# Package 'fence’ 

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## Type Package <br> Title Using Fence Methods for Model Selection <br> Version 1.0

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Description This method is a new class of model selection strategies, for mixed model selection, which includes linear and generalized linear mixed models. The idea involves a procedure to isolate a subgroup of what are known as correct models (of which the optimal model is a member). This is accomplished by constructing a statistical fence, or barrier, to carefully eliminate incorrect models. Once the fence is constructed, the optimal model is selected from among those within the fence according to a criterion which can be made flexible.
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## adaptivefence Adaptive Fence model selection

## Description

Adaptive Fence model selection

## Usage

adaptivefence(mf, f, ms, d, lf, pf, bs, grid = 101, bandwidth)

## Arguments

$\mathrm{mf} \quad$ function for fitting the model
$f \quad$ formula of full model
ms list of formula of candidates models
d data
lf measure lack of fit (to minimize)
pf model selection criteria, e.g., model dimension
bs bootstrap samples
grid grid for c
bandwidth bandwidth for kernel smooth function

## Value

models list all model candidates in the model space
B list the number of bootstrap samples that have been used
lack_of_fit_matrix
list a matrix of Qs for all model candidates (in columns). Each row is for each bootstrap sample
Qd_matrix list a matrix of QM - QM.tilde for all model candidates. Each row is for each bootrap sample
bandwidth list the value of bandwidth
model_mat list a matrix of selected models at each c values in grid (in columns). Each row is for each bootstrap sample
freq_mat list a matrix of coverage probabilities (frequency/smooth_frequency) of each selected models for a given c value (index)
c list the adaptive choice of c value from which the parsimonious model is selected
sel_model list the selected (parsimonious) model given the adaptive c value

## Author(s)

Jiming Jiang Jianyang Zhao J. Sunil Rao Thuan Nguyen

## References

- Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692
- Jiang J., Nguyen T., Rao J.S. (2009), A Simplified Adaptive Fence Procedure. Statistics and Probability Letters, 79, 625-629
- Thuan Nguyen, Jie Peng, Jiming Jiang (2014), Fence Methods for Backcross Experiments. Statistical Computation and Simulation, 84(3), 644-662


## Examples

```
## Not run:
require(fence)
#### Example 1 #####
data(iris)
full = Sepal.Length ~ Sepal.Width + Petal.Length + Petal.Width + (1|Species)
test_af = fence.lmer(full, iris)
plot(test_af)
test_af$sel_model
#### Example 2 #####
r =1234; set.seed(r)
p=8; n=150; rho = 0.6
id = rep(1:50,each=3)
R = diag(p)
for(i in 1:p){
    for(j in 1:p){
        R[i,j] = rho^(abs(i-j))
    }
}
R = 1*R
x=mvrnorm(n, rep(0, p), R) # all x's are time-varying dependence #
colnames(x)=paste('x',1:p, sep='')
tbetas = c(0,0.5,1,0,0.5,1,0,0.5) # non-zero beta 2,3,5,6,8
epsilon = rnorm(150)
y = x%*%tbetas + epsilon
colnames(y) = 'y'
data = data.frame(cbind(x,y,id))
full = y ~ x1 +x2+x3+x4+x5+x6+x7+x8+(1|id)
#X = paste('x',1:p, sep='', collapse='+')
#full = as.formula(paste('y~',X,'+(1|id)', sep="")) #same as previous one
fence_obj = fence.lmer(full,data) # it takes 3-5 min #
plot(fence_obj)
fence_obj$sel_model
## End(Not run)
```


## Description

Adaptive Fence model selection (Small Area Estmation)

## Usage

adaptivefence.fh(mf, f, ms, d, lf, pf, bs, grid = 101, bandwidth, method)

## Arguments

$m f \quad$ Call function, for example: default calls: function $(m, b)$ eblupFH(formula $=m$, vardir $=\mathrm{D}$, data $=\mathrm{b}$, method $=$ "FH")
f Full Model
ms find candidate model, findsubmodel.fh(full)
d Dimension number
lf Measures lack of fit using function(res) -res\$fit\$goodness[1]
pf Dimensions of model
bs Bootstrap
grid grid for c
bandwidth bandwidth for kernel smooth function
method Method to be used. Fay-Herriot method is the default.

## Details

In Jiang et. al (2008), the adaptive c value is chosen from the highest peak in the p* vs. c plot. In Jiang et. al (2009), $95 \%$ CI is taken into account while choosing such an adaptive choice of c. In Thuan Nguyen et. al (2014), the adaptive c value is chosen from the first peak. This approach works better in the moderate sample size or weak signal situations. Empirically, the first peak becomes highest peak when sample size increases or signals become stronger

## Value

models list all model candidates in the model space
B list the number of bootstrap samples that have been used
lack_of_fit_matrix
list a matrix of Qs for all model candidates (in columns). Each row is for each bootstrap sample
Qd_matrix list a matrix of QM - QM.tilde for all model candidates. Each row is for each bootrap sample
bandwidth list the value of bandwidth

| model_mat | list a matrix of selected models at each c values in grid (in columns). Each row <br> is for each bootstrap sample |
| :--- | :--- |
| freq_mat | list a matrix of coverage probabilities (frequency/smooth_frequency) of each <br> selected models for a given c value (index) |
| c | list the adaptive choice of c value from which the parsimonious model is selected |
| sel_model | list the selected (parsimonious) model given the adaptive c value |

## Note

- The current Fence package focuses on variable selection. However, Fence methods can be used to select other parameters of interest, e.g., tunning parameter, variance-covariance structure, etc.
- The number of bootstrap samples is suggested to be increased, e.g., $B=1000$ when the sample size is small, or signals are weak


## Author(s)

Jiming Jiang Jianyang Zhao J. Sunil Rao Thuan Nguyen

## References

- Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692
- Jiang J., Nguyen T., Rao J.S. (2009), A Simplified Adaptive Fence Procedure. Statistics and Probability Letters, 79, 625-629
- Thuan Nguyen, Jie Peng, Jiming Jiang (2014), Fence Methods for Backcross Experiments. Statistical Computation and Simulation, 84(3), 644-662


## Examples

```
## Not run:
require(fence)
### example 1 ####
data("kidney")
data = kidney[-which.max(kidney$x),] # Delete a suspicious data point #
data$x2 = data$x^2
data$x3 = data$x^3
data$x4 = data$x^4
data$D = data$sqrt.D.^2
plot(data$y ~ data$x)
full = y~x+x2+x3+x4
testfh = fence.sae(full, data, B=1000, fence="adaptive", method="F-H", D = D)
testfh$sel_model
testfh$c
## End(Not run)
```

fence.lmer Fence model selection (Linear Mixed Model)

## Description

Fence model selection (Linear Mixed Model)

## Usage

fence.lmer(full, data, $B=100$, grid = 101, fence $=c($ "adaptive", "nonadaptive"), cn = NA, REML = TRUE, bandwidth = NA, cpus = parallel::detectCores())

## Arguments

| full | formula of full model |
| :--- | :--- |
| data | data |
| B | number of bootstrap samples, parametric bootstrap is used |
| grid | grid for c |
| fence | a procedure of the fence method to be used. It's suggested to choose nonadaptive <br> procedure if c is known; otherwise nonadaptive must be chosen <br> cn value for nonadaptive |
| cn | Restricted Maximum Likelihood approach |
| REML | bandwidth for kernel smooth function |
| bandwidth |  |
| cpus | Number of parallel computers |

## Details

In Jiang et. al (2008), the adaptive c value is chosen from the highest peak in the p* vs. c plot. In Jiang et. al (2009), $95 \%$ CI is taken into account while choosing such an adaptive choice of c. In Thuan Nguyen et. al (2014), the adaptive c value is chosen from the first peak. This approach works better in the moderate sample size or weak signal situations. Empirically, the first peak becomes highest peak when sample size increases or signals become stronger

## Value

models list all model candidates in the model space
B
list the number of bootstrap samples that have been used
lack_of_fit_matrix
list a matrix of Qs for all model candidates (in columns). Each row is for each bootstrap sample
Qd_matrix list a matrix of QM - QM.tilde for all model candidates. Each row is for each bootrap sample
bandwidth list the value of bandwidth
model_mat list a matrix of selected models at each c values in grid (in columns). Each row is for each bootstrap sample
freq_mat list a matrix of coverage probabilities (frequency/smooth_frequency) of each selected models for a given c value (index)

C
list the adaptive choice of c value from which the parsimonious model is selected
sel_model list the selected (parsimonious) model given the adaptive c value
@ note The current Fence package focuses on variable selection. However, Fence methods can be used to select other parameters of interest, e.g., tunning parameter, variance-covariance structure, etc.

## Author(s)

Jiming Jiang Jianyang Zhao J. Sunil Rao Thuan Nguyen

## References

- Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692
- Jiang J., Nguyen T., Rao J.S. (2009), A Simplified Adaptive Fence Procedure. Statistics and Probability Letters, 79, 625-629
- Thuan Nguyen, Jie Peng, Jiming Jiang (2014), Fence Methods for Backcross Experiments. Statistical Computation and Simulation, 84(3), 644-662


## Examples

require(fence)
library (snow)
\#\#\#\# Example 1 \#\#\#\#\#
data(iris)
full $=$ Sepal.Length $\sim$ Sepal.Width + Petal.Length + Petal.Width + (1|Species)
\# Takes greater than 5 seconds to run
\# test_af = fence.lmer(full, iris)
\# test_af\$c
\# test_naf = fence.lmer(full, iris, fence = "nonadaptive", cn = 12)
\# plot(test_af)
\# test_af\$sel_model
\# test_naf\$sel_model
fence. NF Fence model selection (Nonparametric Model)

## Description

Fence model selection (Noparametric Model)

## Usage

fence. NF (full, data, spline, ps = 1:3, qs = NA, B = 100, grid = 101, bandwidth = NA, lambda)

## Arguments

| full | formula of full model |
| :--- | :--- |
| data | data |
| spline | variable needed for spline terms |
| ps | order of power |
| qs | number of knots |
| B | number of bootstrap sample, parametric for lmer |
| grid | grid for c |
| bandwidth | bandwidth for kernel smooth function |
| lambda | A grid of lambda values |

## Value

models list all model candidates with p polynomial degrees and q knots in the model space
Qd_matrix list a matrix of QM - QM.tilde for all model candidates. Each row is for each bootrap sample
bandwidth list the value of bandwidth
model_mat list a matrix of selected models at each c values in grid (in columns). Each row is for each bootstrap sample
freq_mat list a matrix of coverage probabilities (frequency/smooth_frequency) of each selected models for a given c value (index)
c list the adaptive choice of c value from which the parsimonious model is selected
lambda penalty (or smoothing) parameter estimate given selected p and q
sel_model list the selected (parsimonious) model given the adaptive c value
beta.est.u A list of coefficient estimates given a lambda value
f.x.hat A vector of fitted values obtained from a given lambda value and beta.est.u
@ note The current Fence method in Nonparametric model focuses on one spline variable. This method can be extended to a general case with more than one spline variables, and includes nonspline variables.

## Author(s)

Jiming Jiang Jianyang Zhao J. Sunil Rao Bao-Qui Tran Thuan Nguyen

## References

- Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692
- Jiang J., Nguyen T., Rao J.S. (2009), A Simplified Adaptive Fence Procedure. Statistics and Probability Letters, 79, 625-629
- Jiang J., Nguyen T., Rao J.S. (2010), Fence Method for Nonparametric Small Area Estimation. Survey Methodology, 36, 1, 3-11


## Examples

```
## Not run:
    require(fence)
    n = 100
    set.seed(1234)
    x=runif(n,0,3)
    y = 1-x+x^2- 2*(x-1)^2*(x>1) + 2*(x-2)^2*(x>2) + rnorm(n,sd=.2)
    lambda=exp((c(1:60)-30)/3)
    data=data.frame(cbind(x,y))
    test_NF = fence.NF(full=y~x, data=data, spline='x', ps=c(1:3), qs=c(2,5), B=1000, lambda=lambda)
    plot(test_NF)
    summary <- summary(test_NF)
    model_sel <- summary[[1]]
    model_sel
    lambda_sel <- summary[[2]]
    lambda_sel
    ## End(Not run)
```

fence.sae Fence model selection (Small Area Estmation)

## Description

Fence model selection (Small Area Estmation)

## Usage

fence.sae(full, data, $B=100$, grid $=101$, fence $=c(" a d a p t i v e "$,
"nonadaptive"), cn = NA, method = c("F-H", "NER"), D = NA, REML = FALSE, bandwidth = NA, cpus = parallel::detectCores())

## Arguments

| full | formular of full model |
| :--- | :--- |
| data | data |
| B | number of bootstrap sample, parametric for lmer |
| grid | grid for c |


| fence | fence method to be used, e.g., adaptive, or nonadaptive. It's suggested to choose <br> nonadaptive procedure if c is known; otherwise nonadaptive must be chosen |
| :--- | :--- |
| cn | cn for nonadaptive |
| method | Select method to use |
| D | vector containing the D sampling variances of direct estimators for each domain. |
| REML | The values must be sorted as the variables in formula. Only used in FH model |
| Restricted Maximum Likelihood approach |  |
| bandwidth | bandwidth for kernel smooth function |
| cpus | Number of parallel computers |

## Details

In Jiang et. al (2008), the adaptive c value is chosen from the highest peak in the $p^{*}$ vs. c plot. In Jiang et. al (2009), $95 \%$ CI is taken into account while choosing such an adaptive choice of c. In Thuan Nguyen et. al (2014), the adaptive c value is chosen from the first peak. This approach works better in the moderate sample size or weak signal situations. Empirically, the first peak becomes highest peak when sample size increases or signals become stronger

## Value

models list all model candidates in the model space
B
list the number of bootstrap samples that have been used
lack_of_fit_matrix
list a matrix of Qs for all model candidates (in columns). Each row is for each bootstrap sample
Qd_matrix list a matrix of QM - QM.tilde for all model candidates. Each row is for each bootrap sample
bandwidth list the value of bandwidth
model_mat list a matrix of selected models at each c values in grid (in columns). Each row is for each bootstrap sample
freq_mat list a matrix of coverage probabilities (frequency/smooth_frequency) of each selected models for a given c value (index)
c list the adaptive choice of c value from which the parsimonious model is selected
sel_model list the selected (parsimonious) model given the adaptive c value

Note

- The current Fence package focuses on variable selection. However, Fence methods can be used to select other parameters of interest, e.g., tunning parameter, variance-covariance structure, etc.
- The number of bootstrap samples is suggested to be increased, e.g., $B=1000$ when the sample size is small, or signals are weak


## Author(s)

Jiming Jiang Jianyang Zhao J. Sunil Rao Thuan Nguyen

## References

- Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692
- Jiang J., Nguyen T., Rao J.S. (2009), A Simplified Adaptive Fence Procedure. Statistics and Probability Letters, 79, 625-629
- Thuan Nguyen, Jie Peng, Jiming Jiang (2014), Fence Methods for Backcross Experiments. Statistical Computation and Simulation, 84(3), 644-662


## Examples

```
require(fence)
library(snow)
### example 1 ####
data("kidney")
data = kidney[-which.max(kidney$x),] # Delete a suspicious data point #
data$x2 = data$x^2
data$x3 = data$x^3
data$x4 = data$x^4
data$D = data$sqrt.D.^2
plot(data$y ~ data$x)
full = y~x+x2+x3+x4
# Takes more than 5 seconds to run
# testfh = fence.sae(full, data, B=100, fence="adaptive", method="F-H", D = D)
# testfh$sel_model
# testfh$c
```

IF.lm

## Description

Invisible Fence model selection (Linear Model)

## Usage

IF.lm(full, data, $B=100$, cpus $=2$, lftype $=c(" a b s c o e f ", ~ " p v a l u e "))$

## Arguments

| full | formula of full model |
| :--- | :--- |
| data | data |
| B | number of bootstrap sample, parametric for $\operatorname{lm}$ |
| cpus | number of parallel computers |
| lftype | subtractive measure type, e.g., absolute value of coefficients, p-value, $t$-value, <br> etc. |

## Details

This method (Jiang et. al, 2011) is motivated by computational expensive in complex and high dimensional problem. The idea of the method-there is the best model in each dimension (in model space). The boostrapping determines the coverage probability of the selected model in each dimensions. The parsimonious model is the selected model with the highest coverage probabily (except the one for the full model, always probability of 1.)

Value
full list the full model
B
list the number of bootstrap samples that have been used
freq list the coverage probabilities of the selected model for each dimension
size list the number of variables in the parsimonious model
term list variables included in the full model
model list the variables selected in-the-order in the parsimonious model
@ note The current Invisible Fence focuses on variable selection. The current routine is applicable to the case in which the subtractive measure is the absolute value of the coefficients, p -value, t value. However, the method can be extended to other subtractive measures. See Jiang et. al (2011) for more details.

## Author(s)

Jiming Jiang Jianyang Zhao J. Sunil Rao Thuan Nguyen

## References

- Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692
- Jiming Jiang, Thuan Nguyen and J. Sunil Rao (2011), Invisible fence methods and the identification of differentially expressed gene sets. Statistics and Its Interface, Volume 4, 403-415.


## Examples

```
library(fence)
library(MASS)
library(snow)
\(r=1234\); set.seed(r)
\(\mathrm{p}=10\); \(\mathrm{n}=300\); rho \(=0.6\)
R \(=\operatorname{diag}(p)\)
for (i in 1:p)\{
    for ( \(j\) in 1:p)\{
        R[i,j] = rho^(abs(i-j))
    \}
\}
\(R=1 * R\)
x=mvrnorm(n, rep(0, p), R)
colnames( \(x\) )=paste('x',1:p, sep='')
X = cbind(rep(1,n),x)
```

```
tbetas = c(1,1,1,0,1,1,0,1,0,0,0) # non-zero beta 1,2,4,5,7
epsilon = rnorm(n)
y = as.matrix(X)%*%tbetas + epsilon
colnames(y) = 'y'
data = data.frame(cbind(X,y))
full = y ~ x1+x2+x3+x4+x5+x6+x7+x8+x9+x10
# Takes greater than 5 seconds (~`17 seconds) to run
# obj1 = IF.lm(full = full, data = data, B = 100, lftype = "abscoef")
# sort((names(obj1$model$coef)[-1]))
# obj2 = IF.lm(full = full, data = data, B = 100, lftype = "pvalue")
# sort(setdiff(names(data[c(-1,-12)]), names(obj2$model$coef)))
```


## IF.lmer

Invisible Fence model selection (Linear Mixed Model)

## Description

Invisible Fence model selection (Linear Mixed Model)

## Usage

```
IF.lmer(full, data, \(B=100\), REML = TRUE, method = c("marginal",
    "conditional"), cpus = parallel::detectCores(), lftype = c("abscoef",
    "tvalue"))
```


## Arguments

full formula of full model
data data

B number of bootstrap sample, parametric for lmer

REML Restricted maximum likelihood estimation
method choose either marginal (e.g., GEE) or conditional model
cpus Number of parallel computers
lftype subtractive measure type, e.g., absolute value of coefficients, p-value, $t$-value, etc.

## Details

This method (Jiang et. al, 2011) is motivated by computational expensive in complex and high dimensional problem. The idea of the method-there is the best model in each dimension (in model space). The boostrapping determines the coverage probability of the selected model in each dimensions. The parsimonious model is the selected model with the highest coverage probabily (except the one for the full model, always probability of 1. )

## Value

full
B
freq
size
term list variables included in the full model
model list the variables selected in-the-order in the parsimonious model
@ note The current Invisible Fence focuses on variable selection. The current routine is applicable to the case in which the subtractive measure is the absolute value of the coefficients, p -value, t value. However, the method can be extended to other subtractive measures. See Jiang et. al (2011) for more details.

## Author(s)

Jiming Jiang Jianyang Zhao J. Sunil Rao Thuan Nguyen

## References

- Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692
- Jiming Jiang, Thuan Nguyen and J. Sunil Rao (2011), Invisible fence methods and the identification of differentially expressed gene sets. Statistics and Its Interface, Volume 4, 403-415.


## Examples

```
require(fence)
library(snow)
library(MASS)
data("X.1mer")
data = data.frame(X.lmer)
# non-zero beta I.col.2, I.col.3a, I.col.3b, V5, V7, V8, V9
beta = matrix(c(0, 1, 1, 1, 1, 0, 0.1, 0.05, 0.25, 0), ncol = 1)
set.seed(1234)
alpha = rep(rnorm(100), each = 3)
mu = alpha + as.matrix(data[,-1]) %*% beta
data$id = as.factor(data$id)
data$y = mu + rnorm(300)
raw = "y ~ (1|id)+I.col.2+I.col.3a+I.col.3b"
for (i in 5:10) {
    raw = paste0(raw, "+V", i)
}
full = as.formula(raw)
# The following output takes more than 5 seconds (~70 seconds) to run.
# obj1.lmer = IF.lmer(full = full, data = data, B = 100, method="conditional",lftype = "abscoef")
# sort(obj1.lmer$model)
# obj2.lmer = IF.lmer(full = full, data = data, B = 100, method="conditional",lftype = "tvalue")
```

```
# sort(obj2.lmer$model)
# Similarly, the following scenarios can be run
# obj2.lmer = IF.lmer(full = full, data = data, B = 100, method="conditional",lftype = "tvalue")
# sort(obj2.lmer$model)
# obj1.lm = IF.lmer(full = full, data = data, B = 100, method="marginal", lftype = "abscoef")
# sort(names(obj1.lm$model$coefficients[-1]))
# obj2.lm = IF.lmer(full = full, data = data, B = 100, method="marginal", lftype = "tvalue")
# sort(names(obj2.lm$model$coefficients[-1]))
```


## invisiblefence Invisible Fence model selection

## Description

Invisible Fence model selection

## Usage

invisiblefence(mf, f, d, lf, bs)

## Arguments

$m f \quad$ Call function, for example: default calls: function $(m, b)$ eblupFH(formula $=m$, vardir $=\mathrm{D}$, data $=\mathrm{b}$, method $=$ "FH")
f
Full model
d Dimension number
lf Measures lack of fit using function(res) -res\$fit\$goodness[1]
bs Bootstrap

## Details

This method (Jiang et. al, 2011) is motivated by computational expensive in complex and high dimensional problem. The idea of the method-there is the best model in each dimension (in model space). The boostrapping determines the coverage probability of the selected model in each dimensions. The parsimonious model is the selected model with the highest coverage probabily (except the one for the full model, always probability of 1.)

## Value

full list the full model
B
list the number of bootstrap samples that have been used
freq
size list the number of variables in the parsimonious model

| term | list variables included in the full model |
| :--- | :--- |
| model | list the variables selected in-the-order in the parsimonious model |

@ note The current Invisible Fence focuses on variable selection. The current routine is applicable to the case in which the subtractive measure is the absolute value of the coefficients, p -value, t value. However, the method can be extended to other subtractive measures. See Jiang et. al (2011) for more details.

## Author(s)

Jiming Jiang Jianyang Zhao J. Sunil Rao Thuan Nguyen

## References

- Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692
- Jiming Jiang, Thuan Nguyen and J. Sunil Rao (2011), Invisible fence methods and the identification of differentially expressed gene sets. Statistics and Its Interface, Volume 4, 403-415.


## Examples

```
## Not run:
data("X.1mer")
data = data.frame(X.lmer)
beta = matrix(c(0, 1, 1, 1, 1, 0, 0.1, 0.05, 0.25, 0), ncol = 1)
set.seed(1234)
alpha = rep(rnorm(100), each = 3)
mu = alpha + as.matrix(data[,-1]) %*% beta
data$id = as.factor(data$id)
data$y = mu + rnorm(300)
raw = "y ~ (1|id)+I.col.2+I.col.3a+I.col.3b"
for (i in 5:10) {
    raw = paste0(raw, "+V", i)
}
full = as.formula(raw)
obj1.lmer = IF.lmer(full = full, data = data, B = 100, method="conditional",lftype = "abscoef")
obj1.lmer$model$coefficients
obj2.lmer = IF.lmer(full = full, data = data, B = 100, method="conditional",lftype = "tvalue")
obj2.1mer$model$coefficients
obj1.lm = IF.lmer(full = full, data = data, B = 100, method="marginal", lftype = "abscoef")
obj1.lm$model$coefficients
obj2.lm = IF.lmer(full = full, data = data, B = 100, method="marginal", lftype = "tvalue")
obj2.1m$model$coefficients
## End(Not run)
```

kidney kidney

## Description

Data used for kidney example

## Usage

kidney

## Format

A data frame with 4 variables
nonadaptivefence Nonadaptive Fence model selection

## Description

Nonadaptive Fence model selection

## Usage

nonadaptivefence(mf, f, ms, d, lf, pf, cn)

## Arguments

| mf | function for fitting the model |
| :--- | :--- |
| f | formula of full model |
| ms | list of formula of candidates models |
| d | data |
| lf | measure lack of fit (to minimize) |
| pf | model selection criteria, e.g., model dimension |
| cn | given a specific c value |

## Value

models list all model candidates in the model space
lack_of_fit list a vector of Qs for all model candidates
formula list the model of the selected parsimonious model
sel_model list the selected (parsimonious) model given the adaptive c value

## Author(s)

Jiming Jiang Jianyang Zhao J. Sunil Rao Thuan Nguyen

## References

- Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692
- Jiang J., Nguyen T., Rao J.S. (2009), A Simplified Adaptive Fence Procedure. Statistics and Probability Letters, 79, 625-629
- Thuan Nguyen, Jie Peng, Jiming Jiang (2014), Fence Methods for Backcross Experiments. Statistical Computation and Simulation, 84(3), 644-662


## Examples

```
## Not run:
require(fence)
#### Example 1 #####
data(iris)
full = Sepal.Length ~ Sepal.Width + Petal.Length + Petal.Width + (1|Species)
test_naf = fence.lmer(full, iris, fence = "nonadaptive", cn = 12)
test_naf$sel_model
## End(Not run)
```

plot.AF

Plot Adaptive Fence model selection

## Description

Plot Adaptive Fence model selection

## Usage

```
    ## S3 method for class 'AF'
```

    plot(x = res, ...)
    
## Arguments

x
Object to be plotted
... Additional arguments. CNot currently used.
plot.NF Plot Nonparametric Fence model selection

## Description

Plot Nonparametric Fence model selection

## Usage

\#\# S3 method for class 'NF'
plot(x = res, ...)

## Arguments

x
Object to be plotted
Additional arguments. CNot currently used.

## Description

Adaptive Fence model selection (Restricted Fence)

## Usage

RF(full, data, groups, $B=100$, grid $=101$, bandwidth $=$ NA, plot = FALSE, method = c("marginal", "conditional"), id = "id", cpus = parallel::detectCores())

## Arguments

full formula of full model
data data
groups
B
grid grid for c
bandwidth bandwidth for kernel smooth function
plot Plot object
method either marginal (GEE) or conditional approach is selected
id Subject or cluster id variable
cpus Number of parallel computers

## Details

In Jiang et. al (2008), the adaptive c value is chosen from the highest peak in the p* vs. c plot. In Jiang et. al (2009), $95 \%$ CI is taken into account while choosing such an adaptive choice of c. In Thuan Nguyen et. al (2014), the adaptive c value is chosen from the first peak. This approach works better in the moderate sample size or weak signal situations. Empirically, the first peak becomes highest peak when sample size increases or signals become stronger

## Value

models list all model candidates in the model space
B
list the number of bootstrap samples that have been used
lack_of_fit_matrix
list a matrix of Qs for all model candidates (in columns). Each row is for each bootstrap sample
Qd_matrix list a matrix of QM - QM.tilde for all model candidates. Each row is for each bootrap sample
bandwidth list the value of bandwidth
model_mat list a matrix of selected models at each c values in grid (in columns). Each row is for each bootstrap sample
freq_mat list a matrix of coverage probabilities (frequency/smooth_frequency) of each selected models for a given c value (index)
c list the adaptive choice of c value from which the parsimonious model is selected sel_model list the selected (parsimonious) model given the adaptive c value

## Note

bandwidth $=(\operatorname{cs}[2]-\operatorname{cs}[1]) * 3$. So it's chosen as 3 times grid between two c values.

## References

- Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692
- Jiang J., Nguyen T., Rao J.S. (2009), A Simplified Adaptive Fence Procedure. Statistics and Probability Letters, 79, 625-629
- Thuan Nguyen, Jiming Jiang (2012), Restricted fence method for covariate selection in longitudinal data analysis. Biostatistics, 13(2), 303-314
- Thuan Nguyen, Jie Peng, Jiming Jiang (2014), Fence Methods for Backcross Experiments. Statistical Computation and Simulation, 84(3), 644-662


## Examples

## \#\# Not run:

$r=1234$; set. $\operatorname{seed}(r)$
$n=100 ; p=15 ;$ rho $=0.6$
beta $=c(1,1,1,0,1,1,0,1,0,0,1,0,0,0,0) \quad \#$ non-zero beta $1,2,3, \mathrm{~V} 6, \mathrm{~V} 7, \mathrm{~V} 9, \mathrm{~V} 12$
id $=\operatorname{rep}(1: n$, each=3)

```
V.1 = rep(1,n*3)
I. }1=\operatorname{rep}(c(1,-1),each=150
I.2a = rep(c(0,1, -1),n)
I.2b}=\operatorname{rep}(c(0,-1,1),n
x = matrix(rnorm(n*3*11), nrow=n*3, ncol=11)
x = cbind(id,V.1,I.1,I.2a,I.2b,x)
R = diag(3)
for(i in 1:3){
    for(j in 1:3){
        R[i,j] = rho^(abs(i-j))
    }
}
e=as.vector(t(mvrnorm(n, rep(0, 3), R)))
y = as.vector(x[,-1]%*%beta) + e
data = data.frame(x,y)
raw = "y ~ V.1 + I.1 + I.2a +I.2b"
for (i in 6:16) { raw = paste0(raw, "+V", i)}; full = as.formula(raw)
bin1="y ~ V.1 + I.1 + I.2a +I.2b"
for (i in 6:8) { bin1 = paste0(bin1, "+V", i)}; bin1 = as.formula(bin1)
bin2="y ~ v9"
for (i in 10:16){ bin2 = paste0(bin2, "+V", i)}; bin2 = as.formula(bin2)
# May take longer than 30 min since there are two stages in this RF procedure
obj1.RF = RF(full = full, data = data, groups = list(bin1,bin2), method="conditional")
obj1.RF$sel_model
obj2.RF = RF(full = full, data = data, groups = list(bin1,bin2), B=100, method="marginal")
obj2.RF$sel_model
## End(Not run)
```

summary.AF
Summary Adaptive Fence model selection

## Description

Summary Adaptive Fence model selection

## Usage

\#\# S3 method for class 'AF'
summary (object $=$ res, ...)

## Arguments

object
Object to be summarized
... addition arguments. Not currently used

| summary.NF $\quad$ Summary Nonparametric Fence model selection |
| :--- | :--- |

## Description

Summary Nonparametric Fence model selection

## Usage

\#\# S3 method for class 'NF'
summary (object = res, ...)

## Arguments

| object | Object to be summarized |
| :--- | :--- |
| $\ldots$ | addition arguments. Not currently used |


| X.lmer $\quad X . l m e r ~$ |
| :--- | :--- |

## Description

Data used in the example for X.lmer

## Usage

data(X.lmer)

## Format

A data frame with 10 variables:

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