

Package ‘changepointsHD’

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Title Change-Point Estimation for Expensive and High-Dimensional Models

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Description This implements the methods developed in, L. Bybee and Y. Atchade. (2018). Contains a series of methods for estimating change-points given user specified black-box models. The methods include binary segmentation for multiple change-point estimation. For estimating each individual change-point the package includes simulated annealing, brute force, and, for Gaussian graphical models, an applications specific rank-one update implementation. Additionally, code for estimating Gaussian graphical models is included. The goal of this package is to allow for the efficient estimation of change-points in complicated models with high dimensional data.

License GPL (>= 2)

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changepointsHD-package

Change-Point Estimation for Expensive and High-Dimensional Models

Description

This implements the methods developed in, L. Bybee and Y. Atchade. (2018). Contains a series of methods for estimating change-points given user specified black-box models. The methods include binary segmentation for multiple change-point estimation. For estimating each individual change-point the package includes simulated annealing, brute force, and, for Gaussian graphical models, an applications specific rank-one update implementation. Additionally, code for estimating Gaussian graphical models is included. The goal of this package is to allow for the efficient estimation of change-points in complicated models with high dimensional data.

Details

| | |
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Author(s)

Leland Bybee

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References

1. L. Bybee and Y. Atchade: "Change-Point Computation for Large Graphical Models: A Scalable Algorithm for Gaussian Graphical Models with Change-Points", 2018; [<http://jmlr.csail.mit.edu/papers/volume19/17-218/17-218.pdf>].

| | |
|--------------|---|
| bbmod_method | <i>Wrapper method for black-box estimation.</i> |
|--------------|---|

Description

Applies the black-box estimator to the specified partition given the current tau value. Additionally, this wrapper handles the different data structures possible for part_values and whole_values.

Usage

```
bbmod_method(object, part, tau)

## S4 method for signature 'changepointsMod'
bbmod_method(object, part, tau)
```

Arguments

- | | |
|--------|--|
| object | Corresponding changepointsMod class. |
| part | Index for current partition, should be 1 or 2. |
| tau | Current change-point. Should be between buff and N - buff. |

Value

An updated version of the change-point model. There are currently three possible updates depending on the form of the part_values and whole_values provided. 1) If only part_values are provided, then we assume the black-box method only updates part_values. 2) If only whole_values are provided, we assume the black-box method only updates whole_values. 3) If both part_values and whole_values are provided, we assume that both are updated.

Author(s)

Leland Bybee <lelandb@umich.edu>

| | |
|---------------------|--------------------------------------|
| binary_segmentation | <i>Multiple change-point method.</i> |
|---------------------|--------------------------------------|

Description

Estimates multiple change-points using the binary-segmentation method. This does a breadth first search and uses the specified single change-point method for each sub-search.

Usage

```
binary_segmentation(object, method, thresh = 0, buff = 100,
method_params = list())

## S4 method for signature 'changepointsMod'
binary_segmentation(object, method, thresh = 0,
buff = 100, method_params = list())
```

Arguments

| | |
|----------------------------|--|
| <code>object</code> | Corresponding <code>changepointsMod</code> class. |
| <code>method</code> | <code>changepointHD</code> method for finding single change-point. |
| <code>thresh</code> | Stopping threshold for cost comparison. |
| <code>buff</code> | Distance from edge of sample to be maintained during search. |
| <code>method_params</code> | List of additional parameters for <code>method</code> . |

Value

An updated version of the change-point model. The update will effect: 1) An estimate for the current set of change-points. 2) The `mod_list`, this will correspond to all the active single change-point models generated during the binary-segmentation procedure. Active models correspond to models that have not been superseded by more granular models. 3) The `mod_range`, this corresponds to the range of observations covered by each model. It can be used to determine which models are active.

Author(s)

Leland Bybee <lelandb@umich.edu>

Examples

```
set.seed(334)

mcp_data = read.table(system.file("extdata", "mcp.txt", package="changepointsHD"))
mcp_data = as.matrix(mcp_data)

# prox gradient black-box method
cov_est = cov(mcp_data)
init = solve(cov_est)
res_map = prox_gradient_mapping(mcp_data, init, 0.1, 0.99, 0.1, 100, 1e-20)

# prox gradient black-box l1
res_l1 = prox_gradient_l1(mcp_data, res_map, 0.1)

prox_gradient_params=list()
prox_gradient_params$update_w = 0.1
prox_gradient_params$update_change = 0.99
prox_gradient_params$regularizer = 0.1
prox_gradient_params$max_iter = 1
prox_gradient_params$tol = 1e-5
```

```

prox_gradient_ll_params=list()
prox_gradient_ll_params$regularizer = 0.1

simulated_annealing_params = list()
simulated_annealing_params$buff=10

changepoints_mod = changepointsMod(bbmod=prox_gradient_mapping,
                                    log_likelihood=prox_gradient_ll,
                                    bbmod_params=prox_gradient_params,
                                    ll_params=prox_gradient_ll_params,
                                    part_values=list(init, init),
                                    data=list(mcp_data))

changepoints_mod = binary_segmentation(changepoints_mod, method=simulated_annealing,
                                         thresh=0, buff=10,
                                         method_params=simulated_annealing_params)

```

brute_force*Single change-point brute force method.***Description**

Estimates a single change-point by testing all possible change-points.

Usage

```

brute_force(object, niter = 1, buff = 100)

## S4 method for signature 'changepointsMod'
brute_force(object, niter = 1, buff = 100)

```

Arguments

| | |
|---------------------|--|
| <code>object</code> | Corresponding <code>changepointsMod</code> class. |
| <code>niter</code> | Number of iterations at each possible change-point. |
| <code>buff</code> | Distance from edge of sample to be maintained during search. |

Value

An updated version of the change-point model. The update will effect: 1) the `part_values` and/or `whole_values` (depending on the initial values provided). 2) An estimate for the current change-point. 3) The trace for the search.

Author(s)

Leland Bybee <lelandb@umich.edu>

Examples

```

set.seed(334)

scp_data = read.table(system.file("extdata", "scp.txt", package="changepointsHD"))
scp_data = as.matrix(scp_data)

# prox gradient black-box method
cov_est = cov(scp_data)
init = solve(cov_est)
res_map = prox_gradient_mapping(scp_data, init, 0.1, 0.99, 0.1, 100, 1e-20)

# prox gradient black-box ll
res_ll = prox_gradient_ll(scp_data, res_map, 0.1)

prox_gradient_params=list()
prox_gradient_params$update_w = 0.1
prox_gradient_params$update_change = 0.99
prox_gradient_params$regularizer = 0.1
prox_gradient_params$max_iter = 1
prox_gradient_params$tol = 1e-5

prox_gradient_ll_params=list()
prox_gradient_ll_params$regularizer = 0.1

changepoints_mod = changepointsMod(bbmod=prox_gradient_mapping,
                                    log_likelihood=prox_gradient_ll,
                                    bbmod_params=prox_gradient_params,
                                    ll_params=prox_gradient_ll_params,
                                    part_values=list(init, init),
                                    data=list(scp_data))
changepoints_mod = brute_force(changepoints_mod, buff=10)

```

changepointsMod-class *An S4 class corresponding to the change-point model.*

Description

An S4 class corresponding to the change-point model.

Slots

data A list containing the data for the change-point model. The exact structure of the data is dependent on the **bbmod** and **log_likelihood** provided. In cases where the data is fairly simple, it should still be wrapped with a list, e.g. **X = list(X)**, to allow **changepointsMod** to handle it properly.

part_values A list containing the values estimated by **bbmod**. **part_values**, in particular, contain values that are updated independently for each partition (as opposed to **whole_values**).

`whole_values` A list containing the values estimated by `bbmod`. `whole` values, in particular, contain values that are shared between partitions (as opposed to `part_values`).
`bbmod` An R function for performing the black-box estimation.
`bbmod_params` A list containing any additional parameters for `bbmod`.
`log_likelihood` An R function for estimating the log-likelihood for the corresponding `bbmod`.
`ll_params` A list containing any additional parameters for `log_likelihood`.
`trace` A vector corresponding the the trace of the estimated change-points based on the method used.
`changepoints` A scalar/vector corresponding to the changepoint(s) estimated based on the method used.
`mod_list` A list corresponding to all the active single change-point models used with `binary_segmentation`.
`mod_range` A list of the range of observations corresponding to each active model for `binary_segmentation`.

Author(s)

Leland Bybee <lelandb@umich.edu>

`log_likelihood_method` *Wrapper method for log-likelihood estimation.*

Description

Generates the log-likelihood for the specified partition given the current tau value. Additionally, this wrapper handles the different data structures possible for `part_values` and `whole_values`.

Usage

```
log_likelihood_method(object, part, tau)

## S4 method for signature 'changepointsMod'
log_likelihood_method(object, part, tau)
```

Arguments

| | |
|---------------------|--|
| <code>object</code> | Corresponding <code>changepointsMod</code> class. |
| <code>part</code> | Index for current partition, should be 1 or 2. |
| <code>tau</code> | Current change-point. Should be between buff and N - buff. |

Value

The log-likelihood estimate for the current state. There are currently three possible versions depending on the form of the `part_values` and `whole_values` provided. 1) If only `part_values` are provided, then we assume the log-likelihood takes only the `part_values`. 2) If only `whole_values` are provide, we assume the log-likelihood takes only the `whole_values`. 3) If both `part_values` and `whole_values` are provided, we assume that the log-likelihood takes both.

Author(s)

Leland Bybee <lelandb@umich.edu>

prox_gradient_ll *Proximal-gradient log-likelihood estimator.*

Description

Estimates the log-likelihood for the corresponding precision matrix and data set.

Usage

```
prox_gradient_ll(data, theta_i, regularizer)
```

Arguments

| | |
|-------------|---|
| data | N x P matrix corresponding to the raw data. |
| theta_i | Estimate for precision. |
| regularizer | Regularizing constant, lambda. |

Value

Log-likelihood estimate.

Author(s)

Leland Bybee <lelandb@umich.edu>

prox_gradient_mapping *Proximal-gradient mapping method.*

Description

Performs the proximal-gradient mapping operation to estimate a regularized version of the inverse cov. matrix. Follows the procedure described in, http://dept.stat.lsa.umich.edu/~yvesa/sto_prox.pdf

Usage

```
prox_gradient_mapping(data, theta_start, update_w, update_change, regularizer,
                      max_iter, tol)
```

Arguments

| | |
|---------------|---|
| data | N x P matrix corresponding to the raw data. |
| theta_start | Initial value for precision estimate. |
| update_w | Step size for prox-gradient mapping. |
| update_change | Proportion of update_w to keep when the algorithm fails to successfully estimate precision. |
| regularizer | Regularizing constant, lambda. |
| max_iter | Number of mapping iterations. |
| tol | Tolerance at which the algorithm stops running. |

Value

Theta (precision matrix) estimate.

Author(s)

Leland Bybee <lelandb@umich.edu>

rank_one

Rank one update single change-point estimation.

Description

This is a method for estimating a single-changepoint which takes advantage of the special structure of the Gaussian graphical model. It cannot take arbitrary black-box models like simulated_annealing or brute_force. However, it can still be run within binary_segmentation.

Usage

```
rank_one(data, theta_init, buff = 10L, regularizer = 1, tau = -1L,
         max_iter = 25L, update_w = 1, update_change = 0.9, mapping_iter = 1L,
         tol = 1e-05)
```

Arguments

| | |
|---------------|---|
| data | N x P Matrix corresponding to the raw data. |
| theta_init | Initial value for theta estimate. |
| buff | Distance to maintain from edge of sample. |
| regularizer | Regularizing constant, lambda. |
| tau | Initial Estimate for change-point. |
| max_iter | Maximum number of rank-one updates to be run. |
| update_w | Step size for prox-gradient. |
| update_change | Proportion of update_w to keep when the algorithm fails to successfully estimate theta. |
| mapping_iter | Number of mapping iterations. |
| tol | Tolerance at which the algorithm stops running. |

Value

List containing the estimated change-point and theta values.

Author(s)

Leland Bybee <lelandb@umich.edu>

simulated_annealing *Single change-point simulated annealing method*

Description

Estimates a single change-point using the simulated annealing method.

Usage

```
simulated_annealing(object, niter = 500, min_beta = 1e-04, buff = 100)

## S4 method for signature 'changepointsMod'
simulated_annealing(object, niter = 500,
min_beta = 1e-04, buff = 100)
```

Arguments

| | |
|----------|--|
| object | Corresponding changepointsMod class. |
| niter | Number of simulated annealing iterations. |
| min_beta | Lowest temperature. |
| buff | Distance from edge of sample to be maintained during search. |

Value

An updated version of the change-point model. The update will effect: 1) the part_values and/or whole_values (depending on the initial values provided). 2) An estimate for the current change-point. 3) The trace for the search.

Author(s)

Leland Bybee <lelandb@umich.edu>

Examples

```
set.seed(334)

scp_data = read.table(system.file("extdata", "scp.txt", package="changepointsHD"))
scp_data = as.matrix(scp_data)

# prox gradient black-box method
cov_est = cov(scp_data)
init = solve(cov_est)
res_map = prox_gradient_mapping(scp_data, init, 0.1, 0.99, 0.1, 100, 1e-20)

# prox gradient black-box ll
res_ll = prox_gradient_ll(scp_data, res_map, 0.1)

prox_gradient_params=list()
prox_gradient_params$update_w = 0.1
prox_gradient_params$update_change = 0.99
prox_gradient_params$regularizer = 0.1
prox_gradient_params$max_iter = 1
prox_gradient_params$tol = 1e-5

prox_gradient_ll_params=list()
prox_gradient_ll_params$regularizer = 0.1

changepoints_mod = changepointsMod(bbmod=prox_gradient_mapping,
                                    log_likelihood=prox_gradient_ll,
                                    bbmod_params=prox_gradient_params,
                                    ll_params=prox_gradient_ll_params,
                                    part_values=list(init, init),
                                    data=list(scp_data))
changepoints_mod = simulated_annealing(changepoints_mod, buff=10)
```

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