Package 'adoptr'

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Description Optimize one or two-arm, two-stage designs for clinical trials with respect to several pre-implemented objective criteria or implement custom objectives.

Optimization under uncertainty and conditional (given stage-one outcome) constraints are supported.

See <doi:10.1002/sim.8291> and <doi:10.18637/jss.v098.i09> for details.

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adoptr

Adaptive Optimal Two-Stage Designs

Description

The **adoptr** package provides functionality to explore custom optimal two-stage designs for one- or two-arm superiority tests. For more details on the theoretical background see <doi:10.1002/sim.8291> and <doi:10.18637/jss.v098.i09>. **adoptr** makes heavy use of the S4 class system. A good place to start learning about it can be found here.

Quickstart

For a sample workflow and a quick demo of the capabilities, see here.

A more detailed description of the background and the usage of **adoptr** can be found here or here <doi:10.18637/jss.v098.i09>.

A variety of examples is presented in the validation report hosted here.

Designs

adoptr currently supports TwoStageDesign, GroupSequentialDesign, and OneStageDesign.

Data distributions

Currently, the only implemented data distribution is Normal (one or two arms).

Priors

Both ContinuousPrior and PointMassPrior are supported for the single parameter of a DataDistribution.

Scores

See Scores for information on the basic system of representing scores. Available scores are ConditionalPower, ConditionalSampleSize, Power, and ExpectedSampleSize..

AverageN2-class

Regularization via L1 norm

Description

Implements the L1-norm of the design's stage-two sample size function. The average of the stage-two sample size without weighting with the data distribution is computed. This can be interpreted as integration over a unifrom prior on the continuation region.

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Usage

```
AverageN2(label = NA_character_)
## S4 method for signature 'AverageN2,TwoStageDesign'
evaluate(s, design, optimization = FALSE, subdivisions = 10000L, ...)
```

Arguments

label object label (string)
s Score object

design object

optimization logical, if TRUE uses a relaxation to real parameters of the underlying design;

used for smooth optimization.

subdivisions number of subdivisions to use for adaptive integration (only affects non-optimization

code)

... further optional arguments

Value

an object of class AverageN2

See Also

N1 for penalizing n1 values

Examples

```
avn2 <- AverageN2()
evaluate(
    AverageN2(),
    TwoStageDesign(100, 0.5, 1.5, 60.0, 1.96, order = 5L)
) # 60</pre>
```

Binomial-class

Binomial data distribution

Description

Implements the normal approximation for a test on rates. The reponse rate in the control group, r_C , has to be specified by rate_control. The null hypothesis is: $r_E <= r_C$, where r_E denotes the response rate in the invervention group. It is tested against the alternative $r_E > r_C$. The test statistic is given as $X_1 = \sqrt{n}(r_E - r_C)/\sqrt{2r_0(1-r_0)}$, where r_0 denotes the mean between r_E and r_C in the two-armed case, and r_E in the one-armed case.#' All priors have to be defined for the rate difference $r_E - r_C$.

Binomial-class 5

Usage

```
Binomial(rate_control, two_armed = TRUE)
## S4 method for signature 'Binomial'
quantile(x, probs, n, theta, ...)
## S4 method for signature 'Binomial, numeric'
simulate(object, nsim, n, theta, seed = NULL, ...)
```

Arguments

rate_control assumed response rate in control group

two_armed logical indicating if a two-armed trial is regarded

x outcome

probs vector of probabilities

n sample size

theta distribution parameter

... further optional arguments

object of class Binomial
nsim number of simulation runs

seed random seed

Details

Note that simulate for class Binomial simulates the normal approximation of the test statistic.

Slots

```
rate_control cf. parameter 'rate_control'
```

See Also

see probability_density_function and cumulative_distribution_function to evaluate the pdf and the cdf, respectively.

```
datadist <- Binomial(rate_control = 0.2, two_armed = FALSE)</pre>
```

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bounds

Get support of a prior or data distribution

Description

bounds() returns the range of the support of a prior or data distribution.

Usage

```
bounds(dist, ...)
## S4 method for signature 'PointMassPrior'
bounds(dist, ...)
## S4 method for signature 'ContinuousPrior'
bounds(dist, ...)
```

Arguments

```
dist a univariate distribution object
... further optional arguments
```

Value

```
numeric of length two, c(lower, upper)
```

Examples

```
bounds(PointMassPrior(c(0, .5), c(.3, .7))) # > 0.3 0.7 bounds(ContinuousPrior(function(x) dunif(x, .2, .4), c(.2, .4))) # > 0.2 0.4
```

c2

Query critical values of a design

Description

Methods to access the stage-two critical values of a TwoStageDesign. c2 returns the stage-two critical value conditional on the stage-one test statistic.

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Usage

```
c2(d, x1, ...)
## S4 method for signature 'TwoStageDesign,numeric'
c2(d, x1, ...)
## S4 method for signature 'OneStageDesign,numeric'
c2(d, x1, ...)
```

Arguments

```
d designx1 stage-one test statistic... further optional arguments
```

See Also

TwoStageDesign, see n for accessing the sample size of a design

```
design <- TwoStageDesign(</pre>
 n1
       = 25,
 c1f = 0,
 c1e = 2.5,
 n2
       = 50,
 c2
       = 1.96,
 order = 7L
c2(design, 2.2) # 1.96
c2(design, 3.0) # -Inf
c2(design, -1.0) # Inf
design <- TwoStageDesign(</pre>
  n1 = 25,
  c1f = 0,
  c1e = 2.5,
  n2
      = 50,
  c2 = 1.96,
  order = 7L
)
c2(design, 2.2) # 1.96
c2(design, 3.0) # -Inf
c2(design, -1.0) # Inf
```

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composite

Score Composition

Description

composite defines new composite scores by point-wise evaluation of scores in any valid numerical expression.

Usage

```
composite(expr, label = NA_character_)
## S4 method for signature 'CompositeScore,TwoStageDesign'
evaluate(s, design, ...)
```

Arguments

expr Expression (in curly brackets); must contain at least one score variable; if multiple scores are used, they must either all be conditional or unconditional. Currently, no non-score variables are supported

label object label (string)

s object of class CompositeScore

design object

... further optional arguments

Value

an object of class CompositeConditionalScore or CompositeUnconditionalScore depending on the class of the scores used in expr

See Also

Scores

```
ess <- ExpectedSampleSize(Normal(), PointMassPrior(.4, 1))
power <- Power(Normal(), PointMassPrior(.4, 1))

# linear combination:
composite({ess - 50*power})

# control flow (e.g. for and while loops)
composite({
  res <- 0
  for (i in 1:3) {
     res <- res + ess</pre>
```

condition 9

```
}
  res
})

# functional composition
composite({log(ess)})
cp <- ConditionalPower(Normal(), PointMassPrior(.4, 1))
composite({3*cp})</pre>
```

condition

Condition a prior on an interval

Description

Restrict an object of class Prior to a sub-interval and re-normalize the PDF.

Usage

```
condition(dist, interval, ...)
## S4 method for signature 'PointMassPrior,numeric'
condition(dist, interval, ...)
## S4 method for signature 'ContinuousPrior,numeric'
condition(dist, interval, ...)
```

Arguments

dist a univariate distribution object
interval length-two numeric vector giving the parameter interval to condition on
further optional arguments

Value

conditional Prior on given interval

10 ConditionalPower-class

```
ConditionalPower-class
```

(Conditional) Power of a Design

Description

This score evaluates $P[X_2 > c_2(design, X_1)|X_1 = x_1]$. Note that the distribution of X_2 is the posterior predictive after observing $X_1 = x_1$.

Usage

```
ConditionalPower(dist, prior, label = "Pr[x2>=c2(x1)|x1]")
Power(dist, prior, label = "Pr[x2>=c2(x1)]")
## S4 method for signature 'ConditionalPower,TwoStageDesign'
evaluate(s, design, x1, optimization = FALSE, ...)
```

Arguments

```
dist a univariate distribution object

prior a Prior object

label object label (string)

s Score object

design object

x1 stage-one test statistic

optimization logical, if TRUE uses a relaxation to real parameters of the underlying design; used for smooth optimization.

... further optional arguments
```

See Also

Scores

```
prior <- PointMassPrior(.4, 1)
cp <- ConditionalPower(Normal(), prior)
evaluate(
    cp,
    TwoStageDesign(50, .0, 2.0, 50, 2.0, order = 5L),
    x1 = 1
)
# these two are equivalent:
expected(cp, Normal(), prior)
Power(Normal(), prior)</pre>
```

```
ConditionalSampleSize-class (Conditional) Sample Size of a Design
```

Description

This score simply evaluates n(d, x1) for a design d and the first-stage outcome x1. The data distribution and prior are only relevant when it is integrated.

Usage

```
ConditionalSampleSize(label = "n(x1)")
ExpectedSampleSize(dist, prior, label = "E[n(x1)]")
## S4 method for signature 'ConditionalSampleSize,TwoStageDesign'
evaluate(s, design, x1, optimization = FALSE, ...)
```

Arguments

```
label object label (string)

dist a univariate distribution object

prior a Prior object

s Score object

design object

x1 stage-one test statistic

optimization logical, if TRUE uses a relaxation to real parameters of the underlying design; used for smooth optimization.

... further optional arguments
```

See Also

Scores

```
design <- TwoStageDesign(50, .0, 2.0, 50, 2.0, order = 5L)
prior <- PointMassPrior(.4, 1)

css <- ConditionalSampleSize()
evaluate(css, design, c(0, .5, 3))

ess <- ExpectedSampleSize(Normal(), prior)

# those two are equivalent
evaluate(ess, design)</pre>
```

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```
evaluate(expected(css, Normal(), prior), design)
```

Constraints

Formulating Constraints

Description

Conceptually, constraints work very similar to scores (any score can be put in a constraint). Currently, constraints of the form 'score <=/>= x', 'x <=/>= score' and 'score <=/>= score' are admissible.

Usage

```
## S4 method for signature 'Constraint, TwoStageDesign'
evaluate(s, design, optimization = FALSE, ...)
## S4 method for signature 'ConditionalScore, numeric'
e1 <= e2
## S4 method for signature 'ConditionalScore, numeric'
e1 >= e2
## S4 method for signature 'numeric, ConditionalScore'
## S4 method for signature 'numeric, Conditional Score'
e1 >= e2
## S4 method for signature 'ConditionalScore, ConditionalScore'
e1 <= e2
## S4 method for signature 'ConditionalScore, ConditionalScore'
e1 >= e2
## S4 method for signature 'UnconditionalScore, numeric'
## S4 method for signature 'UnconditionalScore, numeric'
e1 >= e2
## S4 method for signature 'numeric, Unconditional Score'
e1 <= e2
## S4 method for signature 'numeric, Unconditional Score'
e1 >= e2
```

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```
## S4 method for signature 'UnconditionalScore,UnconditionalScore'
e1 <= e2
## S4 method for signature 'UnconditionalScore,UnconditionalScore'
e1 >= e2
```

Arguments

S	Score object
design	object
optimization	logical, if TRUE uses a relaxation to real parameters of the underlying design; used for smooth optimization.
	further optional arguments
e1	left hand side (score or numeric)
e2	right hand side (score or numeric)

See Also

minimize

Examples

```
design <- OneStageDesign(50, 1.96)

cp     <- ConditionalPower(Normal(), PointMassPrior(0.4, 1))
pow     <- Power(Normal(), PointMassPrior(0.4, 1))

# unconditional power constraint
constraint1 <- pow >= 0.8
evaluate(constraint1, design)

# conditional power constraint
constraint2 <- cp >= 0.7
evaluate(constraint2, design, .5)
constraint3 <- 0.7 <= cp # same as constraint2
evaluate(constraint3, design, .5)</pre>
```

Continuous Prior-class Continuous univariate prior distributions

Description

ContinuousPrior is a sub-class of Prior implementing a generic representation of continuous prior distributions over a compact interval on the real line.

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Usage

```
ContinuousPrior(
  pdf,
  support,
  order = 10,
  label = NA_character_,
  tighten_support = FALSE,
  check_normalization = TRUE
)
```

Arguments

pdf vectorized univariate PDF function

support numeric vector of length two with the bounds of the compact interval on which

the pdf is positive.

order integer, integration order of the employed Gaussian quadrature integration rule

to evaluate scores. Automatically set to length(n2_pivots) if

length(n2_pivots) == length(c2_pivots) > 1, otherwise c2 and n2 are taken to be constant in stage-two and replicated to match the number of pivots speci-

fied by order

label object label (string)

tighten_support

logical indicating if the support should be tightened

check_normalization

logical indicating if it should be checked that pdf defines a density.

Slots

```
pdf cf. parameter 'pdf'
support cf. parameter 'support'
pivots normalized pivots for integration rule (in [-1, 1]) the actual pivots are scaled to the support of the prior
weights weights of of integration rule at pivots for approximating integrals over delta
```

See Also

Discrete priors are supported via PointMassPrior

```
ContinuousPrior(function(x) 2*x, c(0, 1))
```

```
cumulative_distribution_function

Cumulative distribution function
```

Description

cumulative_distribution_function evaluates the cumulative distribution function of a specific distribution dist at a point x.

Usage

```
cumulative_distribution_function(dist, x, n, theta, ...)
## S4 method for signature 'Binomial,numeric,numeric,numeric'
cumulative_distribution_function(dist, x, n, theta, ...)
## S4 method for signature 'Normal,numeric,numeric,numeric'
cumulative_distribution_function(dist, x, n, theta, ...)
## S4 method for signature 'Student,numeric,numeric,numeric'
cumulative_distribution_function(dist, x, n, theta, ...)
```

Arguments

```
dist a univariate distribution object
x outcome
n sample size
theta distribution parameter
... further optional arguments
```

Details

If the distribution is Binomial, theta denotes the rate difference between intervention and control group. Then, the mean is assumed to be $\sqrt{n}theta$.

If the distribution is Normal, then the mean is assumed to be $\sqrt{n}theta$.

```
cumulative_distribution_function(Binomial(.1, TRUE), 1, 50, .3)
cumulative_distribution_function(Normal(), 1, 50, .3)
cumulative_distribution_function(Student(two_armed = FALSE), .75, 50, .9)
```

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DataDistribution-class

Data distributions

Description

DataDistribution is an abstract class used to represent the distribution of a sufficient statistic x given a sample size n and a single parameter value theta.

Arguments

X	outcome
n	sample size
theta	distribution parameter
	further optional arguments

Details

This abstraction layer allows the representation of t-distributions (unknown variance), normal distribution (known variance), and normal approximation of a binary endpoint. Currently, the two implemented versions are Normal-class and Binomial-class.

The logical option two_armed allows to decide whether a one-arm or a two-arm (the default) design should be computed. In the case of a two-arm design all sample sizes are per group.

Slots

two_armed Logical that indicates if a two-arm design is assumed.

Examples

```
normaldist <- Normal(two_armed = FALSE)</pre>
binomialdist <- Binomial(rate_control = .25, two_armed = TRUE)</pre>
```

expectation

Expected value of a function

Description

Computes the expected value of a vectorized, univariate function f with respect to a distribution dist. I.e., E[f(X)].

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Usage

```
expectation(dist, f, ...)
## S4 method for signature 'PointMassPrior, `function`'
expectation(dist, f, ...)
## S4 method for signature 'ContinuousPrior, `function`'
expectation(dist, f, ...)
```

Arguments

```
dist a univariate distribution object
f a univariate function, must be vectorized
... further optional arguments
```

Value

numeric, expected value of f with respect to dist

Examples

```
expectation(PointMassPrior(c(0, .5), c(.3, .7)), identity)
# > .35

expectation(
    ContinuousPrior(function(x) dunif(x, .2, .4), c(.2, .4)),
    identity
)
# > 0.3
```

get_initial_design

Initial design

Description

The optimization method minimize requires an initial design for optimization. The function get_initial_design provides an initial guess based on a fixed design that fulfills constraints on type I error rate and power. Note that a situation-specific initial design may be much more efficient.

Usage

```
get_initial_design(
  theta,
  alpha,
  beta,
  type = c("two-stage", "group-sequential", "one-stage"),
```

```
dist = Normal(),
  order = 7L,
    ...
)
```

Arguments

theta	the alternative effect size in the normal case, the rate difference under the alternative in the binomial case
alpha	maximal type I error rate
beta	maximale type II error rate
type	is a two-stage, group-sequential, or one-stage design requried?
dist	distribution of the test statistic
order	desired integration order
	further optional arguments

Details

The distribution of the test statistic is specified by dist. The default assumes a two-armed z-test.

Examples

```
init <- get_initial_design(
   theta = 0.3,
   alpha = 0.025,
   beta = 0.2,
   type = "two-stage",
   dist = Normal(two_armed = FALSE),
   order = 7L
)</pre>
```

```
{\tt get\_lower\_boundary\_design} \\ {\tt Boundary\ designs}
```

Description

The optimization method minimize is based on the package nloptr. This requires upper and lower boundaries for optimization. Such boundaries can be computed via lower_boundary_design respectively upper_boundary_design. They are implemented by default in minimize. Note that minimize allows the user to define its own boundary designs, too.

Usage

```
get_lower_boundary_design(initial_design, ...)
get_upper_boundary_design(initial_design, ...)
## S4 method for signature 'OneStageDesign'
get_lower_boundary_design(initial_design, n1 = 1, c1_buffer = 2, ...)
## S4 method for signature 'GroupSequentialDesign'
get_lower_boundary_design(
  initial_design,
 n1 = 1,
  n2_pivots = 1,
  c1\_buffer = 2,
  c2\_buffer = 2,
)
## S4 method for signature 'TwoStageDesign'
get_lower_boundary_design(
  initial_design,
 n1 = 1,
 n2_pivots = 1,
  c1_buffer = 2,
  c2\_buffer = 2,
)
## S4 method for signature 'OneStageDesign'
get_upper_boundary_design(
  initial_design,
 n1 = 5 * initial_design@n1,
  c1\_buffer = 2,
)
## S4 method for signature 'GroupSequentialDesign'
get_upper_boundary_design(
  initial_design,
 n1 = 5 * initial_design@n1,
  n2_pivots = 5 * initial_design@n2_pivots,
 c1\_buffer = 2,
  c2\_buffer = 2,
)
## S4 method for signature 'TwoStageDesign'
get_upper_boundary_design(
```

```
initial_design,
n1 = 5 * initial_design@n1,
n2_pivots = 5 * initial_design@n2_pivots,
c1_buffer = 2,
c2_buffer = 2,
...
)
```

Arguments

```
initial_design The initial design

optional arguments
The values c1f and c1e from the initial design are shifted to c1f -c1_buffer and c1e -c1_buffer in get_lower_boundary_design, respectively, to c1f + c1_buffer and c1e + c1_buffer in get_upper_boundary_design. This is handled analogously with c2_pivots and c2_buffer.

n1 bound for the first-stage sample size n1

c1_buffer shift of the early-stopping boundaries from the initial ones

n2_pivots bound for the second-stage sample size n2

c2_buffer shift of the final decision boundary from the initial one
```

Examples

```
initial_design <- TwoStageDesign(
  n1 = 25,
  c1f = 0,
  c1e = 2.5,
  n2 = 50,
  c2 = 1.96,
  order = 7L
  )
get_lower_boundary_design(initial_design)</pre>
```

GroupSequentialDesign-class

Group-sequential two-stage designs

Description

Group-sequential designs are a sub-class of the TwoStageDesign class with constant stage-two sample size. See TwoStageDesign for slot details. Any group-sequential design can be converted to a fully flexible TwoStageDesign (see examples section).

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Usage

```
GroupSequentialDesign(n1, c1f, c1e, n2_pivots, c2_pivots, order = NULL, ...)
## S4 method for signature 'GroupSequentialDesign'
TwoStageDesign(n1, ...)
```

Arguments

n1	stage one sample size or GroupSequentialDesign object to convert (overloaded from ${\sf TwoStageDesign})$
c1f	early futility stopping boundary
c1e	early efficacy stopping boundary
n2_pivots	numeric of length one, stage-two sample size
c2_pivots	numeric vector, stage-two critical values on the integration pivot points
order	of the Gaussian uadrature rule to use for integration, set to length(c2_pivots) if NULL, otherwise first value of c2_pivots is repeated 'order'-times.
	further optional arguments

See Also

TwoStageDesign for superclass and inherited methods

Examples

```
design <- GroupSequentialDesign(25, 0, 2, 25, c(1, 1.5, 2.5)) summary(design)

TwoStageDesign(design)
```

make_tunable

Fix parameters during optimization

Description

The methods make_fixed and make_tunable can be used to modify the 'tunability' status of parameters in a TwoStageDesign object. Tunable parameters are optimized over, non-tunable ('fixed') parameters are considered given and not altered during optimization.

Usage

```
make_tunable(x, ...)
## S4 method for signature 'TwoStageDesign'
make_tunable(x, ...)

make_fixed(x, ...)

## S4 method for signature 'TwoStageDesign'
make_fixed(x, ...)
```

Arguments

- x TwoStageDesign object
- ... unquoted names of slots for which the tunability status should be changed.

See Also

TwoStageDesign, tunable_parameters for converting tunable parameters of a design object to a numeric vector (and back), and minimize for the actual minimization procedure

Examples

```
design <- TwoStageDesign(25, 0, 2, 25, 2, order = 5)
# default: all parameters are tunable (except integration pivots,
# weights and tunability status itself)
design@tunable

# make n1 and the pivots of n2 fixed (not changed during optimization)
design <- make_fixed(design, n1, n2_pivots)
design@tunable

# make them tunable again
design <- make_tunable(design, n1, n2_pivots)
design@tunable</pre>
```

MaximumSampleSize-class

Maximum Sample Size of a Design

Description

This score evaluates max(n(d)) for a design d.

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Usage

```
MaximumSampleSize(label = "max(n(x1))")
## S4 method for signature 'MaximumSampleSize,TwoStageDesign'
evaluate(s, design, optimization = FALSE, ...)
```

Arguments

label object label (string)

s Score object

design object

optimization logical, if TRUE uses a relaxation to real parameters of the underlying design; used for smooth optimization.

... further optional arguments

See Also

Scores for general scores and ConditionalSampleSize for evaluating the sample size point-wise.

Examples

```
design <- TwoStageDesign(50, .0, 2.0, 50, 2.0, order = 5L)
mss <- MaximumSampleSize()
evaluate(mss, design)</pre>
```

minimize

Find optimal two-stage design by constraint minimization

Description

minimize takes an unconditional score and a constraint set (or no constraint) and solves the corresponding minimization problem using nloptr (using COBYLA by default). An initial design has to be defined. It is also possible to define lower- and upper-boundary designs. If this is not done, the boundaries are determined automatically heuristically.

Usage

```
minimize(
  objective,
  subject_to,
  initial_design,
  lower_boundary_design = get_lower_boundary_design(initial_design),
  upper_boundary_design = get_upper_boundary_design(initial_design),
  opts = list(algorithm = "NLOPT_LN_COBYLA", xtol_rel = 1e-05, maxeval = 10000),
  ...
)
```

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Arguments

Value

a list with elements:

design The resulting optimal design

nloptr_return Output of the corresponding nloptr call

call_args The arguments given to the optimization call

```
# Define Type one error rate
toer <- Power(Normal(), PointMassPrior(0.0, 1))</pre>
# Define Power at delta = 0.4
pow <- Power(Normal(), PointMassPrior(0.4, 1))</pre>
# Define expected sample size at delta = 0.4
ess <- ExpectedSampleSize(Normal(), PointMassPrior(0.4, 1))</pre>
# Compute design minimizing ess subject to power and toer constraints
## Not run:
minimize(
   ess,
   subject_to(
      toer <= 0.025,
      pow >= 0.9
   ),
   initial_design = TwoStageDesign(50, .0, 2.0, 60.0, 2.0, 5L)
)
## End(Not run)
```

n1

Description

Methods to access the stage-one, stage-two, or overall sample size of a TwoStageDesign. n1 returns the first-stage sample size of a design, n2 the stage-two sample size conditional on the stage-one test statistic and n the overall sample size n1 + n2. Internally, objects of the class TwoStageDesign allow non-natural, real sample sizes to allow smooth optimization (cf. minimize for details). The optional argument round allows to switch between the internal real representation and a rounded version (rounding to the next positive integer).

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Usage

```
n1(d, ...)
## S4 method for signature 'TwoStageDesign'
n1(d, round = TRUE, ...)

n2(d, x1, ...)

## S4 method for signature 'TwoStageDesign,numeric'
n2(d, x1, round = TRUE, ...)

n(d, x1, ...)

## S4 method for signature 'TwoStageDesign,numeric'
n(d, x1, round = TRUE, ...)

## S4 method for signature 'GroupSequentialDesign,numeric'
n2(d, x1, round = TRUE, ...)

## S4 method for signature 'OneStageDesign,numeric'
n2(d, x1, ...)
```

Arguments

```
d design
... further optional arguments
round logical should sample sizes be rounded to next integer?
x1 stage-one test statistic
```

See Also

TwoStageDesign, see c2 for accessing the critical values

N1-class

Examples

```
design <- TwoStageDesign(
    n1 = 25,
    c1f = 0,
    c1e = 2.5,
    n2 = 50,
    c2 = 1.96,
    order = 7L
)

n1(design) # 25
design@n1 # 25
n(design, x1 = 2.2) # 75</pre>
```

N1-class

Regularize n1

Description

N1 is a class that computes the n1 value of a design. This can be used as a score in minimize.

Usage

```
N1(label = NA_character_)
## S4 method for signature 'N1,TwoStageDesign'
evaluate(s, design, optimization = FALSE, ...)
```

Arguments

```
label object label (string)

s Score object

design object

optimization logical, if TRUE uses a relaxation to real parameters of the underlying design; used for smooth optimization.

... further optional arguments
```

Value

an object of class N1

See Also

See AverageN2 for a regularization of the second-stage sample size.

Normal-class 27

Examples

```
n1_score <- N1()
evaluate(
   N1(),
   TwoStageDesign(70, 0, 2, rep(60, 6), rep(1.7, 6))
) # 70</pre>
```

Normal-class

Normal data distribution

Description

Implements a normal data distribution for z-values given an observed z-value and stage size. Standard deviation is 1 and mean $\theta\sqrt{n}$ where θ is the standardized effect size. The option two_armed can be set to decide whether a one-arm or a two-arm design should be computed.

Usage

```
Normal(two_armed = TRUE)
## S4 method for signature 'Normal'
quantile(x, probs, n, theta, ...)
## S4 method for signature 'Normal,numeric'
simulate(object, nsim, n, theta, seed = NULL, ...)
```

Arguments

two_armed	logical indicating if a two-armed trial is regarded
x	outcome
probs	vector of probabilities
n	sample size
theta	distribution parameter
	further optional arguments
object	object of class Normal
nsim	number of simulation runs
seed	random seed

Details

See DataDistribution-class for more details.

See Also

see probability_density_function and cumulative_distribution_function to evaluate the pdf and the cdf, respectively.

Examples

```
datadist <- Normal(two_armed = TRUE)</pre>
```

OneStageDesign-class One-stage designs

Description

OneStageDesign implements a one-stage design as special case of a two-stage design, i.e. as subclass of TwoStageDesign. This is possible by defining $n_2=0,\,c=c_1^f=c_1^e,\,c_2(x_1)=ifelse(x_1< c,Inf,-Inf)$. No integration pivots etc are required (set to NaN).

Usage

```
OneStageDesign(n, c)
## S4 method for signature 'OneStageDesign'
TwoStageDesign(n1, order = 5L, eps = 0.01, ...)
## S4 method for signature 'OneStageDesign'
plot(x, y, ...)
```

Arguments

n	sample size (stage-one sample size)
С	rejection boundary $(c = c_1^f = c_1^e)$
n1	OneStageDesign object to convert, overloaded from TwoStageDesign
order	integer >= 2, default is 5; order of Gaussian quadrature integration rule to use for new TwoStageDesign.
eps	numeric > 0, default = .01; the single critical value c must be split in a continuation interval [c1f, c1e]; this is given by $c +/-eps$.
• • •	further optional arguments
x	design to plot
У	not used

Details

Note that the default plot, TwoStageDesign-method method is not supported for OneStageDesign objects.

See Also

TwoStageDesign, GroupSequentialDesign

Examples

```
design <- OneStageDesign(30, 1.96)
summary(design)
design <- TwoStageDesign(design)
summary(design)</pre>
```

```
plot, TwoStageDesign-method
```

Plot TwoStageDesign with optional set of conditional scores

Description

This method allows to plot the stage-two sample size and decision boundary functions of a chosen design.

Usage

```
## S4 method for signature 'TwoStageDesign'
plot(x, y = NULL, ..., rounded = TRUE, k = 100)
```

Arguments

X	design to plot
У	not used
• • •	$further \ named \ Condition al Scores \ to \ plot \ for \ the \ design \ and/or \ further \ graphic \ parameters$
rounded	should n-values be rounded?
k	number of points to use for plotting

Details

TwoStageDesign and user-defined elements of the class ConditionalScore.

See Also

TwoStageDesign

```
design <- TwoStageDesign(50, 0, 2, 50, 2, 5)
cp <- ConditionalPower(dist = Normal(), prior = PointMassPrior(.4, 1))
plot(design, "Conditional Power" = cp, cex.axis = 2)</pre>
```

30 PointMassPrior-class

PointMassPrior-class Univariate discrete point mass priors

Description

PointMassPrior is a sub-class of Prior representing a univariate prior over a discrete set of points with positive probability mass.

Usage

```
PointMassPrior(theta, mass, label = NA_character_)
```

Arguments

theta numeric vector of pivot points with positive prior mass

mass numeric vector of probability masses at the pivot points (must sum to 1)

label object label (string)

Value

an object of class PointMassPrior, theta is automatically sorted in ascending order

Slots

```
theta cf. parameter 'theta' mass cf. parameter 'mass'
```

See Also

To represent continuous prior distributions use ContinuousPrior.

```
PointMassPrior(c(0, .5), c(.3, .7))
```

posterior 31

post	er	10	٦r

Compute posterior distribution

Description

Return posterior distribution given observing stage-one outcome.

Usage

```
posterior(dist, prior, x1, n1, ...)
## S4 method for signature 'DataDistribution,PointMassPrior,numeric'
posterior(dist, prior, x1, n1, ...)
## S4 method for signature 'DataDistribution,ContinuousPrior,numeric'
posterior(dist, prior, x1, n1, ...)
```

Arguments

```
dist a univariate distribution object
prior a Prior object
x1 stage-one test statistic
n1 stage-one sample size
... further optional arguments
```

Value

Object of class Prior

```
posterior(Normal(), PointMassPrior(0, 1), 2, 20) 
 tmp \leftarrow ContinuousPrior(function(x) \ dunif(x, .2, .4), \ c(.2, .4)) \\ posterior(Normal(), \ tmp, 2, 20)
```

32 predictive_cdf

predictive_cdf

Predictive CDF

Description

predictive_cdf() evaluates the predictive CDF of the model specified by a DataDistribution dist and Prior at the given stage-one outcome.

Usage

```
predictive_cdf(dist, prior, x1, n1, ...)

## S4 method for signature 'DataDistribution,PointMassPrior,numeric'
predictive_cdf(dist, prior, x1, n1, ...)

## S4 method for signature 'DataDistribution,ContinuousPrior,numeric'
predictive_cdf(
    dist,
    prior,
    x1,
    n1,
    k = 10 * (prior@support[2] - prior@support[1]) + 1,
    ...
)
```

Arguments

```
dist a univariate distribution object

prior a Prior object

x1 stage-one test statistic

n1 stage-one sample size

... further optional arguments

k number of pivots for crude integral approximation
```

Value

numeric, value of the predictive CDF

```
\label{eq:predictive_cdf(Normal(), PointMassPrior(.0, 1), 0, 20) \# .5} $$$ tmp <- ContinuousPrior(function(x) dunif(x, .2, .4), c(.2, .4)) $$ predictive_cdf(Normal(), tmp, 2, 20) $$
```

predictive_pdf 33

predictive_pdf

Predictive PDF

Description

predictive_pdf() evaluates the predictive PDF of the model specified by a DataDistribution dist and Prior at the given stage-one outcome.

Usage

```
predictive_pdf(dist, prior, x1, n1, ...)

## S4 method for signature 'DataDistribution,PointMassPrior,numeric'
predictive_pdf(dist, prior, x1, n1, ...)

## S4 method for signature 'DataDistribution,ContinuousPrior,numeric'
predictive_pdf(
    dist,
    prior,
    x1,
    n1,
    k = 10 * (prior@support[2] - prior@support[1]) + 1,
    ...
)
```

Arguments

```
dist a univariate distribution object

prior a Prior object

x1 stage-one test statistic

n1 stage-one sample size

... further optional arguments

k number of pivots for crude integral approximation
```

Value

numeric, value of the predictive PDF

```
predictive_pdf(Normal(), PointMassPrior(.3, 1), 1.5, 20) # ~.343

tmp <- ContinuousPrior(function(x) dunif(x, .2, .4), c(.2, .4))
predictive_pdf(Normal(), tmp, 2, 20)</pre>
```

Prior-class

```
print.adoptrOptimizationResult
```

Printing an optimization result

Description

Printing an optimization result

Usage

```
print(x, ...)
```

Arguments

x object to print

... further arguments passed form other methods

Prior-class

Univariate prior on model parameter

Description

A Prior object represents a prior distribution on the single model parameter of a DataDistribution class object. Together a prior and data-distribution specify the class of the joint distribution of the test statistic, X, and its parameter, theta. Currently, **adoptr** only allows simple models with a single parameter. Implementations for PointMassPrior and ContinuousPrior are available.

Details

For an example on working with priors, see here.

See Also

For the available methods, see bounds, expectation, condition, predictive_pdf, predictive_cdf, posterior

```
disc_prior <- PointMassPrior(c(0.1, 0.25), c(0.4, 0.6))
cont_prior <- ContinuousPrior(
  pdf = function(x) dnorm(x, mean = 0.3, sd = 0.2),
  support = c(-2, 3)
)</pre>
```

Description

probability_density_function evaluates the probability density function of a specific distribution dist at a point x.

Usage

```
probability_density_function(dist, x, n, theta, ...)
## S4 method for signature 'Binomial,numeric,numeric,numeric'
probability_density_function(dist, x, n, theta, ...)
## S4 method for signature 'Normal,numeric,numeric,numeric'
probability_density_function(dist, x, n, theta, ...)
## S4 method for signature 'Student,numeric,numeric,numeric'
probability_density_function(dist, x, n, theta, ...)
```

Arguments

```
dist a univariate distribution object
x outcome
n sample size
theta distribution parameter
... further optional arguments
```

Details

If the distribution is Binomial, theta denotes the rate difference between intervention and control group. Then, the mean is assumed to be $\sqrt{n}theta$.

If the distribution is Normal, then the mean is assumed to be $\sqrt{n}theta$.

```
probability_density_function(Binomial(.2, FALSE), 1, 50, .3)
probability_density_function(Normal(), 1, 50, .3)
probability_density_function(Student(TRUE), 1, 40, 1.1)
```

36 Scores

res Scores

Description

In adoptr scores are used to assess the performance of a design. This can be done either conditionally on the observed stage-one outcome or unconditionally. Consequently, score objects are either of class ConditionalScore or UnconditionalScore.

Usage

```
expected(s, data_distribution, prior, ...)
## S4 method for signature 'ConditionalScore'
expected(s, data_distribution, prior, label = NA_character_, ...)
evaluate(s, design, ...)
## S4 method for signature 'IntegralScore,TwoStageDesign'
evaluate(s, design, optimization = FALSE, subdivisions = 10000L, ...)
```

Arguments

s Score object data_distribution

DataDistribution object

prior a Prior object

... further optional arguments

label object label (string)

design object

optimization logical, if TRUE uses a relaxation to real parameters of the underlying design;

used for smooth optimization.

subdivisions maximal number of subdivisions when evaluating an integral score using adap-

tive quadrature (optimization = FALSE)

Details

All scores can be evaluated on a design using the evaluate method. Note that evaluate requires a third argument x1 for conditional scores (observed stage-one outcome). Any ConditionalScore can be converted to a UnconditionalScore by forming its expected value using expected. The returned unconditional score is of class IntegralScore.

See Also

ConditionalPower, ConditionalSampleSize, composite

Examples

```
design <- TwoStageDesign(</pre>
 n1 = 25,
  c1f = 0,
 c1e = 2.5,
       = 50,
  n2
      = 1.96,
 order = 7L
prior <- PointMassPrior(.3, 1)</pre>
# conditional
cp <- ConditionalPower(Normal(), prior)</pre>
expected(cp, Normal(), prior)
evaluate(cp, design, x1 = .5)
# unconditional
power <- Power(Normal(), prior)</pre>
evaluate(power, design)
evaluate(power, design, optimization = TRUE) # use non-adaptive quadrature
```

```
simulate, {\tt TwoStageDesign}, numeric-method\\ Draw\ samples\ from\ a\ two-stage\ design
```

Description

simulate allows to draw samples from a given TwoStageDesign.

Usage

```
## S4 method for signature 'TwoStageDesign,numeric'
simulate(object, nsim, dist, theta, seed = NULL, ...)
```

Arguments

object	TwoStageDesign to draw samples from
nsim	number of simulation runs
dist	data distribution
theta	location parameter of the data distribution
seed	random seed
	further optional arguments

38 Student-class

Value

simulate() returns a data.frame with nsim rows and for each row (each simulation run) the following columns

- theta The effect size
- n1 First-stage sample size
- c1f Stopping for futility boundary
- cle Stopping for efficacy boundary
- x1 First-stage outcome
- n2 Resulting second-stage sample size after observing x1
- c2 Resulting second-stage decision-boundary after observing x1
- x2 Second-stage outcome
- reject Decision whether the null hypothesis is rejected or not

See Also

```
TwoStageDesign
```

Examples

```
design <- TwoStageDesign(25, 0, 2, 25, 2, order = 5)
# draw samples assuming two-armed design
simulate(design, 10, Normal(), .3, 42)</pre>
```

Student-class

Student's t data distribution

Description

Implements exact t-distributions instead of a normal approximation

Usage

```
Student(two_armed = TRUE)
## S4 method for signature 'Student'
quantile(x, probs, n, theta, ...)
## S4 method for signature 'Student,numeric'
simulate(object, nsim, n, theta, seed = NULL, ...)
```

subject_to 39

Arguments

two_armed logical indicating if a two-armed trial is regarded

x outcome

probs vector of probabilities

n sample size

theta distribution parameter
... further optional arguments
object object of class Student
nsim number of simulation runs

seed random seed

See Also

see probability_density_function and cumulative_distribution_function to evaluate the pdf and the cdf, respectively.

Examples

```
datadist <- Student(two_armed = TRUE)</pre>
```

subject_to

Create a collection of constraints

Description

subject_to(...) can be used to generate an object of class ConstraintsCollection from an arbitrary number of (un)conditional constraints.

Usage

```
subject_to(...)
## S4 method for signature 'ConstraintsCollection,TwoStageDesign'
evaluate(s, design, optimization = FALSE, ...)
```

Arguments

... either constraint objects (for subject_to or optional arguments passed to evaluate)

s object of class ConstraintCollection

design object

optimization logical, if TRUE uses a relaxation to real parameters of the underlying design;

used for smooth optimization.

40 tunable_parameters

Value

an object of class ConstraintsCollection

See Also

subject_to is intended to be used for constraint specification the constraints in minimize.

Examples

```
# define type one error rate and power
toer <- Power(Normal(), PointMassPrior(0.0, 1))
power <- Power(Normal(), PointMassPrior(0.4, 1))

# create constrain collection
subject_to(
  toer <= 0.025,
   power >= 0.9
)
```

tunable_parameters

Switch between numeric and S4 class representation of a design

Description

Get tunable parameters of a design as numeric vector via tunable_parameters or update a design object with a suitable vector of values for its tunable parameters.

Usage

```
tunable_parameters(object, ...)
## S4 method for signature 'TwoStageDesign'
tunable_parameters(object, ...)
## S4 method for signature 'TwoStageDesign'
update(object, params, ...)
## S4 method for signature 'OneStageDesign'
update(object, params, ...)
```

Arguments

object TwoStageDesign object to update
... further optional arguments

vector of design parameters, must be in same order as returned by tunable_parameters

Details

The tunable slot of a TwoStageDesign stores information about the set of design parameters which are considered fixed (not changed during optimization) or tunable (changed during optimization). For details on how to fix certain parameters or how to make them tunable again, see make_fixed and make_tunable.

See Also

```
TwoStageDesign
```

Examples

```
design <- TwoStageDesign(25, 0, 2, 25, 2, order = 5)
tunable_parameters(design)
design2 <-update(design, tunable_parameters(design) + 1)
tunable_parameters(design2)</pre>
```

TwoStageDesign-class Two-stage designs

Description

TwoStageDesign is the fundamental design class of the **adoptr** package. Formally, we represent a generic two-stage design as a five-tuple $(n_1, c_1^f, c_1^e, n_2(\cdot), c_2(\cdot))$. Here, n_1 is the first-stage sample size (per group), c_1^f and c_1^e are boundaries for early stopping for futility and efficacy, respectively. Since the trial design is a two-stage design, the elements $n_2(\cdot)$ (stage-two sample size) and $c_2(\cdot)$ (stage-two critical value) are functions of the first-stage outcome $X_1 = x_1$. X_1 denotes the first-stage test statistic. A brief description on this definition of two-stage designs can be read here. For available methods, see the 'See Also' section at the end of this page.

Usage

```
TwoStageDesign(n1, ...)
## S4 method for signature 'numeric'
TwoStageDesign(n1, c1f, c1e, n2_pivots, c2_pivots, order = NULL, ...)
## S4 method for signature 'TwoStageDesign'
summary(object, ..., rounded = TRUE)
```

Arguments

```
n1 stage-one sample size... further optional argumentsc1f early futility stopping boundary
```

c1e early efficacy stopping boundary

n2_pivots numeric vector, stage-two sample size on the integration pivot points c2_pivots numeric vector, stage-two critical values on the integration pivot points

order integer, integration order of the employed Gaussian quadrature integration rule

to evaluate scores. Automatically set to length(n2_pivots) if

 $length(n2_pivots) == length(c2_pivots) > 1$, otherwise c2 and n2 are taken to be constant in stage-two and replicated to match the number of pivots speci-

fied by order

object object to show

rounded should rounded n-values be used?

Details

summary can be used to quickly compute and display basic facts about a TwoStageDesign. An arbitrary number of names UnconditionalScore objects can be provided via the optional arguments . . . and are included in the summary displayed using print.

Slots

```
n1 cf. parameter 'n1'
c1f cf. parameter 'c1f'
```

c1e cf. parameter 'c1e'

n2_pivots vector of length 'order' giving the values of n2 at the pivot points of the numeric integration rule

c2_pivots vector of length order giving the values of c2 at the pivot points of the numeric integration rule

x1_norm_pivots normalized pivots for integration rule (in [-1, 1]) the actual pivots are scaled to the interval [c1f, c1e] and can be obtained by the internal method adoptr:::scaled_integration_pivots(design)

weights weights of of integration rule at x1_norm_pivots for approximating integrals over x1

tunable named logical vector indicating whether corresponding slot is considered a tunable parameter (i.e. whether it can be changed during optimization via minimize or not; cf. make_fixed)

See Also

For accessing sample sizes and critical values safely, see methods in n and c2; for modifying behaviour during optimizaton see make_tunable; to convert between S4 class representation and numeric vector, see tunable_parameters; for simulating from a given design, see simulate; for plotting see plot, TwoStageDesign-method. Both group-sequential and one-stage designs (!) are implemented as subclasses of TwoStageDesign.

```
design <- TwoStageDesign(50, 0, 2, 50.0, 2.0, 5)
pow <- Power(Normal(), PointMassPrior(.4, 1))
summary(design, "Power" = pow)</pre>
```

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