

# Package ‘ccdf’

September 24, 2021

**Type** Package

**Title** Distribution-Free Single-Cell Differential Expression Analysis

**Version** 1.1.4

**Imports** pbapply,parallel,matrixStats,CompQuadForm, RcppNumerical,  
doParallel, foreach, ggplot2, randomForest, rpart, statmod,  
viridisLite, survey, cowplot

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## Description

Complex hypothesis testing through conditional cumulative distribution function estimation.  
Method is detailed in: Gauthier M, Agniel D, Thiebaut R & Hejblum BP (2020).  
“Distribution-free complex hypothesis testing for single-cell RNA-  
seq differential expression analysis”, BioRxiv <[doi:10.1101/2021.05.21.445165](https://doi.org/10.1101/2021.05.21.445165)>.

**License** GPL (>= 3)

**Encoding** UTF-8

**RoxygenNote** 7.1.1

**Depends** R (>= 3.6)

**BugReports** <https://github.com/mgauth/ccdf/issues>

**NeedsCompilation** no

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**Repository** CRAN

**Date/Publication** 2021-09-24 08:00:05 UTC

## R topics documented:

CCDF . . . . .	2
ccdf_testing . . . . .	3
perm_cont . . . . .	5
plot_CCDF . . . . .	6
plot_pvals . . . . .	7

test_asymp	8
test_perm	9

<b>Index</b>	<b>11</b>
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CCDF	<i>Function to compute (un)conditional cumulative distribution function (CDF), used by plot_CCDF function.</i>
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### Description

Function to compute (un)conditional cumulative distribution function (CDF), used by plot\_CCDF function.

### Usage

```
CCDF(
  Y,
  X,
  Z = NULL,
  method = c("linear regression", "logistic regression", "RF"),
  fast = TRUE,
  space_y = FALSE,
  number_y = length(Y)
)
```

### Arguments

Y	a numeric vector of size n containing the preprocessed expressions from n samples (or cells).
X	a data frame containing numeric or factor vector(s) of size n containing the variable(s) to be tested (the condition(s) to be tested).
Z	a data frame containing numeric or factor vector(s) of size n containing the covariate(s).
method	a character string indicating which method to use to compute the CCDF, either 'linear regression', 'logistic regression' and 'permutations' or 'RF' for Random Forests. Default is 'linear regression' since it is the method used in the test.
fast	a logical flag indicating whether the fast implementation of logistic regression should be used. Only if 'dist_permutations' is specified. Default is TRUE.
space_y	a logical flag indicating whether the y thresholds are spaced. When space_y is TRUE, a regular sequence between the minimum and the maximum of the observations is used. Default is FALSE.
number_y	an integer value indicating the number of y thresholds (and therefore the number of regressions) to perform the test. Default is length(Y).

**Value**

A list with the following elements:

- `cdf`: a vector of the cumulative distribution function of a given gene.
- `ccdf`: a vector of the conditional cumulative distribution function of a given gene, computed given `X`. Only if `Z` is `NULL`.
- `ccdf_nox`: a vector of the conditional cumulative distribution function of a given gene, computed given `Z` only (i.e. `X` is ignored.). Only if `Z` is not `NULL`.
- `ccdf_x`: a vector of the conditional cumulative distribution function of a given gene, computed given `X` and `Z`. Only if `Z` is not `NULL`.
- `y_sort`: a vector of the sorted expression points at which the CDF and the CCDFs are calculated.
- `x_sort`: a vector of the variables associated with `y_sort`.
- `z_sort`: a vector of the covariates associated with `y_sort`. Only if `Z` is not `NULL`.

**Examples**

```
X <- as.factor(rbinom(n=100, size = 1, prob = 0.5))
Y <- ((X==1)*rnorm(n = 50,0,1)) + ((X==0)*rnorm(n = 50,0.5,1))
res <- CCDF(Y,data.frame(X=X),method="linear regression")
```

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<code>ccdf_testing</code>	<i>Main function to perform complex hypothesis testing using (un)conditional independence test</i>
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**Description**

Main function to perform complex hypothesis testing using (un)conditional independence test

**Usage**

```
ccdf_testing(
  exprmat = NULL,
  variable2test = NULL,
  covariate = NULL,
  distance = c("L2", "L1", "L_sup"),
  test = c("asymptotic", "permutations", "dist_permutations"),
  method = c("linear regression", "logistic regression", "RF"),
  fast = TRUE,
  n_perm = 100,
  n_perm_adaptive = c(100, 150, 250, 500),
  thresholds = c(0.1, 0.05, 0.01),
  parallel = TRUE,
  n_cpus = NULL,
```

```

    adaptive = FALSE,
    space_y = FALSE,
    number_y = ncol(exprmat)
)

```

## Arguments

<code>exprmat</code>	a data frame of size $G \times n$ containing the preprocessed expressions from $n$ samples (or cells) for $G$ genes. Default is NULL.
<code>variable2test</code>	a data frame of numeric or factor vector(s) of size $n$ containing the variable(s) to be tested (the condition(s))
<code>covariate</code>	a data frame of numeric or factor vector(s) of size $n$ containing the covariate(s)
<code>distance</code>	a character string indicating which distance to use to compute the test, either 'L2', 'L1' or 'L <sub>sup</sub> ', when method is 'dist_permutations', Default is 'L2'.
<code>test</code>	a character string indicating which method to use to compute the test, either 'asymptotic', 'permutations' or 'dist_permutations'. 'dist_permutations' allows to compute the distance between the CDF and the CCDF or two CCDFs. Default is 'asymptotic'.
<code>method</code>	a character string indicating which method to use to compute the CCDF, either 'linear regression', 'logistic regression' and 'permutations' or 'RF' for Random Forests. Default is 'linear regression' since it is the method used in the test.
<code>fast</code>	a logical flag indicating whether the fast implementation of logistic regression should be used. Only if 'dist_permutations' is specified. Default is TRUE.
<code>n_perm</code>	the number of permutations. Default is 100.
<code>n_perm_adaptive</code>	a vector of the increasing numbers of adaptive permutations when adaptive is TRUE. $\text{length}(n\_perm\_adaptive)$ should be equal to $\text{length}(thresholds)+1$ . Default is $c(0.1, 0.05, 0.01)$ .
<code>thresholds</code>	a vector of the decreasing thresholds to compute adaptive permutations when adaptive is TRUE. $\text{length}(thresholds)$ should be equal to $\text{length}(n\_perm\_adaptive)-1$ . Default is $c(100, 150, 250, 500)$ .
<code>parallel</code>	a logical flag indicating whether parallel computation should be enabled. Default is TRUE.
<code>n_cpus</code>	an integer indicating the number of cores to be used when parallel is TRUE. Default is <code>parallel::detectCores() - 1</code> .
<code>adaptive</code>	a logical flag indicating whether adaptive permutations should be performed. Default is FALSE.
<code>space_y</code>	a logical flag indicating whether the y thresholds are spaced. When <code>space_y</code> is TRUE, a regular sequence between the minimum and the maximum of the observations is used. Default is FALSE.
<code>number_y</code>	an integer value indicating the number of y thresholds (and therefore the number of regressions) to perform the test. Default is <code>ncol(exprmat)</code> .

**Value**

A list with the following elements:

- `which_test`: a character string carrying forward the value of the `'which_test'` argument indicating which test was performed (either `'asymptotic'`, `'permutations'`, `'dist_permutations'`).
- `n_perm`: an integer carrying forward the value of the `'n_perm'` argument or `'n_perm_adaptive'` indicating the number of permutations performed (NA if asymptotic test was performed).
- `pval`: computed p-values. A data frame with one row for each gene, and with 2 columns: the first one `'raw_pval'` contains the raw p-values, the second one `'adj_pval'` contains the FDR adjusted p-values using Benjamini-Hochberg correction.

**References**

Gauthier M, Agniel D, Thiébaud R & Hejblum BP (2019). Distribution-free complex hypothesis testing for single-cell RNA-seq differential expression analysis, *bioRxiv* 445165. [DOI: 10.1101/2021.05.21.445165](https://doi.org/10.1101/2021.05.21.445165).

**Examples**

```
X <- as.factor(rbinom(n=100, size = 1, prob = 0.5))
Y <- t(replicate(10, ((X==1)*rnorm(n = 50,0,1)) + ((X==0)*rnorm(n = 50,0.5,1))))
res_asymp <- ccdf_testing(exprmat=data.frame(Y=Y),
variable2test=data.frame(X=X), test="asymptotic",
n_cpus=1)$pvals # asymptotic test
```

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perm\_cont

*Permutation procedure when Z is continuous*


---

**Description**

Permutation procedure when Z is continuous

**Usage**

```
perm_cont(Y, X, Z)
```

**Arguments**

- |   |   |
|---|---|
| Y | a numeric vector of size n containing the preprocessed expressions from n samples (or cells).           |
| X | a numeric or factor vector of size n containing the variable to be tested (the condition to be tested). |
| Z | a numeric vector of size n containing the covariate. Multiple variables are not allowed.                |

**Value**

X\_star a vector of permuted X.

**Examples**

```
if(interactive()){
  X <- rbinom(n=100, size = 1, prob = 0.5)
  Z <- rnorm(100,0,1)
  Y <- ((X==1)*rnorm(n = 50,0,1)) + ((X==0)*rnorm(n = 50,0.5,1))
  res <- perm_cont(Y,X,Z)}
```

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plot\_CCDF

*Function to plot the CCDF according to the type of X et Z*

---

**Description**

Function to plot the CCDF according to the type of X et Z

**Usage**

```
plot_CCDF(
  Y,
  X,
  Z = NULL,
  method = "linear regression",
  fast = TRUE,
  space_y = FALSE,
  number_y = length(Y)
)
```

**Arguments**

- |        |   |
|--------|---|
| Y      | a numeric vector of size n containing the preprocessed expressions from n samples (or cells).   |
| X      | a numeric or factor vector of size n containing the variable to be tested (the condition to be tested).   |
| Z      | a numeric or factor vector of size n containing the covariate. Multiple variables are not allowed.  |
| method | a character string indicating which method to use to compute the CCDF, either 'linear regression', 'logistic regression' and 'permutations' or 'RF' for Random Forests. Default is 'linear regression' since it is the method used in the test. |
| fast   | a logical flag indicating whether the fast implementation of logistic regression should be used. Only if 'dist_permutations' is specified. Default is TRUE.   |

- space\_y a logical flag indicating whether the y thresholds are spaced. When space\_y is TRUE, a regular sequence between the minimum and the maximum of the observations is used. Default is FALSE.
- number\_y an integer value indicating the number of y thresholds (and therefore the number of regressions) to perform the test. Default is length(Y).

**Value**

a `ggplot` object

**Examples**

```
X <- as.factor(rbinom(n=100, size = 1, prob = 0.5))
Y <- ((X==1)*rnorm(n = 50,0,1)) + ((X==0)*rnorm(n = 50,0.5,1))
plot_CCDF(data.frame(Y=Y),data.frame(X=X),method="linear regression")
```

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plot\_pvals

*Plot of gene-wise p-values*

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**Description**

This function prints the sorted exact p-values along with the Benjamini-Hochberg limit and the 5

**Usage**

```
plot_pvals(pvals)
```

**Arguments**

pvals a vector of length n containing the raw p-values for each gene

**Value**

a plot of sorted gene-wise p-values  
a `ggplot` object

**Examples**

```
plot_pvals(runif(100,0,1))
```

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test_asymp	<i>Asymptotic test</i>
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**Description**

Asymptotic test

**Usage**

```
test_asymp(Y, X, Z = NULL, space_y = FALSE, number_y = length(unique(Y)))
```

**Arguments**

Y	a numeric vector of size n containing the preprocessed expression for a given gene from n samples (or cells).
X	a data frame of numeric or factor vector(s) of size n containing the variable(s) to be tested (the condition(s))
Z	a data frame of numeric or factor vector(s) of size n containing the covariate(s)
space_y	a logical flag indicating whether the y thresholds are spaced. When space_y is TRUE, a regular sequence between the minimum and the maximum of the observations is used. Default is FALSE.
number_y	an integer value indicating the number of y thresholds (and therefore the number of regressions) to perform the test. Default is length(Y).

**Value**

A data frame with the following elements:

- raw\_pval contains the raw p-values for a given gene.
- Stat contains the test statistic for a given gene.

**Examples**

```
X <- as.factor(rbinom(n=100, size = 1, prob = 0.5))
Y <- ((X==1)*rnorm(n = 50,0,1)) + ((X==0)*rnorm(n = 50,0.5,1))
res_asymp <- test_asymp(Y,data.frame(X=X))
```



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test_perm	<i>Permutation test</i>
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**Description**

Permutation test

**Usage**

```
test_perm(
  Y,
  X,
  Z = NULL,
  n_perm = 100,
  parallel = FALSE,
  n_cpus = NULL,
  space_y = FALSE,
  number_y = length(Y)
)
```

**Arguments**

Y	a numeric vector of size n containing the preprocessed expression for a given gene from n samples (or cells).
X	a data frame of numeric or factor vector(s) of size n containing the variable(s) to be tested (the condition(s)). Multiple variables are not allowed.
Z	a data frame of numeric or factor vector(s) of size n containing the covariate(s). Multiple variables are not allowed.
n_perm	the number of permutations. Default is 100.
parallel	a logical flag indicating whether parallel computation should be enabled. Default is TRUE.
n_cpus	an integer indicating the number of cores to be used when parallel is TRUE. Default is <code>parallel::detectCores() - 1</code> .
space_y	a logical flag indicating whether the y thresholds are spaced. When space_y is TRUE, a regular sequence between the minimum and the maximum of the observations is used. Default is FALSE.
number_y	an integer value indicating the number of y thresholds (and therefore the number of regressions) to perform the test. Default is <code>length(Y)</code> .

**Value**

A data frame with the following elements:

- score contains the test statistic for a given gene.
- raw\_pval contains the raw p-values for a given gene computed from n\_perm permutations.

**Examples**

```
if(interactive()){  
  X <- as.factor(rbinom(n=100, size = 1, prob = 0.5))  
  Y <- ((X==1)*rnorm(n = 50,0,1)) + ((X==0)*rnorm(n = 50,0.5,1))  
  res_perm <- test_perm(Y,data.frame(X=X),n_perm=10)}
```

# Index

CCDF, [2](#)  
ccdf\_testing, [3](#)  
  
ggplot, [7](#)  
  
perm\_cont, [5](#)  
plot\_CCDF, [6](#)  
plot\_pvals, [7](#)  
  
test\_asymp, [8](#)  
test\_perm, [9](#)