Package 'cherry'

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Description Provides an alternative approach to multiple testing by calculating a simultaneous upper confidence bounds for the number of true null hypotheses among any subset of the hypotheses of interest, using the methods of Goeman and Solari (2011) <doi:10.1214/11-STS356>.
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Adjusted

Adjusted p-values for the number of true hypotheses.

Description

Calculates adjusted p-values for the number of true hypotheses on the basis of the closed testing procedure.

Usage

adjusted (closure, reject, n=0)

Arguments

| closure | An object of class closure, typically created through a call to closed . |
|---------|---|
| reject | A character vector identifying the hypotheses to be rejected. Must be a subvector of hypotheses(closure). |
| n | The maximum number of false null hypotheses allowed. |

Details

The function pick calculates adjusted p-values for intersection hypotheses of interest.

Value

The function returns a p-value (numeric).

Author(s)

Jelle Goeman: <j.j.goeman@lumc.nl>

Closed Testing

Examples

```
# Example: the birthwt data set from the MASS library
# We want to find variables associated with low birth weight
library(MASS)
fullfit <- glm(low~age+lwt+race+smoke+ptl+ht+ui+ftv, family=binomial, data=birthwt)</pre>
hypotheses <- c("age", "lwt", "race", "smoke", "ptl", "ht", "ui", "ftv")</pre>
# Define the local test to be used in the closed testing procedure
mytest <- function(hyps) {</pre>
 others <- setdiff(hypotheses, hyps)</pre>
  form <- formula(paste(c("low~", paste(c("1", others), collapse="+"))))</pre>
 anov <- anova(glm(form, data=birthwt, family=binomial), fullfit, test="Chisq")</pre>
 res <- anov$"Pr("[2]
                                           # for R >= 2.14.0
 if (is.null(res)) res <- anov$"P("[2] # earlier versions</pre>
  res
}
# Perform the closed testing with ajdusted p-values
cl <- closed(mytest, hypotheses, alpha=NA)</pre>
# What is the adjusted p-value of the intersection of the following hypotheses?
adjusted(cl, c("ht", "lwt", "smoke", "ui"))
# From what confidence level would we conclude
# that more than 2 of the following hypotheses would be false?
adjusted(cl, c("ht", "lwt", "smoke", "ui"), n=2)
```

Closed Testing Closed Testing for Exploratory Research

Description

Performs the closed testing procedure for user-specified local test.

Usage

```
closed (test, hypotheses, alpha = 0.05, adjust=FALSE)
```

Arguments

| test | A function that performs the local test. The function should accept a subvector of the hypotheses argument as input, and return a p-value. |
|------------|--|
| hypotheses | Identifiers of the collection of elementary hypotheses. |
| alpha | The significance level of the test procedure. If set to NA, the function calculates adjusted p-values for each hypothesis in the closure. |
| adjust | Whether adjusted p-values should be calculated. |

Details

The function closed performs the closed testing procedure on the collection hypotheses, testing all their intersection hypotheses and controlling the familywise error rate.

Value

The function closed returns an object of class closure.

Note

The number of intersection hypotheses is exponential in the number of elementary hypotheses. The number of elementary hypotheses is therefore limited to log2(.Machine\$integer.max+1) (typically 31) for computational reasons.

It is possible to set both adjust to TRUE and specify alpha. In that case, adjusted p-values are calculated up to a value alpha; all higher p-values are set to 1.

Author(s)

Jelle Goeman: <j.j.goeman@lumc.nl>

References

Goeman and Solari (2011) Statistical Science 26 (4) 584-597.

```
# Example: the birthwt data set from the MASS library
# We want to find variables associated with low birth weight
library(MASS)
fullfit <- glm(low~age+lwt+race+smoke+ptl+ht+ui+ftv, family=binomial, data=birthwt)</pre>
hypotheses <- c("age", "lwt", "race", "smoke", "ptl", "ht", "ui", "ftv")</pre>
# Define the local test to be used in the closed testing procedure
mytest <- function(hyps) {</pre>
  others <- setdiff(hypotheses, hyps)</pre>
  form <- formula(paste(c("low~", paste(c("1", others), collapse="+"))))</pre>
 anov <- anova(glm(form, data=birthwt, family=binomial), fullfit, test="Chisq")
 res <- anov$"Pr("[2]</pre>
                                            # for R >= 2.14.0
 if (is.null(res)) res <- anov$"P("[2] # earlier versions</pre>
  res
}
# perform the closed testing
cl <- closed(mytest, hypotheses)</pre>
cl
# how many variables among a chosen set are associated with the response?
pick(cl, c("ht", "lwt", "smoke", "ui"))
# adjusted p-values and a confidence distribution
cl <- closed(mytest, hypotheses, alpha=NA)</pre>
```

Closure class

```
pick(cl, c("ht", "lwt", "smoke", "ui"))
```

Closure class

Class "closure" for storing the result of the closed testing procedure

Description

The class closure is the output of a call to closed. It stores the information needed to calculate confidence sets for the number of true and/or false hypotheses among a selected set.

Slots

These slots are not meant to be directly accessed by the user.

adjusted: Object of class "numeric". Sores the adjusted p-values.

- defining: Object of class "integer". Stores the identifiers of the intersection hypotheses that are the defining rejections of the closed testing procedure. The identifiers should be read as binary booleans, i.e. 19 = 10011 (binary) is the intersection of the first, second and fifth elementary hypothesis.
- hypotheses: Object of class "character". Holds the names of the elementary hypotheses.
- alpha: Object of class "numeric". The type I error level chosen.
- max.alpha: Object of class "numeric". The largest value for which adjusted p-values have been calculated.

Methods

- **show** (closure): Prints a brief description of the test results, including the upper bound of the number of true hypotheses and the corresponding lower bound to the number of false hypotheses among the full set.
- summary (closure): Prints the test results (as show) plus the defining rejections.

defining (closure): Extracts the defining rejections as a list.

shortlist (closure): Extracts the shortlist as a list.

hypotheses (closure): Extracts the hypotheses slot.

Author(s)

Jelle Goeman: <j.j.goeman@lumc.nl>

See Also

closed, pick.

Examples

```
# Example: the birthwt data set from the MASS library
# We want to find variables associated with low birth weight
library(MASS)
fullfit <- glm(low~age+lwt+race+smoke+ptl+ht+ui+ftv, family=binomial, data=birthwt)</pre>
hypotheses <- c("age", "lwt", "race", "smoke", "ptl", "ht", "ui", "ftv")</pre>
# Define the local test to be used in the closed testing procedure
mytest <- function(hyps) {</pre>
  others <- setdiff(hypotheses, hyps)</pre>
  form <- formula(paste(c("low~", paste(c("1", others), collapse="+"))))</pre>
 anov <- anova(glm(form, data=birthwt, family=binomial), fullfit, test="Chisq")
 res <- anov$"Pr("[2]
                                           # for R >= 2.14.0
 if (is.null(res)) res <- anov$"P("[2] # earlier versions</pre>
  res
}
# perform the closed testing procedure
cl <- closed(mytest, hypotheses)</pre>
summary(cl)
defining(cl)
shortlist(cl)
hypotheses(cl)
# how many variables among a chosen set are associated with the response?
pick(cl, c("ht", "lwt", "smoke", "ui"))
```

Construct the DAG from a given collection of sets. *Constructing a DAG.*

Description

Constructs a DAG from a given collection of sets. Filters duplicates, and checks whether the eventual DAG structure has twoway logical relationships.

Usage

```
construct (sets)
```

Arguments

| sets | A list of sets/hypotheses for which you want to construct a DAG according to |
|------|--|
| | the underlying subset relations. |

Value

The function construct returns an object of class DAGstructure.

DAG class

Author(s)

Rosa Meijer: <r.j.meijer@lumc.nl>

See Also

DAGstructure

Examples

```
#Generate data, where the response Y is associated with two (out of 4) covariates
set.seed(1)
n=100
p=4
X <- matrix(rnorm(n*p),n,p)
beta <- c(0,0.5,0.5,0)
Y <- X %*% beta + rnorm(n)
# Let us assume we have the following sets that we want to test:
sets <- list(c(1,2,3,4), c(1,2), c(2,3,4), c(2,3), 1, 2, 3, 4)
names(sets) <- c(1234, 12, 234, 23, 1, 2, 3, 4)
# Start by making the corresponding graph structure
struct <- construct(sets)
# Check whether the DAG has toway logical relations:
istwoway(struct)
```

DAG class

Class "DAG" for storing the result of the DAG multiple testing method

Description

The class DAG is the output of a call to DAGmethod. It stores which hypotheses have been rejected and can be used to calculate confidence sets for the number of true and/or false hypotheses among a selected set of hypotheses.

Slots

These slots are not meant to be directly accessed by the user.

- sets: Object of class "list". Stores unique original sets that are to be tested.
- method: Object of class "character". Stores whether the any-parent, all-parents or structuredHolm method has been used.
- isadjusted: Object of class "logical". Stores whether adjusted p-values are calculated.
- allpvalues: Object of class "numeric". Stores (adjusted) p-values for all hypotheses. Has value NA if adjusted p-value is larger than alpha.

- implications: Object of class "logical". Stores whether hypotheses are implications at chosen alpha-level
- alpha: Object of class "numeric". The type I error level chosen.
- rejected: Object of class "logical". Stores for each hypothesis wether this hypothesis has been rejected
- leaf_based_sets: Object of class "list". Stores sets expressed in the indices of their corresponding leaf nodes (which are sets itself).
- twoway: Object of class "logical". Is TRUE if the final DAG structure has twoway logical relationships.

Methods

show (DAG): Prints how many hypotheses there are in total and how many of them were rejected. **summary** (DAG): Prints the test results (as show).

alpha (DAG): Retrieves the maximal alpha_value from the DAG object.

implications (DAG): Retrieves the implications from a given DAG object.

pvalue (DAG,indicator): Retrieves pvalues for all possible hypotheses (as specified by indicator) from the DAG object.

Author(s)

Rosa Meijer: <r.j.meijer@lumc.nl>

See Also

DAGmethod, DAGpick, structuredHolm.

```
#Generate data, where the response Y is associated with two (out of 4) covariates
set.seed(1)
n=100
p=4
X <- matrix(rnorm(n*p),n,p)
beta <- c(0,0.5,0.5,0)
Y <- X %*% beta + rnorm(n)
# Let us assume we have the following sets that we want to test:
sets <- list(c(1,2,3,4), c(1,2), c(2,3,4), c(2,3), 1, 2, 3, 4)
names(sets) <- c(1234, 12, 234, 23, 1, 2, 3, 4)
# Start by making the corresponding graph structure
struct <- construct(sets)
# Check whether the DAG has toway logical relations:
istwoway(struct)
# Define the local test to be used in the closed testing procedure.
```

```
# This test expects a set as input.
mytest <- function(set)</pre>
{
  X <- X[,set,drop=FALSE]</pre>
  lm.out <- lm(Y ~ X)
  x <- summary(lm.out)</pre>
  return(pf(x$fstatistic[1],x$fstatistic[2],x$fstatistic[3],lower.tail=FALSE))
}
# Perform the DAG procedure (default is all-parents method).
DAG <- DAGmethod(struct, mytest, isadjusted=TRUE)</pre>
summary(DAG)
# What are the smallest sets that are found to be significant? If the sets have names,
# as in our example, the implications function will return the names
# of the implying sets, together with their (adjusted) p-value.
# If no names are provided, indices will be used instead of the names.
implications(DAG)
# What is the adjusted p-value of the null-hypothesis corresponding to the fourth set,
# which is set c(2,3)?
# To look up the pvalue, the function uses the index or name of the set
# in the list of sets stored in the DAGstructure.
# (Note that, if there were duplicate sets in the original list, this index can be different from
# the one in the original list given to \code{construct})
pvalue(DAG,4)
pvalue(DAG, "23") #as above, but while using names
# How many of the elementary hypotheses (the last 4 sets) have to be false
# with probability 1-alpha?
# Sets (don't have to be elementary hypotheses in general) must be specified
# by their index or name.
DAGpick(DAG, 5:8)
DAGpick(DAG, c("1","2","3","4")) #as above, but while using names
```

DAG Testing

Testing of hypotheses, forming a DAG.

Description

Tests all hypotheses in a given DAG while controlling the FWER, using a user-specified local test.

Usage

Arguments

| DAGstructure | DAGstructure object, as returned by the function construct. |
|--------------|---|
| test | A function that performs the local test. The function should have a set as input and return a p-value. |
| alpha_max | The significance level of the test procedure. |
| method | Type of DAG procedure that is chosen. "all" gives the all-parents procedure, "any" the any-parent procedure. |
| isadjusted | If set to TRUE, adjusted p-values will be calculated. Otherwise, the p-values of all rejected hypotheses will equal alpha_max. |
| optimization | Can be, in ascending order of accuracy and computational costs: "none", "LP" (linear programming) or "ILP" (integer linear programming). |
| degree | Can be "group" or "individual". If "group" is chosen, optimization is done on a group level, otherwise on an individual level (more accurate, but more time-consuming). |
| pvalues | Optional (in case of stored p-values): a vector in which the raw p-values of the exact sets as found in the DAGstructure argument are stored (in the same order). If the test function is provided, this argument is not necessary. |
| verbose | If set to TRUE, while running the method, a counter will indicate how many hypotheses are already rejected. |

Details

The function DAGmethod tests all possible hypotheses within a given DAG structure, while controlling the familywise error rate.

Value

The function DAGmethod returns an object of class DAG.

Author(s)

Rosa Meijer: <r.j.meijer@lumc.nl>

References

Meijer and Goeman (2015) Biometrical Journal 57 (1) 123-143.

See Also

DAG, DAGstructure, construct, DAGpick.

Examples

#Generate data, where the response Y is associated with two (out of 4) covariates set.seed(1) $n\!=\!100$

DAGpick

```
p=4
X <- matrix(rnorm(n*p),n,p)</pre>
beta <- c(0,0.5,0.5,0)
Y <- X %*% beta + rnorm(n)
# Let us assume we have the following sets that we want to test:
sets <- list(c(1,2,3,4), c(1,2), c(2,3,4), c(2,3), 1, 2, 3, 4)
names(sets) <- c(1234, 12, 234, 23, 1, 2, 3, 4)
# Start by making the corresponding graph structure
struct <- construct(sets)</pre>
# Check whether the DAG has toway logical relations:
istwoway(struct)
# Define the local test to be used in the closed testing procedure.
# This test expects a set as input.
mytest <- function(set)</pre>
{
  X <- X[,set,drop=FALSE]</pre>
  lm.out <- lm(Y ~ X)
  x <- summary(lm.out)</pre>
  return(pf(x$fstatistic[1],x$fstatistic[2],x$fstatistic[3],lower.tail=FALSE))
}
# Perform the DAG procedure (default is all-parents method).
DAG <- DAGmethod(struct, mytest, isadjusted=TRUE)</pre>
summary(DAG)
# What are the smallest sets that are found to be significant?
implications(DAG)
# What is the adjusted p-value of the null-hypothesis corresponding to the fourth set,
# which is set c(2,3)?
# To look up the pvalue, the function uses the index or name of the set
# in the list of sets stored in the DAGstructure.
# (Note that, if there were duplicate sets in the original list, this index can be different from
# the one in the original list given to \code{construct})
pvalue(DAG,4)
pvalue(DAG, "23") #as above, but while using names
# How many of the elementary hypotheses (the last 4 sets) have to be false
# with probability 1-alpha?
# Sets (don't have to be elementary hypotheses in general) must be specified
# by their index or name.
DAGpick(DAG, 5:8)
DAGpick(DAG, c("1","2","3","4")) #as above, but while using names
```

DAGpick

Description

Calculates confidence limits for the number of false hypotheses on the basis of the DAG procedure within a family of sets.

Usage

DAGpick (DAG, indicators, optimization = "ILP")

Arguments

| DAG | DAG object, as returned by the function DAGmethod. |
|--------------|--|
| indicators | The names or indices of the sets (as specified in the DAGstructure object) for which you want to know the confidence limits. Note that, if there were duplicate sets in the original list, the index can be different from the one in the original list given to construct. |
| optimization | Can be, in ascending order of accuracy and computational costs: "LP" (linear programming) or "ILP" (integer linear programming). |

Value

The function DAGpick returns the lower bound of a 1-alpha confidence set for the number of false sets. For the moment, the function can only be used on DAG objects that correspond to a DAG with two-way logical relationships.

Author(s)

Rosa Meijer: <r.j.meijer@lumc.nl>

See Also

DAGmethod, DAG.

Examples

#Generate data, where the response Y is associated with two (out of 4) covariates
set.seed(1)
n=100
p=4
X <- matrix(rnorm(n*p),n,p)
beta <- c(0,0.5,0.5,0)
Y <- X %*% beta + rnorm(n)</pre>

Let us assume we have the following sets that we want to test:

DAGstructure class

```
sets <- list(c(1,2,3,4), c(1,2), c(2,3,4), c(2,3), 1, 2, 3, 4)
names(sets) <- c(1234, 12, 234, 23, 1, 2, 3, 4)
# Start by making the corresponding graph structure
struct <- construct(sets)</pre>
# Define the local test to be used in the closed testing procedure.
# This test expects a set as input.
mytest <- function(set)</pre>
 X <- X[,set,drop=FALSE]</pre>
 lm.out <- lm(Y ~ X)
 x <- summary(lm.out)</pre>
  return(pf(x$fstatistic[1],x$fstatistic[2],x$fstatistic[3],lower.tail=FALSE))
}
# Perform the DAG procedure (default is all-parents method).
DAG <- DAGmethod(struct, mytest, isadjusted=TRUE)</pre>
summary(DAG)
# How many of the elementary hypotheses (the last 4 sets) have to be false
# with probability 1-alpha?
# Sets (don't have to be elementary hypotheses in general) must be specified
# by their index or name.
DAGpick(DAG, 5:8)
DAGpick(DAG, c("1","2","3","4")) #as above, but while using names
```

| DAGstructure class | Class "DAGstructure" for storing the result of the construct method |
|--------------------|---|
| | that constructs the DAG. |

Description

The class DAGstructure is the output of a call to construct. It stores the DAG structure that is induced by the given sets.

Slots

These slots are not meant to be directly accessed by the user.

parents: Object of class "list". Stores the parents of each set, indicated by indices.

children: Object of class "list". Stores the children of each set, indicated by indices.

sets: Object of class "list". Stores the sets that are used for the DAG construction.

twoway: Object of class "logical". Is TRUE if the final DAG structure has twoway logical relationships.

Methods

istwoway (DAGstructure): Indicates whether given DAGstructure has twoway relationships.

Author(s)

Rosa Meijer: <r.j.meijer@lumc.nl>

See Also

DAGmethod

Examples

```
# Let us assume we have the following sets that we want to test:
sets <- list(c(1,2,3,4), c(1,2), c(2,3,4), c(2,3), 1, 2, 3, 4)
# The sets need to have names in order to be able to look up their p-values later
names(sets) <- c(1234, 12, 234, 23, 1, 2, 3, 4)
# Start by making the corresponding graph structure
struct <- construct(sets)
# Check whether the DAG has toway logical relations:
istwoway(struct)
```

hommelFast Calculates adjusted p-values of Hommel's method efficiently.

Description

Calculates adjusted p-values of Hommel's method efficiently.

Usage

hommelFast (pvalues, simes = TRUE)

Arguments

| pvalues | A vector of p-values. |
|---------|---|
| simes | If TRUE, a Simes' test is used, if FALSE Hommel's test is used. |

Value

Returns a hommel object.

Author(s)

Rosa Meijer: <r.j.meijer@lumc.nl>

NAEP

Examples

```
#Generate a vector of pvalues
set.seed(1)
n <- 1000
pvalues <- c(runif(0.50*n,0,0.001), runif(0.50*n,0,1))
#Create an hommel object in which the adjusted p-values are stored, based on a Simes'test
#(or Hommel's test, by choosing simes = FALSE):
hom <- hommelFast(pvalues, simes = TRUE)
#Retrieve the first 10 adjusted p-values by using the \code{p.adjust} method
# from the hommel package. Note that they are not sorted</pre>
```

```
hommel::p.adjust(hom)[1:10]
```

NAEP

National Assessment of Educational Progress (NAEP) p-values

Description

P-values for the null hypothesis of no change in the average eighth-grade mathematics achievement scores for the 34 states that participated in both the 1990 and the 1992 National Assessment of Educational Progress (NAEP) Trial State Assessment.

Usage

data(NAEP)

Format

A named numeric vector of p-values, uncorrected for multiple testing.

References

Benjamini Y. and Hochberg, Y. 2000. On the adaptive control of the false discovery rate in multiple testing with independent statistics. Journal of Educational and Behavioral Statistics 25 (1) 60-83.

Williams, V.S.L., Jones, L.V. and Tukey, J.W. 1999. Controlling error in multiple comparisons, with examples from state-to-state differences in educational achievement. Journal of Educational and Behavioral Statistics 24 (1) 42-69.

Description

Calculates confidence limits for the number of true hypotheses on the basis of the closed testing procedure.

Usage

pick (closure, reject, alpha, silent=FALSE, plot=FALSE)

Arguments

| closure | An object of class closure, typically created through a call to closed. |
|---------|---|
| reject | A character vector identifying the hypotheses to be rejected. Must be a subvector of hypotheses(closure). |
| alpha | For closure objects with adjusted p-values, specifies the value of alpha for which confidence limits are to be calculated (optional). |
| silent | If FALSE, prints the result to the screen. |
| plot | Whether a a confidence distribution should be plotted. Only available for closure objects with adjusted p-values. |

Details

The function pick calculates a confidence interval for the number of true hypotheses among a selected set of hypotheses.

Value

The function returns the upper confidence limit for the number of true hypotheses among the set reject. The lower confidence limit is always equal to 0. If closed was called with alpha=NA, a confidence distribution is plotted and returned.

Author(s)

Jelle Goeman: <j.j.goeman@lumc.nl>

Examples

Example: the birthwt data set from the MASS library # We want to find variables associated with low birth weight library(MASS) fullfit <- glm(low~age+lwt+race+smoke+ptl+ht+ui+ftv, family=binomial, data=birthwt) hypotheses <- c("age", "lwt", "race", "smoke", "ptl", "ht", "ui", "ftv")</pre>

Define the local test to be used in the closed testing procedure

Pick

Plot region objects Visualizing of the region hypotheses that could be rejected.

Description

Visualizes region objects as created through a call to regionmethod.

Usage

```
regionplot (region, alpha, color="red")
```

```
regionplot2 (region, alpha, color_rej="red", color_unrej="grey")
```

Arguments

| a labo East region objects with adjusted a values, specifies the value of alaba for w | hich |
|---|------|
| rejections should be plotted (optional). | |
| color Color that is used to indicate rejected region hypotheses. | |
| color_rej Color that is used to indicate rejected region hypotheses. | |
| color_unrej Color that is used to indicate unrejected region hypotheses. | |

Details

Both plot functions create a graph that visualizes all possible region hypotheses. Each region hypothesis is a node in the graph, and from each region hypothesis two edged connect the hypothesis with its child hypotheses. The regionplot2 function visualized the graph with its nodes and edges. This function is especially useful for region objects with a limited number of elementary hypotheses. The regionplot function does not display the nodes and edges separately, but draws a polygon that follows the original graph structure.

Author(s)

Rosa Meijer: <r.j.meijer@lumc.nl>

Examples

```
#generate data, where the response Y is associated with certain groups of covariates
#namely cov 3-6, 9-12, 15-18
set.seed(1)
n=100
p=20
X <- matrix(rnorm(n*p),n,p)</pre>
beta <- c(rep(0,2),rep(1,4),rep(0,2),rep(1,4),rep(0,2),rep(1,4),rep(0,2))</pre>
Y \leq X \% beta + rnorm(n)
# Define the local test to be used in the closed testing procedure
mytest <- function(left,right)</pre>
{
  X <- X[,(left:right),drop=FALSE]</pre>
  lm.out <- lm(Y ~ X)
  x <- summary(lm.out)</pre>
  return(pf(x$fstatistic[1],x$fstatistic[2],x$fstatistic[3],lower.tail=FALSE))
}
# perform the region procedure
reg <- regionmethod(rep(1,p), mytest, isadjusted=TRUE)</pre>
summary(reg)
#what are the smallest regions that are found to be significant?
implications(reg)
#how many covariates within the full region of length 20 are at least associated with the response?
regionpick(reg, list(c(1,p)), alpha=0.05)
#visualize the results by either plotting a polygon corresponding to the underlying graph
regionplot(reg)
#or by plotting the graph itself
regionplot2(reg)
```

Region class

Class "region" for storing the result of the region procedure

Description

The class region is the output of a call to regionmethod. It stores which region hypotheses have been rejected and can be used to calculate confidence sets for the number of true and/or false hypotheses among a selected region.

Region class

Slots

These slots are not meant to be directly accessed by the user.

weights: Object of class "numeric". Stores the weights of elementary hypotheses.

- isadjusted: Object of class "logical". Stores whether adjusted p-values are calculated.
- allpvalues: Object of class "matrix". Stores (adjusted) p-values for all possible region hypotheses. Has value NA if adjusted p-value is larger than alpha. Corresponds to a 0x0 matrix if all_pvalues is set to FALSE (by default).
- implications: Object of class "matrix". Stores implications includinge (adjusted) p-values at chosen alpha-level

alpha: Object of class "numeric". The type I error level chosen.

totalrejected: Object of class "numeric". Stores the total number of rejected region hypotheses.

Methods

show (region): Prints how many region hypotheses were tested and how many of them were rejected.

summary (region): Prints the test results (as show).

alpha (region): Retrieves the maximal alpha_value from the region object.

- **implications** (region,alpha): Retrieves the implications from a given region object. By default, the alpha-level is set to alpha_max, but the alpha level can be varied, if the supporting information is present in the region object.
- **pvalue** (region,left,right): Retrieves pvalues for all possible region hypotheses (indicated with left and right bound) from the region object. Only able to return the value if the allovalues matrix is stored in the region object.

Author(s)

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See Also

regionmethod, regionpick.

Examples

```
#generate data, where the response Y is associated with certain groups of covariates
#namely cov 3-6, 9-12, 15-18
set.seed(1)
n=100
p=20
X <- matrix(rnorm(n*p),n,p)
beta <- c(rep(0,2),rep(1,4),rep(0,2),rep(1,4),rep(0,2),rep(1,4),rep(0,2))
Y <- X %*% beta + rnorm(n)</pre>
```

Define the local test to be used in the closed testing procedure
mytest <- function(left,right)</pre>

```
{
 X <- X[,(left:right),drop=FALSE]</pre>
 lm.out <- lm(Y ~ X)
 x <- summary(lm.out)</pre>
 return(pf(x$fstatistic[1],x$fstatistic[2],x$fstatistic[3],lower.tail=FALSE))
}
# perform the region procedure
reg <- regionmethod(rep(1,p), mytest, isadjusted=TRUE, all_pvalues=TRUE)</pre>
summary(reg)
#what are the smallest regions that are found to be significant?
implications(reg)
#what are the smallest regions that are found to be significant at an alpha-level of 0.03?
implications(reg, alpha=0.03)
#what is the adjusted p-value of the overall null-hypothesis
#(corresponding to the region ranging from 1 to 20)?
pvalue(reg,1,20)
#how many covariates within the full region of length 20 are at least associated with the response?
regionpick(reg, list(c(1,p)), alpha=0.05)
#visualize the results by either plotting a polygon corresponding to the underlying graph
regionplot(reg)
#or by plotting the graph itself
regionplot2(reg)
```

Region Testing Testing of all possible region hypotheses

Description

Tests all possible region hypotheses in a given region while controlling the FWER, using a userspecified local test.

Usage

Arguments

weights a vector that indicates the weight each elementary hypotheses should receive in the multiple testing procedure. The length of the vector should equal the number of elementary hypotheses. All values should be strictly positive.

```
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```

Region Testing

| test | A function that performs the local test. The function should have the left and rightbound of the region as input (as two separate numbers), and return a p-value. |
|-------------|--|
| alpha_max | The significance level of the test procedure. |
| all_pvalues | If set to TRUE, the procedure will return a matrix with the p-values of all tested region hypotheses. If set to FALSE, only the p-values of the implications will be returned. |
| isadjusted | If set to TRUE, adjusted p-values will be calculated. Otherwise, the p-values of all rejected hypotheses will equal alpha_max. |
| verbose | If set to TRUE, while running the method, a counter will indicate how many region hypotheses are already rejected. |

Details

The function regionmethod tests all possible region hypotheses within one main interval, while controlling the familywise error rate.

Value

The function regionmethod returns an object of class region.

Note

The number of region hypotheses is quadratic in the number of elementary hypotheses. The number of elementary hypotheses should for computational reasons not be too large. For values in between 1000 and 10.000 the region procedure can still be used, but one might consider calculating the individual raw p-values beforehand.

If both isadjusted and all_pvalues are set to TRUE, afterwards implications can be obtained for all alpha-values smaller or equal to alpha_max.

Author(s)

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References

Meijer, Krebs and Goeman (2015) Statistical Applications in Genetics and Molecular Biology 14 (1) 1-19.

```
#generate data, where the response Y is associated with certain groups of covariates
#namely cov 3-6, 9-12, 15-18
set.seed(1)
n=100
p=20
X <- matrix(rnorm(n*p),n,p)
beta <- c(rep(0,2),rep(1,4),rep(0,2),rep(1,4),rep(0,2),rep(1,4),rep(0,2))</pre>
```

regionpick

```
Y <- X %*% beta + rnorm(n)
# Define the local test to be used in the closed testing procedure
mytest <- function(left,right)</pre>
{
  X <- X[,(left:right),drop=FALSE]</pre>
  lm.out <- lm(Y \sim X)
  x <- summary(lm.out)</pre>
  return(pf(x$fstatistic[1],x$fstatistic[2],x$fstatistic[3],lower.tail=FALSE))
}
# perform the region procedure
reg <- regionmethod(rep(1,p), mytest, isadjusted=TRUE)</pre>
summary(reg)
#what are the smallest regions that are found to be significant?
implications(reg)
#at least how many covariates within the full region of length 20
#are associated with the response?
regionpick(reg, list(c(1,p)), alpha=0.05)
#visualize the results by either plotting a polygon corresponding to the underlying graph
regionplot(reg)
#or by plotting the graph itself
```

#or by plotting the graph itse regionplot2(reg)

regionpick

Confidence limits for the number of false hypotheses in a given region.

Description

Calculates confidence limits for the number of false hypotheses on the basis of the region procedure within one or more regions.

Usage

```
regionpick (region, intervals, alpha, silent = FALSE, ignore_weights = TRUE)
```

Arguments

| region | An object of class region, typically created through a call to regionmethod. |
|-----------|--|
| intervals | A list containing one or more regions, specified by a left and rightbound. |
| alpha | For region objects with adjusted p-values, specifies the value of alpha for which confidence limits are to be calculated (optional). |
| silent | If FALSE, prints the result to the screen. |

```
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```

regionpick

ignore_weights If set to TRUE, a confidence interval for the number of false elementary hypotheses will be computed. If set to FALSE, a confidence interval for the combined weight of false elementary hypotheses will be computed.

Details

The function regionpick calculates a confidence interval for the number (or weight) of false hypotheses among a selected set of elementary hypotheses.

Value

The function returns the lower confidence limit for the number of false hypotheses (i.e. true findings) among the set of elementary hypotheses as specified by intervals. The upper confidence limit is always equal to the size of the set.

Author(s)

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```
#generate data, where the response Y is associated with certain groups of covariates
#namely cov 3-6, 9-12, 15-18
set.seed(1)
n=100
p=20
X <- matrix(rnorm(n*p),n,p)</pre>
beta <- c(rep(0,2),rep(1,4),rep(0,2),rep(1,4),rep(0,2),rep(1,4),rep(0,2))</pre>
Y <- X %*% beta + rnorm(n)</pre>
# Define the local test to be used in the closed testing procedure
mytest <- function(left,right)</pre>
{
  X <- X[,(left:right),drop=FALSE]</pre>
  lm.out <- lm(Y \sim X)
  x <- summary(lm.out)</pre>
  return(pf(x$fstatistic[1],x$fstatistic[2],x$fstatistic[3],lower.tail=FALSE))
}
# perform the region procedure
reg <- regionmethod(rep(1,p), mytest, isadjusted=TRUE)</pre>
summary(reg)
#what are the smallest regions that are found to be significant?
implications(reg)
#how many covariates within the full region of length 20 are at least associated with the response?
regionpick(reg, list(c(1,p)), alpha=0.05)
```

```
#how many covariates within the two subregions, (1,5) and (16,20)
#are at least associated with the response?
```

```
regionpick(reg, list(c(1,5),c(16,20)))
```

Select with shortcuts Confidence limits for the number of true hypotheses, with shortcuts.

Description

Calculates confidence limits for the number of true hypotheses on the basis of the closed testing procedure using specific local tests that allow shortcuts.

Usage

```
pickFisher (p, select = seq_along(p), alpha=0.05, silent=FALSE)
curveFisher (p, select = seq_along(p), order, alpha=0.05, plot = TRUE)
pickSimes (hommel, select, alpha=0.05, silent=FALSE)
curveSimes (hommel, select, order, alpha=0.05, plot = TRUE)
pickMeinshausen (p, PM, select = seq_along(p), alpha=0.05, silent=FALSE)
curveMeinshausen (p, PM, select = seq_along(p), order, alpha=0.05, plot = TRUE)
```

Arguments

| р | The vector of p-values for all tested hypotheses. |
|--------|--|
| hommel | The hommel object, obtained from the hommelFast function. |
| PM | A matrix of permutation p-values. Rows are hypotheses; columns are permutations. |
| select | The indexing vector of the p-values of the hypotheses to be selected. May be any type of appropriate indexing vector (integers, logical, or character). |
| order | The indexing vector specifying the order in which p-values of the hypotheses are to be rejected. May be integer or character. |
| alpha | The significance level of the test procedure. |
| silent | If FALSE, prints verbose result to the screen. |
| plot | If TRUE, plots the curve of correct rejections versus total rejections. |
| | |

Details

The results of the pickFisher, pickSimes and pickMeinshausen functions are identical to applying closed and pick, for specific choices of the local test, but are computationally more efficient. pickFisher uses local tests based on Fisher combinations. This local test is only valid if p-values of true hypotheses are independent. pickSimes uses a local test based on Simes' inequality. It is

Select with shortcuts

valid if p-values of true hypotheses are independent but also under some forms of positive correlations. The Hommel variant of the Simes local test is valid under any dependence structure of the p-values. pickMeinshausen is a permutation-based variant of pickSimes. See the reference below.

In the curve functions, the user may specify either select or order. Specifying order fixes the precise order in which hypotheses are selected, whereas specifying select only specifies which hypotheses are candidates for selection, leaving the order to be chosen by the function to maximize the number of correct rejections.

Value

For pickFisher, pickSimes and pickMeinshausen, the function returns the lower confidence limit for the number of false hypotheses (correct rejection) among the set reject. The upper confidence limit is always equal to the number of rejections made. curveFisher and curveSimes return the same confidence limit, but for selecting only the first 1,2,3,... hypotheses from the selected set.

Author(s)

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References

Goeman and Solari (2011) Statistical Science 26 (4) 584-597.

Meinshausen (2006) Scandinavian Journal of Statistics 33 (2), 227-237.

```
# Fisher's method
data(NAEP)
pickFisher(NAEP, c("NH", "NC", "IA"))
pickFisher(NAEP, 1:7)
curveFisher(NAEP)
curveFisher(NAEP, order=7:1)
# Simes method
hom <- hommelFast(NAEP)</pre>
pickSimes(hom, c("NH", "NC", "IA"))
pickSimes(hom, 1:7)
curveSimes(hom)
curveSimes(hom, select=1:7)
# Meinshausen's method
# This example uses data from the multtest package on bioconductor
if(require("multtest")) {
  data(golub)
  smallglb <- golub[1:500,]</pre>
 TM<-sapply(1:nrow(smallglb), function(i) {</pre>
    mt.sample.teststat(smallglb[i,], golub.cl,test="t.equalvar",B=500)
  })
  PM<-2*(1-pt(abs(TM),df=length(golub.cl)-2)) # permutation matrix</pre>
```

```
# p-values
p<-apply(smallglb,1, function(z) t.test(z[golub.cl==0],z[golub.cl==1],var.equal=TRUE)$p.value)
pickMeinshausen(p, PM, select=1:100)
pickMeinshausen(p, PM, select=sort.list(p)[1:100])
curveMeinshausen(p,PM, select=1:200)
curveMeinshausen(p,PM, order=1:200)
}
```

structured Holm *Testing of hypotheses, forming a DAG, by using a variant of Holm's method.*

Description

Tests all hypotheses in a given DAG while controlling the FWER, using a user-specified local test.

Usage

```
structuredHolm (DAGstructure, test, alpha_max = 0.05, isadjusted = FALSE,
optimization = "none", pvalues = NULL, verbose = FALSE)
```

Arguments

| DAGstructure | DAGstructure object, as returned by the function construct. |
|--------------|---|
| test | A function that performs the local test. The function should have a set as input and return a p-value. |
| alpha_max | The significance level of the test procedure. |
| isadjusted | If set to TRUE, adjusted p-values will be calculated. Otherwise, the p-values of all rejected hypotheses will equal alpha_max. |
| optimization | Can be, in ascending order of accuracy and computational costs: "none", "LP" (linear programming) or "ILP" (integer linear programming). |
| pvalues | Optional (in case of stored p-values): a vector in which the raw p-values of the exact sets as found in the DAGstructure argument are stored (in the same order). If the test function is provided, this argument is not necessary. |
| verbose | If set to TRUE, while running the method, a counter will indicate how many hypotheses are already rejected. |

Details

The function structuredHolm tests all possible hypotheses within a given DAG structure, while controlling the familywise error rate.

Value

The function structuredHolm returns an object of class DAG.

structured Holm

Author(s)

Rosa Meijer: <r.j.meijer@lumc.nl>

References

Meijer and Goeman (2015) Briefings in Bioinformatics, submitted.

See Also

DAG, DAGstructure, construct, DAGpick.

```
#Generate data, where the response Y is associated with two (out of 4) covariates
set.seed(1)
n=100
p=4
X <- matrix(rnorm(n*p),n,p)</pre>
beta <- c(0,0.5,0.5,0)
Y <- X \% + morm(n)
# Let us assume we have the following sets that we want to test:
sets <- list(c(1,2,3,4), c(1,2), c(2,3,4), c(2,3), 1, 2, 3, 4)
names(sets) <- c(1234, 12, 234, 23, 1, 2, 3, 4)
# Start by making the corresponding graph structure
struct <- construct(sets)</pre>
# Check whether the DAG has toway logical relations:
istwoway(struct)
# Define the local test to be used in the closed testing procedure.
# This test expects a set as input.
mytest <- function(set)</pre>
{
 X <- X[,set,drop=FALSE]</pre>
 lm.out <- lm(Y ~ X)
 x <- summary(lm.out)</pre>
  return(pf(x$fstatistic[1],x$fstatistic[2],x$fstatistic[3],lower.tail=FALSE))
}
# Perform the structuredHolm procedure.
DAG <- structuredHolm(struct, mytest, isadjusted=TRUE)</pre>
summary(DAG)
# What are the smallest sets that are found to be significant?
implications(DAG)
# What is the adjusted p-value of the null-hypothesis corresponding to the fourth set,
# which is set c(2,3)?
# To look up the pvalue, the function uses the index or name of the set
```

```
# in the list of sets stored in the DAGstructure.
# (Note that, if there were duplicate sets in the original list, this index can be different from
# the one in the original list given to \code{construct})
pvalue(DAG, 4)
pvalue(DAG, "23") #as above, but while using names
# How many of the elementary hypotheses (the last 4 sets) have to be false
# with probability 1-alpha?
# Sets (don't have to be elementary hypotheses in general) must be specified
# by their index or name.
DAGpick(DAG, 5:8)
DAGpick(DAG, c("1","2","3","4")) #as above, but while using names
```

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