  for patient i with treatment assignment  $Z_i$ ,  $i = 1, \ldots, n$ . Suppose that  $Y_i$  follows a negative binomial distribution such that

$$P(Y_i = y \mid Z_i = j) = \frac{\Gamma(y + 1/k_j)}{\Gamma(y + 1)\Gamma(1/k_j)} \left(\frac{k_j u_i}{1 + k_j u_i}\right)^y \left(\frac{1}{1 + k_j u_i}\right)^{1/k_j},$$

where  $k_j, j = 0, 1$  are the dispersion parameters for control j = 0 and treatment j = 1 and

$$\log(u_i) = \log(t_i) + \beta_0 + \beta_1 Z_i$$

The data will be gnerated according to the above model. Note that the piecewise exponential distribution and the piecewise uniform distribution are genrated using R package PWEALL functions "rpwe" and "rpwu", respectively.

The parameters in the model are estimated by MLE using the R package MASS function "glm.nb".

#### Value

simulation power (in percentage)

#### Author(s)

power

Xiaodong Luo

#### Examples

#### ynegbinomsize

```
ratec1=c(0.15,0.15,0.15),rn=10)
###Power
abc$power
```

ynegbinomsize

*Two-sample sample size calculation for negative binomial distribution with variable follow-up* 

#### Description

This will calculate the sample size for the negative binomial distribution for the 2-sample case under different follow-up scenarios: 1: fixed follow-up, 2: fixed follow-up with drop-out, 3: variable follow-up with a minimum fu and a maximum fu, 4: variable follow-up with a minimum fu and a maximum fu and a maximum fu and drop-out.

#### Usage

#### Arguments

r0	event rate for the control
r1	event rate for the treatment
shape0	dispersion parameter for the control
shape1	dispersion parameter for the treatment
pi1	allocation prob for the treatment
alpha	type-1 error
twosided	1: two-side, others: one-sided
beta	tyep-2 error
fixedfu	fixed follow-up time for each patient
type	follow-up time type, type=1: fixed fu with fu time fixedfu; type=2: same as 1 but subject to censoring; type=3: depending on entry time, minimum fu is fixedfu and maximum fu is maxfu; type=4: same as 3 but subject to censoring
u	recruitment rate
ut	recruitment interval, must have the same length as u
tfix	fixed study duration, often equals to recruitment time plus minimum follow-up ${\tt fixedfu}$
maxfu	maximum follow-up time, should not be greater than tfix
tchange	a strictly increasing sequence of time points starting from zero at which the drop-out rate changes. The first element of tchange must be zero.

ratec1	piecewise constant drop-out rate for the treatment. The rate and tchange must have the same length.
ratec0	piecewise constant drop-out rate for the control. The rate and tchange must have the same length.
eps	error tolerance for the numerical intergration

#### Details

Let  $\tau_{min}$  and  $\tau_{max}$  correspond to the minimum follow-up time fixedfu and the maximum followup time maxfu. Let  $T_f$ , C, E and R be the follow-up time, the drop-out time, the study entry time and the total recruitment period(R is the last element of ut). For type 1 follow-up,  $T_f = \tau_{min}$ . For type 2 follow-up  $T_f = min(C, \tau_{min})$ . For type 3 follow-up,  $T_f = min(R + \tau_{min} - E, \tau_{max})$ . For type 4 follow-up,  $T_f = min(R + \tau_{min} - E, \tau_{max}, C)$ . Let f be the density of  $T_f$ . Suppose that  $Y_i$  is the number of event observed in follow-up time  $t_i$  for patient i with treatment assignment  $Z_i$ ,  $i = 1, \ldots, n$ . Suppose that  $Y_i$  follows a negative binomial distribution such that

$$P(Y_i = y \mid Z_i = j) = \frac{\Gamma(y + 1/k_j)}{\Gamma(y + 1)\Gamma(1/k_j)} \left(\frac{k_j u_i}{1 + k_j u_i}\right)^y \left(\frac{1}{1 + k_j u_i}\right)^{1/k_j},$$

where

 $\log(u_i) = \log(t_i) + \beta_0 + \beta_1 Z_i.$ 

Let  $\hat{\beta}_0$  and  $\hat{\beta}_1$  be the MLE of  $\beta_0$  and  $\beta_1$ . The variance of  $\hat{\beta}_1$  is

$$\operatorname{var}(\beta_1) = 1/\tilde{a}_0(r_0) + 1/\tilde{a}_1(r_1)$$

where

$$\tilde{a}_j(r) = \sum_{i=1}^n I(Z_i = j)k_j r t_i / (1 + k_j r t_i), \quad j = 0, 1,$$

and  $k_j$ , j = 0, 1 are the dispersion parameters for control j = 0 and treatment j = 1. Note that Zhu and Lakkis (2014) use

$$a_j(r) = \sum_{i=1}^n I(Z_i = j)k_j r E(t_i) / \{1 + k_j r E(t_i)\},\$$

to replace  $\tilde{a}_j(r)$ , j = 0, 1. Using Jensen's inequality, we can show  $a_j(r) \ge \tilde{a}_j(r)$ , which means Zhu and Lakkis's method will underestimate variance of  $\hat{\beta}_1$ , which leads to either smaller than required sample size or inflated power. For comparison, I provide sample sizes under both  $\tilde{a}_j(r)$  and  $a_j(r)$ .

Zhu and Lakkis (2014) discuss three types of the variance under the null. The first way is to set  $\tilde{r}_0 = \tilde{r}_1 = r_0$ , using event rate from the control group. The second way is to set  $\tilde{r}_0 = r_0$ ,  $\tilde{r}_1 = r_1$ , using true event rates. The third way is to set  $\tilde{r}_0 = \tilde{r}_1 = \tilde{r}$ , where  $\tilde{r} = \pi_1 r_1 + \pi_0 r_0$ , using maximum likelihood estimation.

Therefore, for each type of follow-up, there are 3 sample sizes calculated (because there are 3 varainces under the null) for with and without approximation of Zhu and Lakkis (2014).

Note that PASS14.0 provides 3 ways of null varaince with the default being the MLE. PASS does not allow different dispersion parameters between treatmetn and control. EAST only provides the second way of null varaince but allows for different dispersion parameters. Both of these softwares base on the approximatin method of Zhu and Lakkis (2014), which underestimate the required sample sizes.

#### ynegbinomsize

#### Value

tildeXN	sample sizes based on current approach, i.e. not based on the Zhu and Lakkis's approximation
XN	sample sizes based on the Zhu and Lakkis's approximation
Exposure	mean exposure under different follow-up types with element 1 for control, element 2 for treatment and element 3 for overall.
SDExp	Sd of the exposure under different follow-up types with element 1 for control, element 2 for treatment and column 3 for overall.

#### Author(s)

Xiaodong Luo

#### References

Zhu~H and Lakkis~H. Sample size calculation for comparing two negative binomial rates. Statistics in Medicine 2014, 33: 376-387.

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