

# Package ‘geostan’

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**Title** Bayesian Spatial Analysis

**Version** 0.3.0

**URL** <https://connordonegan.github.io/geostan/>,

<https://github.com/ConnorDonegan/geostan/>

**Description** For Bayesian inference with spatial data, provides exploratory spatial analysis tools, multiple spatial model specifications, spatial model diagnostics, and special methods for inference with small area survey data (e.g., the America Community Survey (ACS)) and censored population health surveillance data. Models are pre-specified using the Stan programming language, a platform for Bayesian inference using Markov chain Monte Carlo (MCMC). References: Carpenter et al. (2017) <[doi:10.18637/jss.v076.i01](https://doi.org/10.18637/jss.v076.i01)>; Donegan (2021) <[doi:10.31219/osf.io/3ey65](https://doi.org/10.31219/osf.io/3ey65)>; Donegan, Chun and Hughes (2020) <[doi:10.1016/j.spasta.2020.100450](https://doi.org/10.1016/j.spasta.2020.100450)>; Donegan, Chun and Griffith (2021) <[doi:10.3390/ijerph18136856](https://doi.org/10.3390/ijerph18136856)>; Morris et al. (2019) <[doi:10.1016/j.sste.2019.100301](https://doi.org/10.1016/j.sste.2019.100301)>.

**License** GPL (>= 3)

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**Author** Connor Donegan [aut, cre] (<<https://orcid.org/0000-0002-9698-5443>>),  
Mitzi Morris [ctb]

**Maintainer** Connor Donegan <connor.donegan@gmail.com>

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## R topics documented:

geostan-package . . . . .	3
aple . . . . .	3
auto_gaussian . . . . .	4
edges . . . . .	5
expected_mc . . . . .	6
georgia . . . . .	7
get_shp . . . . .	8
gr . . . . .	9
lg . . . . .	11
lisa . . . . .	12
make_EV . . . . .	14
mc . . . . .	15
me_diag . . . . .	16
moran_plot . . . . .	18
n_eff . . . . .	20
posterior_predict . . . . .	21
prep_car_data . . . . .	22
prep_icar_data . . . . .	24
prep_me_data . . . . .	25
print.geostan_fit . . . . .	27
priors . . . . .	31
row_standardize . . . . .	34
sentencing . . . . .	35
se_log . . . . .	36
shape2mat . . . . .	37
sim_sar . . . . .	38
sp_diag . . . . .	39
stan_car . . . . .	42
stan_esf . . . . .	48
stan_glm . . . . .	55
stan_icar . . . . .	61
waic . . . . .	69

**Index**

**70**

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geostan-package

*The geostan R package.*

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## Description

Bayesian spatial modeling powered by Stan. **geostan** provides access to a variety of hierarchical spatial models using the R formula interface, supporting a complete spatial analysis workflow with a suite of spatial analysis tools. It is designed primarily for public health research but is generally applicable to modeling areal data. Unique features of the package include its spatial measurement error modeling strategy (for inference with small area estimates such as those from the American Community Survey), its fast proper CAR models, and its eigenvector spatial filtering methodology.

## References

- Carpenter, B., Gelman, A., Hoffman, M.D., Lee, D., Goodrich, B., Betancourt, M., Brubaker, M., Guo, J., Li, P., Riddell, A., 2017. Stan: A probabilistic programming language. *Journal of statistical software* 76. doi:10.18637/jss.v076.i01.
- Donegan, C., Y. Chun and A. E. Hughes (2020). Bayesian estimation of spatial filters with Moran's Eigenvectors and hierarchical shrinkage priors. *Spatial Statistics*. doi:10.1016/j.spasta.2020.100450 (open access: doi:10.31219/osf.io/fah3z).
- Donegan, Connor and Chun, Yongwan and Griffith, Daniel A. (2021). Modeling community health with areal data: Bayesian inference with survey standard errors and spatial structure. *Int. J. Env. Res. and Public Health* 18 (13): 6856. doi:10.3390/ijerph18136856. Supplementary material: <https://github.com/ConnorDonegan/survey-HBM>.
- Donegan, Connor (2021). Building spatial conditional autoregressive models in the Stan programming language. *OSF Preprints*. doi:10.31219/osf.io/3ey65.
- Gabry, J., Goodrich, B. and Lysy, M. (2020). rstantools: Tools for developers of R packages interfacing with Stan. R package version 2.1.1 <https://mc-stan.org/rstantools/>.
- Morris, M., Wheeler-Martin, K., Simpson, D., Mooney, S. J., Gelman, A., & DiMaggio, C. (2019). Bayesian hierarchical spatial models: Implementing the Besag York Mollié model in stan. *Spatial and spatio-temporal epidemiology*, 31, 100301. doi:10.1016/j.sste.2019.100301.
- Stan Development Team (2019). RStan: the R interface to Stan. R package version 2.19.2. <https://mc-stan.org>

---

aple

*Spatial autocorrelation estimator*

---

## Description

The approximate-profile likelihood estimator for the spatial autocorrelation parameter from a simultaneous autoregressive (SAR) model (Li et al. 2007). Note, the APLE approximation is not reliable when the number of observations is large.

**Usage**

```
aple(x, w, digits = 3)
```

**Arguments**

**x** Numeric vector of values, length  $n$ . This will be standardized internally with `scale(x)`.

**w** An  $n \times n$  row-standardized spatial connectivity matrix. See [shape2mat](#).

**digits** Number of digits to round results to.

**Details**

The APLE is an estimate of the spatial autocorrelation parameter one would obtain from fitting an intercept-only SAR model.

**Value**

the APLE estimate, a numeric value.

**Source**

Li, Honfei and Calder, Catherine A. and Cressie, Noel (2007). Beyond Moran's I: testing for spatial dependence based on the spatial autoregressive model. *Geographical Analysis*: 39(4): 357-375.

**See Also**

[mc](#), [moran\\_plot](#), [lisa](#), [sim\\_sar](#)

**Examples**

```
library(sf)
data(georgia)
w <- shape2mat(georgia, "W")
x <- georgia$ICE
aple(x, w)
```

---

auto\_gaussian

*Auto-Gaussian family for CAR models*

---

**Description**

create a family object for the auto-Gaussian CAR specification

**Usage**

```
auto_gaussian()
```

**Value**

An object of class family

**See Also**

[stan\\_car](#)

**Examples**

```
cp = prep_car_data(shape2mat(georgia))
fit <- stan_car(log(rate.male) ~ 1,
               data = georgia,
               car_parts = cp,
               family = auto_gaussian(),
               chains = 2, iter = 800) # for speed only

print(fit)
```

---

edges

*Edge list*

---

**Description**

Creates a list of connected nodes following the graph representation of a spatial connectivity matrix.

**Usage**

```
edges(C, unique_pairs_only = TRUE)
```

**Arguments**

**C** A connectivity matrix where connection between two nodes is indicated by non-zero entries.

**unique\_pairs\_only** By default, only unique pairs of nodes (i, j) will be included in the output.

**Details**

This is used internally for [stan\\_icar](#) and it is also helpful for creating the scaling factor for BYM2 models fit with [stan\\_icar](#).

**Value**

Returns a data.frame with three columns. The first two columns (node1 and node2) contain the indices of connected pairs of nodes; only unique pairs of nodes are included (unless `unique_pairs_only = FALSE`). The third column (weight) contains the corresponding matrix element, `C[node1, node2]`.

**See Also**

[shape2mat](#), [prep\\_icar\\_data](#), [stan\\_icar](#)

**Examples**

```
data(sentencing)
C <- shape2mat(sentencing)
nbs <- edges(C)
head(nbs)

## similar to:
head(Matrix::summary(C))
head(Matrix::summary(shape2mat(georgia, "W")))
```

---

expected\_mc

*Expected value of the residual Moran coefficient*

---

**Description**

Expected value for the Moran coefficient of model residuals under the null hypothesis of no spatial autocorrelation.

**Usage**

```
expected_mc(X, C)
```

**Arguments**

X                    model matrix, including column of ones.  
C                    Connectivity matrix.

**Value**

Returns a numeric value.

**Source**

Chun, Yongwan and Griffith, Daniel A. (2013). Spatial statistics and geostatistics. Sage, p. 18.

**Examples**

```
data(georgia)
C <- shape2mat(georgia)
X <- model.matrix(~ ICE + college, georgia)
expected_mc(X, C)
```

---

 georgia

*Georgia all-cause, sex-specific mortality, ages 55-64, years 2014-2018*


---

### Description

A simple features (sf) object for Georgia counties with sex- and age-specific deaths and populations at risk (2014-2018), plus select estimates (with standard errors) of county characteristics. Standard errors of the ICE were calculated using the Census Bureau's variance replicate tables.

### Usage

```
georgia
```

### Format

A simple features object with county geometries and the following columns:

**GEOID** Six digit combined state and county FIPS code

**NAME** County name

**ALAND** Land area

**AWATER** Water area

**population** Census Bureau 2018 county population estimate

**white** Percent White, ACS 2018 five-year estimate

**black** Percent Black, ACS 2018 five-year estimate

**hisp** Percent Hispanic/Latino, ACS 2018 five-year estimate

**ai** Percent American Indian, ACS 2018 five-year estimate

**deaths.male** Male deaths, 55-64 yo, 2014-2018

**pop.at.risk.male** Population estimate, males, 55-64 yo, years 2014-2018 (total), ACS 2018 five-year estimate

**pop.at.risk.male.se** Standard error of the pop.at.risk.male estimate

**deaths.female** Female deaths, 55-64 yo, 2014-2018

**pop.at.risk.female** Population estimate, females, 55-64 yo, years 2014-2018 (total), ACS 2018 five-year estimate

**pop.at.risk.female.se** Standard error of the pop.at.risk.female estimate

**ICE** Index of Concentration at the Extremes

**ICE.se** Standard error of the ICE estimate, calculated using variance replicate tables

**income** Median household income, ACS 2018 five-year estimate

**income.se** Standard error of the income estimate

**college** Percent of the population age 25 or higher than has a bachelors degree of higher, ACS 2018 five-year estimate

**college.se** Standard error of the college estimate

**insurance** Percent of the population with health insurance coverage, ACS 2018 five-year estimate

**insurance.se** Standard error of the insurance estimate

**rate.male** Raw (crude) age-specific male mortality rate, 2014-2018

**rate.female** Raw (crude) age-specific female mortality rate, 2014-2018

**geometry** simple features geometry for county boundaries

## Source

Centers for Disease Control and Prevention, National Center for Health Statistics. Underlying Cause of Death 1999-2018 on CDC Wonder Online Database. 2020. Available online: <http://wonder.cdc.gov> (accessed on 19 October 2020).

Donegan, Connor and Chun, Yongwan and Griffith, Daniel A. (2021). “Modeling community health with areal data: Bayesian inference with survey standard errors and spatial structure.” *Int. J. Env. Res. and Public Health* 18 (13): 6856. DOI: 10.3390/ijerph18136856 Data and code: <https://github.com/ConnorDonegan/survey-HBM>.

Kyle Walker and Matt Herman (2020). tidyensus: Load US Census Boundary and Attribute Data as 'tidyverse' and 'sf'-Ready Data Frames. R package version 0.11. <https://CRAN.R-project.org/package=tidyensus>

US Census Bureau. Variance Replicate Tables, 2018. Available online: <https://www.census.gov/programs-surveys/acs/data/variance-tables.2018.html> (accessed on 19 October 2020).

## Examples

```
data(georgia)
head(georgia)

library(sf)
plot(georgia[, 'rate.female'])
```

---

get\_shp

*Download shapefiles*

---

## Description

Given a url to a shapefile in a compressed .zip file, download the file and unzip it into a folder in your working directory.

## Usage

```
get_shp(url, folder = "shape")
```

## Arguments

**url** url to download a shapefile.  
**folder** what to name the new folder in your working directory containing the shapefile



**Value**

A folder in your working directory with the shapefile; filepaths are printed to the console.

**Examples**

```
## Not run:
library(sf)
url <- "https://www2.census.gov/geo/tiger/GENZ2019/shp/cb_2019_us_state_20m.zip"
folder <- tempdir()
print(folder)
get_shp(url, folder)
states <- sf::st_read(folder)
head(states)

## End(Not run)
```

---

gr

*The Geary Ratio*

---

**Description**

An index for spatial autocorrelation. Complete spatial randomness (lack of spatial pattern) is indicated by a Geary Ratio (GR) of 1; positive autocorrelation moves the index towards zero, while negative autocorrelation will push the index towards 2.

**Usage**

```
gr(x, w, digits = 3, na.rm = FALSE, warn = TRUE)
```

**Arguments**

x	Numeric vector of length n. By default, this will be standardized using the scale function.
w	An n x n spatial connectivity matrix. See <a href="#">shape2mat</a> .
digits	Number of digits to round results to.
na.rm	If na.rm = TRUE, observations with NA values will be dropped from both x and w.
warn	If FALSE, no warning will be printed to inform you when observations with NA values have been dropped, or if any observations without neighbors have been found.

## Details

The Geary Ratio is an index of spatial autocorrelation. The numerator contains a series of sums of squared deviations, which will be smaller when each observation is similar to its neighbors. This term makes the index sensitive to local outliers, which is advantageous for detecting such outliers and for measuring negative autocorrelation. The denominator contains the total sum of squared deviations from the mean value. Hence, under strong positive autocorrelation, the GR approaches zero. Zero spatial autocorrelation is represented by a GR of 1. Negative autocorrelation pushes the GR above 1, towards 2.

$$GR = \frac{n-1}{2K} \frac{M}{D}$$

$$M = \sum_i \sum_j w_{i,j} (x_i - x_j)^2$$

$$D = \sum_i (x_i - \bar{x})^2$$

Observations with no neighbors are removed before calculating the GR. The alternative is for those observations to contribute zero to the numerator—but zero is not a neutral value, it represents strong positive autocorrelation.

## Source

Chun, Yongwan, and Daniel A. Griffith. *Spatial Statistics and Geostatistics: Theory and Applications for Geographic Information Science and Technology*. Sage, 2013.

Qing, Luo and Griffith, Daniel A. and Wu, Huayi. "The Moran Coefficient and Geary Ratio: Some mathematical and numerical comparisons." *Proceedings of the 13th International Conference on Geocomputation*. Richardson, TX (USA), May 20-23, 2015. <http://www.geocomputation.org/2015/>

Geary, R. C. "The contiguity ratio and statistical mapping." *The Incorporated Statistician* 5, no. 3 (1954): 115-127\_129-146.

Unwin, Antony. "Geary's Contiguity Ratio." *The Economic and Social Review* 27, no. 2 (1996): 145-159.

## Examples

```
data(georgia)
x <- log(georgia$income)
w <- shape2mat(georgia, "W")
gr(x, w)
```

---

lg *Local Geary*

---

### Description

A local indicator of spatial association based on the Geary Ratio (Geary's C) for exploratory spatial data analysis. Large values of this statistic highlight local outliers, that is, values that are not like their neighbors.

### Usage

```
lg(x, w, digits = 3, scale = TRUE, na.rm = FALSE, warn = TRUE)
```

### Arguments

x	Numeric vector of length n. By default, this will be standardized using the scale function.
w	An n x n spatial connectivity matrix. See <a href="#">shape2mat</a> .
digits	Number of digits to round results to.
scale	If TRUE, then x will automatically be standardized using <code>scale(x, center = TRUE, scale = TRUE)</code> .
na.rm	If <code>na.rm = TRUE</code> , observations with NA values will be dropped from both x and w.
warn	If FALSE, no warning will be printed to inform you when observations with NA values have been dropped, or if any observations without neighbors have been found.

### Details

Local Geary's C is found in the numerator of the Geary Ratio (GR). For the  $i^{th}$  observation, the local Geary statistic is

$$C_i = \sum_j w_{i,j} * (x_i - x_j)^2$$

Hence, local Geary values will be largest for those observations that are most unlike their neighboring values. If a binary connectivity matrix is used (rather than row-standardized), then having many neighbors will also increase the value of the local Geary statistic. For most purposes, the row-standardized spatial weights matrix may be the more appropriate choice.

### Value

The function returns a vector of numeric values, each value being a local indicator of spatial association (or dissimilarity), ordered as x.

**Source**

Anselin, Luc. "Local indicators of spatial association—LISA." *Geographical analysis* 27, no. 2 (1995): 93-115.

Chun, Yongwan, and Daniel A. Griffith. *Spatial Statistics and Geostatistics: Theory and Applications for Geographic Information Science and Technology*. Sage, 2013.

**Examples**

```
library(ggplot2)
data(georgia)
x <- log(georgia$income)
w <- shape2mat(georgia, "W")
lisd <- lg(x, w)
hist(lisd)
ggplot(georgia) +
  geom_sf(aes(fill = lisd)) +
  scale_fill_gradient(high = "navy",
                     low = "white")
## or try: scale_fill_viridis()
```

---

 lisa

*Local Moran's I*


---

**Description**

A local indicator of spatial association (LISA) based on Moran's I (the Moran coefficient) for exploratory data analysis.

**Usage**

```
lisa(x, w, type = TRUE, scale = TRUE, digits = 3)
```

**Arguments**

x	Numeric vector of length n.
w	An n × n spatial connectivity matrix. See <a href="#">shape2mat</a> . If w is not row standardized ( <code>all(Matrix::rowSums(w) == 1)</code> ), it will automatically be row-standardized.
type	Return the type of association also (High-High, Low-Low, High-Low, and Low-High)? Defaults to FALSE.
scale	If TRUE, then x will automatically be standardized using <code>scale(x, center = TRUE, scale = TRUE)</code> . If FALSE, then the variate will be centered but not scaled, using <code>scale(x, center = TRUE, scale = FALSE)</code> .
digits	Number of digits to round results to.

## Details

The values of  $x$  will automatically be centered first with  $z = \text{scale}(x, \text{center} = \text{TRUE}, \text{scale} = \text{scale})$  (with user control over the `scale` argument). The LISA values are the product of each  $z$  value with the weighted sum of their respective surrounding value:

$$I_i = z_i \sum_j w_{ij} z_j$$

(or in R code: `lisa = z * (w %*% z)`). These are for exploratory analysis and model diagnostics.

An above-average value (i.e. positive  $z$ -value) with positive mean spatial lag indicates local positive spatial autocorrelation and is designated type "High-High"; a low value surrounded by high values indicates negative spatial autocorrelation and is designated type "Low-High", and so on.

This function uses Equation 7 from Anselin (1995). Note that the `spdep` package uses Formula 12, which divides the same value by a constant term  $\sum_i z_i^2/n$ . So the `geostan` version can be made equal to the `spdep` version by dividing by that value.

## Value

If `type = FALSE` a numeric vector of lisa values for exploratory analysis of local spatial autocorrelation. If `type = TRUE`, a `data.frame` with columns `Li` (the lisa value) and `type`.

## Source

Anselin, Luc. "Local indicators of spatial association—LISA." *Geographical Analysis* 27, no. 2 (1995): 93-115.

## See Also

[moran\\_plot](#), [mc](#), [aple](#), [lg](#), [gr](#)

## Examples

```
library(ggplot2)
library(sf)
data(georgia)
w <- shape2mat(georgia, "W")
x <- georgia$ICE
li = lisa(x, w)
head(li)
ggplot(georgia, aes(fill = li$Li)) +
  geom_sf() +
  scale_fill_gradient2()
```

---

`make_EV`*Extract eigenfunctions of a connectivity matrix for spatial filtering*

---

**Description**

Extract eigenfunctions of a connectivity matrix for spatial filtering

**Usage**

```
make_EV(C, nsa = FALSE, threshold = 0.2, values = FALSE)
```

**Arguments**

<code>C</code>	A binary spatial weights matrix. See <a href="#">shape2mat</a> .
<code>nsa</code>	Logical. Default of <code>nsa = FALSE</code> excludes eigenvectors capturing negative spatial autocorrelation. Setting <code>nsa = TRUE</code> will result in a candidate set of EVs that contains eigenvectors representing positive and negative SA.
<code>threshold</code>	Defaults to <code>threshold=0.2</code> to exclude eigenvectors representing spatial autocorrelation levels that are less than <code>threshold</code> times the maximum possible Moran coefficient achievable for the given spatial connectivity matrix. If <code>threshold = 0</code> , all eigenvectors will be returned (however, the eigenvector of constants (with eigenvalue of zero) will be dropped automatically).
<code>values</code>	Should eigenvalues be returned also? Defaults to <code>FALSE</code> .

**Details**

Returns a set of eigenvectors related to the Moran coefficient (MC), limited to those eigenvectors with  $|MC| > \text{threshold}$  if `nsa = TRUE` or  $MC > \text{threshold}$  if `nsa = FALSE`, optionally with corresponding eigenvalues.

**Value**

A `data.frame` of eigenvectors for spatial filtering. If `values=TRUE` then a named list is returned with elements `eigenvectors` and `eigenvalues`.

**Source**

Daniel Griffith and Yongwan Chun. 2014. "Spatial Autocorrelation and Spatial Filtering." in M. M. Fischer and P. Nijkamp (eds.), *Handbook of Regional Science*. Springer.

**See Also**

[stan\\_esf](#), [mc](#)

**Examples**

```
library(ggplot2)
data(georgia)
C <- shape2mat(georgia, style = "B")
EV <- make_EV(C)
head(EV)

ggplot(georgia) +
  geom_sf(aes(fill = EV[,1])) +
  scale_fill_gradient2()
```

mc

*The Moran coefficient***Description**

The Moran coefficient, a measure of spatial autocorrelation (also known as Global Moran's I)

**Usage**

```
mc(x, w, digits = 3, warn = TRUE, na.rm = FALSE)
```

**Arguments**

x	Numeric vector of input values, length n.
w	An n x n spatial connectivity matrix. See <a href="#">shape2mat</a> .
digits	Number of digits to round results to.
warn	If FALSE, no warning will be printed to inform you when observations with zero neighbors or NA values have been dropped.
na.rm	If na.rm = TRUE, observations with NA values will be dropped from both x and w.

**Details**

The formula for the Moran coefficient (MC) is

$$MC = \frac{n}{K} \frac{\sum_i \sum_j w_{ij} (y_i - \bar{y})(y_j - \bar{y})}{\sum_i (y_i - \bar{y})^2}$$

where  $n$  is the number of observations and  $K$  is the sum of all values in the spatial connectivity matrix  $W$ , i.e., the sum of all row-sums:  $K = \sum_i \sum_j w_{ij}$ .

If any observations with no neighbors are found (i.e. `any(Matrix::rowSums(w) == 0)`) they will be dropped automatically and a message will print stating how many were dropped. The alternative is for those observations to have a spatial lage of zero—but zero is not a neutral value, see the Moran scatter plot.

**Value**

The Moran coefficient, a numeric value.

**Source**

Chun, Yongwan, and Daniel A. Griffith. Spatial Statistics and Geostatistics: Theory and Applications for Geographic Information Science and Technology. Sage, 2013.

Cliff, Andrew David, and J. Keith Ord. Spatial processes: models & applications. Taylor & Francis, 1981.

**See Also**

[moran\\_plot](#), [lisa](#), [aple](#), [gr](#), [lg](#)

**Examples**

```
library(sf)
data(georgia)
w <- shape2mat(georgia, style = "W")
x <- georgia$ICE
mc(x, w)
```

---

me\_diag

*Data model diagnostics*

---

**Description**

Visual diagnostics for spatial measurement error models.

**Usage**

```
me_diag(
  fit,
  varname,
  shape,
  probs = c(0.025, 0.975),
  plot = TRUE,
  mc_style = c("scatter", "hist"),
  size = 0.25,
  index = 0,
  style = c("W", "B"),
  w = shape2mat(shape, match.arg(style)),
  binwidth = function(x) 0.5 * sd(x)
)
```



**Arguments**

fit	A <code>geostan_fit</code> model object as returned from a call to one of the <code>geostan::stan_*</code> functions.
varname	Name of the modeled variable (a character string, as it appears in the model formula).
shape	An object of class <code>sf</code> or another spatial object coercible to <code>sf</code> with <code>sf::st_as_sf</code> .
probs	Lower and upper quantiles of the credible interval to plot.
plot	If <code>FALSE</code> , return a list of <code>ggplots</code> and a <code>data.frame</code> with the raw data values alongside a posterior summary of the modeled variable.
mc_style	Character string indicating how to plot the Moran coefficient for the delta values: if <code>mc = "scatter"</code> , then <code>moran_plot</code> will be used with the marginal residuals; if <code>mc = "hist"</code> , then a histogram of Moran coefficient values will be returned, where each plotted value represents the degree of residual autocorrelation in a draw from the joint posterior distribution of delta values.
size	Size of points and lines, passed to <code>geom_pointrange</code> .
index	Integer value; use this if you wish to identify observations with the largest <code>n=index</code> absolute Delta values; data on the top <code>n=index</code> observations ordered by absolute Delta value will be printed to the console and the plots will be labeled with the indices of the identified observations.
style	Style of connectivity matrix; if <code>w</code> is not provided, <code>style</code> is passed to <code>shape2mat</code> and defaults to "W" for row-standardized.
w	An optional spatial connectivity matrix; if not provided, one will be created using <code>shape2mat</code> .
binwidth	A function with a single argument that will be passed to the <code>binwidth</code> argument in <code>geom_histogram</code> . The default is to set the width of bins to $0.5 * sd(x)$ .

**Value**

A grid of spatial diagnostic plots for measurement error models comparing the raw observations to the posterior distribution of the true values. Includes a point-interval plot of raw values and modeled values; a Moran scatter plot for  $\delta = z - x$  where  $z$  are the survey estimates and  $x$  are the modeled values; and a map of the delta values (take at their posterior means).

**Source**

Donegan, Connor and Chun, Yongwan and Griffith, Daniel A. (2021). "Modeling community health with areal data: Bayesian inference with survey standard errors and spatial structure." *Int. J. Env. Res. and Public Health* 18 (13): 6856. DOI: 10.3390/ijerph18136856 Data and code: <https://github.com/ConnorDonegan/survey-HBM>.

**See Also**

[sp\\_diag](#), [moran\\_plot](#), [mc](#), [aple](#)

## Examples

```

library(sf)
data(georgia)
## binary adjacency matrix
A <- shape2mat(georgia, "B")
## prepare data for the CAR model, using WCAR specification
cars <- prep_car_data(A, style = "WCAR")
## provide list of data for the measurement error model
ME <- prep_me_data(se = data.frame(ICE = georgia$ICE.se),
                  car_parts = cars)
## sample from the prior probability model only, including the ME model
fit <- stan_glm(log(rate.male) ~ ICE,
               ME = ME,
               data = georgia,
               prior_only = TRUE,
               iter = 800, # for speed only
               chains = 2, # for speed only
               refresh = 0 # silence some printing
               )

## see ME diagnostics
me_diag(fit, "ICE", georgia)
## see index values for the largest (absolute) delta values
## (differences between raw estimate and the posterior mean)
me_diag(fit, "ICE", georgia, index = 3)

```

---

moran\_plot

*Moran plot*

---

## Description

Plots a set of values against their spatially lagged values and gives the Moran coefficient as a measure of spatial autocorrelation.

## Usage

```

moran_plot(
  x,
  w,
  xlab = "x (centered)",
  ylab = "Spatial Lag",
  pch = 20,
  col = "darkred",
  size = 2,
  alpha = 1,
  lwd = 0.5,
  na.rm = FALSE
)

```

**Arguments**

x	A numeric vector of length n.
w	An n x n spatial connectivity matrix.
xlab	Label for the x-axis.
ylab	Label for the y-axis.
pch	Symbol type.
col	Symbol color.
size	Symbol size.
alpha	Symbol transparency.
lwd	Width of the regression line.
na.rm	If na.rm = TRUE, any observations of x with NA values will be dropped from x and from w.

**Details**

For details on the symbol parameters see the documentation for [geom\\_point](#).

If any observations with no neighbors are found (i.e. `any(Matrix::rowSums(w) == 0)`) they will be dropped automatically and a message will print stating how many were dropped.

**Value**

Returns a gg plot, a scatter plot with x on the horizontal and its spatially lagged values on the vertical axis (i.e. a Moran scatter plot).

**Source**

Anselin, Luc. "Local indicators of spatial association—LISA." *Geographical analysis* 27, no. 2 (1995): 93-115.

**See Also**

[mc](#), [lisa](#), [aple](#)

**Examples**

```
data(georgia)
x <- georgia$income
w <- shape2mat(georgia, "W")
moran_plot(x, w)
```

---

n_eff	<i>Effective sample size</i>
-------	------------------------------

---

**Description**

An approximate calculation for the effective sample size for spatially autocorrelated data. Only valid for approximately normally distributed data.

**Usage**

```
n_eff(n, rho)
```

**Arguments**

n	Number of observations.
rho	Spatial autocorrelation parameter from a simultaneous autoregressive model.

**Details**

Implements Equation 3 from Griffith (2005).

**Value**

Returns effective sample size  $n^*$ , a numeric value.

**Source**

Griffith, Daniel A. (2005). Effective geographic sample size in the presence of spatial autocorrelation. *Annals of the Association of American Geographers*. Vol. 95(4): 740-760.

**See Also**

[sim\\_sar](#), [aple](#)

**Examples**

```
n_eff(100, 0)
n_eff(100, 0.5)
n_eff(100, 0.9)
n_eff(100, 1)

rho <- seq(0, 1, by = 0.01)
plot(rho, n_eff(100, rho),
     type = 'l',
     ylab = "Effective Sample Size")
```

---

posterior\_predict      *Draw samples from the posterior predictive distribution*

---

### Description

Draw samples from the posterior predictive distribution of a fitted geostan model.

### Usage

```
posterior_predict(object, S, summary = FALSE, width = 0.95, car_parts, seed)
```

### Arguments

object	A geostan_fit object.
S	Optional; number of samples to take from the posterior distribution. The default, and maximum, is the total number of samples stored in the model.
summary	Should the predictive distribution be summarized by its means and central quantile intervals? If summary = FALSE, an S x N matrix of samples will be returned. If summary = TRUE, then a data.frame with the means and 100*width credible intervals is returned.
width	Only used if summary = TRUE, to set the quantiles for the credible intervals. Defaults to width = 0.95.
car_parts	Data for CAR model specification; only required for <a href="#">stan_car</a> with family = auto_gaussian().
seed	A single integer value to be used in a call to <a href="#">set.seed</a> before taking samples from the posterior distribution.

### Value

A matrix of size S x N containing samples from the posterior predictive distribution, where S is the number of samples drawn and N is the number of observations. If summary = TRUE, a data.frame with N rows and 3 columns is returned (with column names mu, lwr, and upr).

### Examples

```
fit <- stan_glm(sents ~ offset(log(expected_sents)),
               re = ~ name,
               data = sentencing,
               family = poisson(),
               chains = 2, iter = 600) # for speed only

yrep <- posterior_predict(fit, S = 65)
plot(density(yrep[1,]))
for (i in 2:nrow(yrep)) lines(density(yrep[i,]), col = 'gray30')
lines(density(sentencing$sents), col = 'darkred', lwd = 2)
```

---

```
prep_car_data
```

---

*Prepare data for a Stan CAR model*

---

## Description

Prepare data for a Stan CAR model

## Usage

```
prep_car_data(
  A,
  style = c("WCAR", "ACAR", "DCAR"),
  k = 1,
  gamma = 0,
  lambda = TRUE,
  cmat = TRUE,
  stan_fn = ifelse(style == "WCAR", "wcar_normal_lpdf", "car_normal_lpdf")
)
```

## Arguments

A	Binary adjacency matrix; for style = DCAR, provide a symmetric matrix of distances instead. The distance matrix should be sparse, meaning that most distances should be zero (usually obtained by setting some threshold distance beyond which all are zero).
style	Specification for the connectivity matrix (C) and conditional variances (M); one of "WCAR", "ACAR", or "DCAR".
k	For style = DCAR, distances will be raised to the -k power ( $d^{-k}$ ).
gamma	For style = DCAR, distances will be offset by gamma before raising to the -kth power.
lambda	If TRUE, return eigenvalues required for calculating the log determinant of the precision matrix and for determining the range of permissible values of rho. These will also be printed with a message if lambda = TRUE.
cmat	If cmat = TRUE, return the full matrix C (in sparse matrix format).
stan_fn	Two computational methods are available for CAR models using <a href="#">stan_car</a> : <code>car\_normal\_lpdf</code> and <code>wcar\_normal\_lpdf</code> . For WCAR models, either method will work but <code>wcar\_normal\_lpdf</code> is faster. To force use <code>car\_normal\_lpdf</code> when style = 'WCAR', provide <code>stan_fn = "car_normal_lpdf"</code> .

## Details

The CAR model is:

$$\text{Normal}(\mu, \Sigma), \Sigma = (I - \rho * C)^{-1} * M * \tau^2,$$

where  $I$  is the identity matrix,  $\rho$  is a spatial autocorrelation parameter,  $C$  is a connectivity matrix, and  $M * \tau^2$  is a diagonal matrix with conditional variances on the diagonal.  $\tau^2$  is a (scalar) scale parameter.

In the WCAR specification,  $C$  is the row-standardized version of  $A$ . This means that the non-zero elements of  $A$  will be converted to  $1/N_i$  where  $N_i$  is the number of neighbors for the  $i$ th site (obtained using `Matrix::rowSums(A)`). The conditional variances (on the diagonal of  $M * \tau^2$ ), are also proportional to  $1/N_i$ .

The ACAR specification is from Cressie, Perrin and Thomas-Agnon (2005); also see Cressie and Wikle (2011, p. 188) and Donegan (2021).

The DCAR specification is inverse distance-based, and requires the user provide a (sparse) distance matrix instead of a binary adjacency matrix. (For  $A$ , provide a symmetric matrix of distances, not inverse distances!) Internally, non-zero elements of  $A$  will be converted to:  $d_{\{ij\}} = (a_{\{ij\}} + \gamma)^{-k}$  (Cliff and Ord 1981, p. 144; Donegan 2021). Default values are  $k=1$  and  $\gamma=0$ . Following Cressie (2015), these values will be scaled (divided) by their maximum value. For further details, see the DCAR\_A specification in Donegan (2021).

For inverse-distance weighting schemes, see Cliff and Ord (1981); for distance-based CAR specifications, see Cressie (2015 [1993]), Haining and Li (2020), and Donegan (2021).

When using `stan_car`, always use `cmat = TRUE` (the default).

Details on CAR model specifications can be found in Table 1 of Donegan (2021).

## Value

A list containing all of the data elements required by the CAR model in `stan_car`.

## Source

Cliff A, Ord J (1981). *Spatial Processes: Models and Applications*. Pion.

Cressie N (2015 [1993]). *Statistics for Spatial Data*. Revised edition. John Wiley & Sons.

Cressie N, Perrin O, Thomas-Agnan C (2005). "Likelihood-based estimation for Gaussian MRFs." *Statistical Methodology*, 2(1), 1–16.

Cressie N, Wikle CK (2011). *Statistics for Spatio-Temporal Data*. John Wiley & Sons.

Donegan, Connor (2021). Spatial conditional autoregressive models in Stan. *OSF Preprints*. [doi:10.31219/osf.io/3ey65](https://doi.org/10.31219/osf.io/3ey65).

Haining RP, Li G (2020). *Modelling Spatial and Spatio-Temporal Data: A Bayesian Approach*. CRC Press.

## Examples

```
data(georgia)

## use a binary adjacency matrix
A <- shape2mat(georgia, style = "B")

## WCAR specification
cp <- prep_car_data(A, "WCAR")
1 / range(cp$lambda)
```

```
## ACAR specification
cp <- prep_car_data(A, "ACAR")

## DCAR specification (inverse-distance based)
A <- shape2mat(georgia, "B")
D <- sf::st_distance(sf::st_centroid(georgia))
A <- D * A
cp <- prep_car_data(A, "DCAR", k = 1)
```

---

```
prep_icar_data      Prepare data for ICAR models
```

---

## Description

Given a symmetric  $n \times n$  connectivity matrix, prepare data for intrinsic conditional autoregressive models in Stan. This function may be used for building custom ICAR models in Stan. This is used internally by [stan\\_icar](#).

## Usage

```
prep_icar_data(C, scale_factor = NULL)
```

## Arguments

<code>C</code>	Connectivity matrix
<code>scale_factor</code>	Optional vector of scale factors for each connected portion of the graph structure. If not provided by the user it will be fixed to a vector of ones.

## Details

This is used internally to prepare data for [stan\\_icar](#) models. It can also be helpful for fitting custom ICAR models outside of `geostan`.

## Value

list of data to add to Stan data list:

**k** number of groups

**group\_size** number of nodes per group

**n\_edges** number of connections between nodes (unique pairs only)

**node1** first node

**node2** second node. (`node1[i]` and `node2[i]` form a connected pair)

**weight** The element `C[node1, node2]`.

**group\_idx** indices for each observation belonging each group, ordered by group.

**m** number of disconnected regions requiring their own intercept.



**A** n-by-m matrix of dummy variables for the component-specific intercepts.

**inv\_sqrt\_scale\_factor** By default, this will be a k-length vector of ones. Placeholder for user-specified information. If user provided `scale_factor`, then this will be  $1/\sqrt{\text{scale\_factor}}$ .

**comp\_id** n-length vector indicating the group membership of each observation.

### Source

Besag, Julian, Jeremy York, and Annie Mollié. 1991. “Bayesian Image Restoration, with Two Applications in Spatial Statistics.” *Annals of the Institute of Statistical Mathematics* 43 (1): 1–20.

Donegan, Connor. Flexible Functions for ICAR, BYM, and BYM2 Models in Stan. Code Repository. 2021. Available online: <https://github.com/ConnorDonegan/Stan-ICAR/> (accessed Sept. 10, 2021).

Freni-Sterrantino, Anna, Massimo Ventrucci, and Håvard Rue. 2018. “A Note on Intrinsic Conditional Autoregressive Models for Disconnected Graphs.” *Spatial and Spatio-Temporal Epidemiology* 26: 25–34.

Morris, Mitzi, Katherine Wheeler-Martin, Dan Simpson, Stephen J Mooney, Andrew Gelman, and Charles DiMaggio. 2019. “Bayesian Hierarchical Spatial Models: Implementing the Besag York Mollié Model in Stan.” *Spatial and Spatio-Temporal Epidemiology* 31: 100301.

Riebler, Andrea, Sigrunn H Sørbye, Daniel Simpson, and Håvard Rue. 2016. “An Intuitive Bayesian Spatial Model for Disease Mapping That Accounts for Scaling.” *Statistical Methods in Medical Research* 25 (4): 1145–65.

### See Also

[edges](#), [shape2mat](#), [stan\\_icar](#), [prep\\_car\\_data](#)

### Examples

```
data(sentencing)
C <- shape2mat(sentencing)
icar.data.list <- prep_icar_data(C)
```

---

```
prep_me_data
```

*Prepare data for spatial measurement error models*

---

### Description

Prepares the list of data required for `geostan`'s (spatial) measurement error models. Given a data frame of standard errors and any optional arguments, the function returns a list with all required data for the models, filling in missing elements with default values.

**Usage**

```

prep_me_data(
  se,
  bounds = c(-Inf, Inf),
  car_parts,
  prior,
  logit = rep(FALSE, times = ncol(se))
)

```

**Arguments**

- |           |   |
|-----------|---|
| se        | Data frame of standard errors; column names must match (exactly) the variable names used in the model formula.  |
| bounds    | An optional numeric vector of length two providing the upper and lower bounds, respectively, of the variables. If not provided, they will be set to <code>c(-Inf, Inf)</code> (i.e., unbounded). Common usages include keeping percentages between zero and one hundred or proportions between zero and one.  |
| car_parts | A list of data required for spatial CAR models, as created by <a href="#">prep_car_data</a> ; optional. If omitted, the measurement error model will be a non-spatial Student's t model.  |
| prior     | <p>A named list of prior distributions (see <a href="#">priors</a>). If none are provided, default priors will be assigned. The list of priors may include the following parameters:</p> <p><b>df</b> If using a non-spatial ME model, the degrees of freedom (df) for the Student's t model is assigned a gamma prior with default parameters of <code>gamma(alpha = 3, beta = 0.2)</code>. Provide values for each covariate in <code>se</code>, listing the values in the same order as the columns of <code>se</code>.</p> <p><b>location</b> The prior for the location parameter (<math>\mu</math>) is a normal (Gaussian) distribution (the default being <code>normal(location = 0, scale = 100)</code>). To adjust the prior distributions, provide values for each covariate in <code>se</code>, listing the values in the same order as the columns of <code>se</code>.</p> <p><b>scale</b> The prior for the scale parameters is Student's t, and the default parameters are <code>student_t(df = 10, location = 0, scale = 40)</code>. To adjust, provide values for each covariate in <code>se</code>, listing the values in the same order as the columns of <code>se</code>.</p> <p><b>car_rho</b> The CAR model, if used, has a spatial autocorrelation parameter, <math>\rho</math>, which is assigned a uniform prior distribution. You must specify values that are within the permissible range of values for <math>\rho</math>; these are automatically printed to the console by the <a href="#">prep_car_data</a> function.</p> |
| logit     | Optional vector of logical values (TRUE, FALSE) indicating if the variable should be logit-transformed before being modeled. When TRUE, the sampling error will be modeled on the untransformed scale as usual; however, the spatial CAR prior model (or non-spatial Student's t prior model) will be assigned to the logit-transformed variate. Transformation can be crucial for modeling proportions with frequency distributions that are highly skewed.  |

**Value**

A list of data as required for (spatial) ME models. Missing arguments will be filled in with default values, including prior distributions.

**Examples**

```
data(georgia)

## for a non-spatial prior model for two covariates
se <- data.frame(ICE = georgia$ICE.se,
                 college = georgia$college.se)
ME <- prep_me_data(se)

## see default priors
print(ME$prior)

## set prior for the scale parameters
ME <- prep_me_data(se,
                  prior = list(scale = student_t(df = c(10, 10),
                                                  location = c(0, 0),
                                                  scale = c(20, 20))))

## for a spatial prior model (often recommended)
A <- shape2mat(georgia, "B")
cars <- prep_car_data(A)
ME <- prep_me_data(se,
                  car_parts = cars)
```

---

print.geostan\_fit      *geostan\_fit methods*

---

**Description**

Methods for fitted geostan models: extract residuals, fitted values, posterior predictive distribution or spatial component from a spatial regression model; extract samples from the posterior distribution; print regression results; plot posterior distributions.

**Usage**

```
## S3 method for class 'geostan_fit'
print(
  x,
  probs = c(0.025, 0.25, 0.5, 0.75, 0.975),
  digits = 3,
  pars = NULL,
  ...
)
```

```

## S3 method for class 'geostan_fit'
plot(x, pars, plotfun = "hist", fill = "steelblue4", ...)

## S3 method for class 'geostan_fit'
as.matrix(x, ...)

## S3 method for class 'geostan_fit'
as.data.frame(x, ...)

## S3 method for class 'geostan_fit'
as.array(x, ...)

## S3 method for class 'geostan_fit'
residuals(object, summary = TRUE, rates = TRUE, detrend = TRUE, ...)

## S3 method for class 'geostan_fit'
fitted(object, summary = TRUE, rates = TRUE, ...)

spatial(object, summary = TRUE, ...)

## S3 method for class 'geostan_fit'
spatial(object, summary = TRUE, ...)

## S3 method for class 'geostan_fit'
predict(
  object,
  newdata,
  alpha = mean(as.matrix(object, pars = "intercept")),
  center = object$x_center,
  summary = TRUE,
  type = c("link", "response"),
  ...
)

```

### Arguments

<code>x</code>	A fitted model object of class <code>geostan_fit</code> .
<code>probs</code>	Argument passed to <code>quantile</code> ; which quantiles to calculate and print.
<code>digits</code>	number of digits to print
<code>pars</code>	parameters to include; a character string (or vector) of parameter names.
<code>...</code>	additional arguments.
<code>plotfun</code>	Argument passed to <code>rstan::plot</code> . Options include histograms ("hist"), MCMC traceplots ("trace"), and density plots ("dens"). Diagnostic plots are also available such as Rhat statistics ("rhat"), effective sample size ("ess"), and MCMC autocorrelation ("ac").
<code>fill</code>	fill color for histograms and density plots.
<code>object</code>	A fitted model object of class <code>geostan_fit</code> .

summary	Logical; should the values be summarized with the mean, standard deviation and quantiles (probs = c(.025, .2, .5, .8, .975)) for each observation? Otherwise a matrix containing samples from the posterior distribution at each observation is returned.
rates	For Poisson and Binomial models, should the fitted values be returned as rates, as opposed to raw counts? Defaults to TRUE.
detrend	For CAR models with Gaussian likelihood only (auto-gaussian); if detrend = TRUE, the implicit spatial trend will be removed from the residuals. The implicit spatial trend is $Trend = \rho * C \%*\% (Y - \mu)$ (see <a href="#">stan_car</a> ). I.e., $resid = Y - (\mu + Trend)$ .
newdata	A data frame in which to look for variables with which to predict, presumably for the purpose of viewing marginal effects. Note that if the model formula includes an offset term, newdata must contain a column with the appropriate name for the offset, even though the values will be ignored (you may set all values to 1); you must use the alpha argument to include any additional terms. Note also that any spatially-lagged covariate terms will be ignored if they were provided using the slx argument. If covariates in the model were centered using the centerx argument, the predict.geostan_fit method will automatically center the predictors in newdata internally using the values stored in fit\$x_center. If newdata is missing, user arguments will be passed to the fitted.geostan_fit method to return the fitted values of the model.
alpha	A single numeric value or a numeric vector with length equal to nrow(newdata); alpha serves as the intercept in the linear predictor. The default is to use the posterior mean of the intercept. Even if type = "response", this needs to be provided on the scale of the linear predictor. See Details for additional information.
center	May be a vector of numeric values or a logical scalar to pass to <a href="#">scale</a> . Defaults to using object\$x_center. If the model was fit using centerx = TRUE, then covariates were centered and their mean values are stored in object\$x_center and the predict method will use them to automatically center newdata; if the model was fit with centerx = FALSE, then object\$x_center = FALSE and newdata will not be centered.
type	By default, results from predict are on the scale of the linear predictor (type = "link"). The alternative (type = "response") is on the scale of the response variable. For example, the default return values for a Poisson model are log-rates, and using type = "response" will return the rates (by exponentiating the log-rates).

## Details

### predict.geostan\_fit:

The purpose of the predict method is to explore marginal effects of (combinations of) covariates. The method sets the intercept equal to its posterior mean (i.e.,  $\alpha = \text{mean}(\text{as.matrix}(\text{object}, \text{pars} = \text{"intercept"}))$ ); the only source of uncertainty in the results is the posterior distribution of the coefficients, which can be obtained using  $\text{Beta} = \text{as.matrix}(\text{object}, \text{pars} = \text{"beta"})$ .

Be aware that in non-linear models (including Poisson and Binomial models) marginal effects of each covariate are sensitive to the level of other covariates in the model. If the model includes any spatially-lagged covariates (introduced using the slx argument) or a spatial autocorrelation term,

these terms will essentially be fixed at zero for the purposes of calculating marginal effects. To explore the impact of these (missing) terms, you can add their values to the linear predictor using the `alpha` argument.

## Value

Methods `residuals`, `fitted`, `predict`, and `spatial` return a matrix containing all samples for each observation if `summary = FALSE`, else if `summary = TRUE` a `data.frame` containing a summary of the posterior distribution at each observation (of, respectively, residuals, fitted values, predicted values, or the spatial trend). The `predict` method will return a data frame with a summary of results together with use-provided `newdata`.

The `predict` method is designed for reviewing marginal effects of covariates. Thus, results do not include spatial trends or offset terms. To obtain the fitted values of the model (as opposed to predictions from new data), use the `fitted` method. For the posterior predictive distribution, see [posterior\\_predict](#).

`plot` returns a `ggplot` object that can be customized using the `ggplot2` package.

`as.matrix`, `as.data.frame`, `as.array` return samples from the joint posterior distribution of parameters in the format corresponding to their names. The `pars` argument is used to return samples from only a subset of parameters.

## See Also

[posterior\\_predict](#), [stan\\_glm](#), [stan\\_esf](#), [stan\\_icar](#), [stan\\_car](#)

## Examples

```
data(georgia)
C <- shape2mat(georgia, style = "B")
cars <- prep_car_data(C)
georgia$income <- georgia$income/1e3

fit <- stan_car(deaths.male ~ offset(log(pop.at.risk.male)) + log(income),
               slx = ~ log(income),
               centerx = TRUE,
               car_parts = cars,
               data = georgia,
               family = poisson(),
               chains = 2, iter = 600) # for speed only

# print and plot results
print(fit)
plot(fit)

# residuals
r = resid(fit)

# fitted values
# (Poisson model defaults to rates)
```

```

f1 = fitted(fit)
f2 = fitted(fit, rates = FALSE)

# spatial diagnostics
sp_diag(fit, georgia)

# spatial trend, county `random effects'
sp = spatial(fit)

# posterior predictive distribution
yrep <- posterior_predict(fit, S = 65)
plot(density(yrep[1,]), col = "gray30")
for (i in 2:nrow(yrep)) lines(density(yrep[i,]), col = "gray30")
lines(density(georgia$deaths.male), col = "darkred", lwd = 2)

# array of samples; MCMC diagnostics
S.array <- as.array(fit, pars = c("intercept", "car_scale", "car_rho"))
S.monitor <- rstan::monitor(S.array, print = FALSE, warmup = 0)
head(S.monitor)

newdata <- data.frame(
  income = seq(min(georgia$income), max(georgia$income), by = 1),
  pop.at.risk.male = 1
)

p <- predict(fit, newdata, type = "response")
plot(newdata$income, p$mean * 1e3,
      type = 'l',
      main = "Deaths per 1,000",
      ylab = NA,
      xlab = "Median county income ($1,000s)")

```

---

priors

*Prior distributions*


---

## Description

Prior distributions

## Usage

```
uniform(lower, upper, variable = NULL)
```

```
normal(location = 0, scale, variable = NULL)
```

```
student_t(df = 10, location = 0, scale, variable = NULL)
```

```
gamma(alpha, beta, variable = NULL)
```

```
hs(global_scale = 1, slab_df = 10, slab_scale, variable = "beta_ev")
```

**Arguments**

lower, upper	lower and upper bounds of the distribution
variable	A reserved slot for the variable name; if provided by the user, this may be ignored by <b>geostan</b> .
location	Location parameter(s), numeric value(s)
scale	Scale parameter(s), positive numeric value(s)
df	Degrees of freedom, positive numeric value(s)
alpha	shape parameter, positive numeric value(s)
beta	inverse scale parameter, positive numeric value(s)
global_scale	Control the (prior) degree of sparsity in the horseshoe model ( $0 < \text{global\_scale} < 1$ ).
slab_df	Degrees of freedom for the Student's t model for large coefficients in the horseshoe model ( $\text{slab\_df} > 0$ ).
slab_scale	Scale parameter for the Student's t model for large coefficients in the horseshoe model ( $\text{slab\_scale} > 0$ ).

**Details**

The prior distribution functions are used to set the values of prior parameters.

Users can control the values of the parameters, but the distribution (model) itself is fixed. The intercept and regression coefficients are given Gaussian prior distributions and scale parameters are assigned Student's t prior distributions. Degrees of freedom parameters are assigned gamma priors, and the spatial autocorrelation parameter in the CAR model, rho, is assigned a uniform prior. The horseshoe (hs) model is used by [stan\\_esf](#).

Note that the `variable` argument is used internally by `geostan`, and any user provided values will be ignored.

**Parameterizations:**

For details on how any distribution is parameterized, see the Stan Language Functions Reference document: <https://mc-stan.org/users/documentation/>.

**The horseshoe prior:**

The horseshoe prior is used by [stan\\_esf](#) as a prior for the eigenvector coefficients. The horseshoe model encodes a prior state of knowledge that effectively states, 'I believe a small number of these variables may be important, but I don't know which of them is important.' The horseshoe is a normal distribution with unknown scale (Polson and Scott 2010):

$$\text{beta}_j \sim \text{Normal}(0, \tau^2 * \lambda_j^2)$$

The scale parameter for this prior is the product of two terms:  $\lambda_j^2$  is specific to the variable  $\text{beta}_j$ , and  $\tau^2$  is known as the global shrinkage parameter.

The global shrinkage parameter is assigned a half-Cauchy prior:

$$\tau \sim \text{Cauchy}(0, \text{global\_scale} * \sigma)$$



where `global_scale` is provided by the user and `sigma` is the scale parameter for the outcome variable; for Poisson and binomial models, `sigma` is fixed at one. Use `global_scale` to control the overall sparsity of the model.

The second part of the model is a Student's t prior for `lambda_j`. Most `lambda_j` will be small, since the model is half-Cauchy:

$$\text{lambda}_j \sim \text{Cauchy}(0, 1)$$

This model results in most `lambda_j` being small, but due to the long tails of the Cauchy distribution, strong evidence in the data can force any particular `lambda_j` to be large. Piironen and Vehtari (2017) adjust the model so that those large `lambda_j` are effectively assigned a Student's t model:

$$\text{Big\_lambda}_j \sim \text{Student\_t}(\text{slab\_df}, 0, \text{slab\_scale})$$

This is a schematic representation of the model; see Piironen and Vehtari (2017) or Donegan et al. (2020) for details.

## Value

An object of class `prior` which will be used internally by **geostan** to set parameters of prior distributions.

### Student's t:

Return value for `student_t` depends on the input; if no arguments are provided (specifically, if the scale parameter is missing), this will return an object of class `'family'`; if at least the scale parameter is provided, `student_t` will return an object of class `prior` containing parameter values for the Student's t distribution.

## Source

Donegan, C., Y. Chun and A. E. Hughes (2020). Bayesian estimation of spatial filters with Moran's Eigenvectors and hierarchical shrinkage priors. *Spatial Statistics*. doi:10.1016/j.spasta.2020.100450 (open access: doi:10.31219/osf.io/fah3z).

Polson, N.G. and J.G. Scott (2010). Shrink globally, act locally: Sparse Bayesian regularization and prediction. *Bayesian Statistics* 9, 501-538.

Piironen, J and A. Vehtari (2017). Sparsity information and regularization in the horseshoe and other shrinkage priors. In *Electronic Journal of Statistics*, 11(2):5018-5051.

## Examples

```
data(georgia)
prior <- list()
prior$beta <- normal(c(0, 0), c(1, 1))
prior$intercept <- normal(-5, 3)
fit <- stan_glm(deaths.male ~ offset(log(pop.at.risk.male)) + ICE + college,
               re = ~ GEOID,
               data = georgia,
               family = poisson(),
               prior = prior,
```

```

      prior_only = TRUE,
      chains = 2, iter = 600) # for speed only
plot(fit)

se <- data.frame(insurance = georgia$insurance.se)
prior <- list()
prior$df <- gamma(3, 0.2)
prior$location <- normal(50, 50)
prior$scale <- student_t(12, 10, 20)
ME <- prep_me_data(se = se, prior = prior)
fit <- stan_glm(log(rate.male) ~ insurance,
               data = georgia,
               ME = ME,
               prior_only = TRUE,
               chains = 2, iter = 600) # for speed only

```

---

row_standardize	<i>Row-standardize a matrix; safe for zero row-sums.</i>
-----------------	--

---

### Description

Row-standardize a matrix; safe for zero row-sums.

### Usage

```
row_standardize(C, warn = TRUE, msg = "Row standardizing connectivity matrix")
```

### Arguments

C	A matrix
warn	Print msg if warn = TRUE.
msg	A warning message to print.

### Value

A row-standardized matrix,  $W$  (i.e., all row sums equal 1, or zero).

### Examples

```

A <- shape2mat(georgia)
head(Matrix::summary(A))
Matrix::rowSums(A)

W <- row_standardize(A)
head(Matrix::summary(W))
Matrix::rowSums(W)

```

---

sentencing

*Florida state prison sentencing counts by county, 1905-1910*

---

### Description

A spatial polygons data frame of historical 1910 county boundaries of Florida with aggregated state prison sentencing counts and census data. Sentencing and population counts are aggregates over the period 1905-1910, where populations were interpolated linearly between decennial censuses of 1900 and 1910.

### Usage

```
sentencing
```

### Format

A spatial polygons data frame with the following attributes:

**name** County name

**wpop** White population total for years 1905-1910

**bpop** Black population total for years 1905-1910

**sents** Number of state prison sentences, 1905-1910

**plantation\_belt** Binary indicator for inclusion in the plantation belt

**pct\_ag\_1910** Percent of land area in agriculture, 1910

**expected\_sents** Expected sentences given demographic information and state level sentencing rates by race

**sir\_raw** Standardized incident ratio (observed/expected sentences)

### Source

Donegan, Connor. "The Making of Florida's 'Criminal Class': Race, Modernity and the Convict Leasing Program." *Florida Historical Quarterly* 97.4 (2019): 408-434. <https://osf.io/2wj7s/>.

Mullen, Lincoln A. and Bratt, Jordon. "USABoundaries: Historical and Contemporary Boundaries of the United States of America," *Journal of Open Source Software* 3, no. 23 (2018): 314, [doi:10.21105/joss.00314](https://doi.org/10.21105/joss.00314).

### Examples

```
data(sentencing)
head(sentencing@data)
```

---

se_log	<i>Standard error of log(x)</i>
--------	---------------------------------

---

**Description**

Transform the standard error of  $x$  to standard error of  $\log(x)$ .

**Usage**

```
se_log(x, se, method = c("mc", "delta"), nsim = 5000, bounds = c(0, Inf))
```

**Arguments**

<code>x</code>	An estimate
<code>se</code>	Standard error of $x$
<code>method</code>	The "delta" method uses a Taylor series approximation; the default method, "mc", uses a simple monte carlo method.
<code>nsim</code>	Number of draws to take if <code>method = "mc"</code> .
<code>bounds</code>	Lower and upper bounds for the variable, used in the monte carlo method. Must be a length-two numeric vector with lower bound greater than or equal to zero (i.e. <code>c(lower, upper)</code> as in default <code>bounds = c(0, Inf)</code> ).

**Details**

The delta method returns  $x^{-1} * se$ . The monte carlo method is detailed in the examples section.

**Value**

Numeric vector of standard errors

**Examples**

```
data(georgia)
x = georgia$college
se = georgia$college.se

lse1 = se_log(x, se)
lse2 = se_log(x, se, method = "delta")
plot(lse1, lse2); abline(0, 1)

# the monte carlo method
x = 10
se = 2
z = rnorm(n = 20e3, mean = x, sd = se)
l.z = log(z)
sd(l.z)
se_log(x, se, method = "mc")
se_log(x, se, method = "delta")
```

---

shape2mat	<i>Create spatial and space-time connectivity matrices</i>
-----------	--

---

## Description

Creates sparse matrix representations of spatial connectivity structures

## Usage

```
shape2mat(
  shape,
  style = c("B", "W"),
  queen = TRUE,
  snap = sqrt(.Machine$double.eps),
  t = 1,
  st.style = c("contemp", "lag")
)
```

## Arguments

shape	An object of class <code>sf</code> , <code>SpatialPolygons</code> or <code>SpatialPolygonsDataFrame</code> .
style	What kind of coding scheme should be used to create the spatial connectivity matrix? Defaults to "B" for binary; use "W" for row-standardized weights.
queen	Passed to <code>poly2nb</code> to set the contiguity condition. Defaults to TRUE so that a single shared boundary point (rather than a shared border/line) between polygons is sufficient for them to be considered neighbors.
snap	Passed to <code>poly2nb</code> ; "boundary points less than 'snap' distance apart are considered to indicate contiguity."
t	Number of time periods. Only the binary coding scheme is available for space-time connectivity matrices.
st.style	For space-time data, what type of space-time connectivity structure should be used? Options are "lag" for the lagged specification and "contemp" (the default) for contemporaneous specification (see Details).

## Details

Haining and Li (Ch. 4) provide a helpful discussion of spatial connectivity matrices (Ch. 4).

The space-time connectivity matrix can be used for eigenvector space-time filtering (`stan_esf`). The lagged' space-time structure connects each observation to its own past (one period lagged) value and the contemporaneous' specification links each observation to its neighbors and to its own in situ past (one period lagged) value (Griffith 2012, p. 23).

## Value

A spatial connectivity matrix

**Source**

Bivand, Roger S. and Pebesma, Edzer and Gomez-Rubio, Virgilio (2013). Applied spatial data analysis with R, Second edition. Springer, NY. <https://asdar-book.org/>

Griffith, Daniel A. (2012). Space, time, and space-time eigenvector filter specifications that account for autocorrelation. *Estadística Espanola*, 54(177), 7-34.

Haining, Robert P. and Li, Guangquan (2020). *Regression Modelling With Spatial and Spatial-Temporal Data: A Bayesian Approach*. CRC Press.

**See Also**

[edges](#) [prep\\_car\\_data](#) [prep\\_icar\\_data](#)

**Examples**

```
data(georgia)

## binary adjacency matrix
C <- shape2mat(georgia, "B")
## row sums gives the numbers of neighbors per observation
Matrix::rowSums(C)
head(Matrix::summary(C))

## row-standardized matrix
W <- shape2mat(georgia, "W")
Matrix::rowSums(W)
head(Matrix::summary(W))

## space-time matrices
## for eigenvector space-time filtering
## if you have multiple years with same neighbors,
## provide the geography (for a single year!) and number of years \code{t}
Cst <- shape2mat(georgia, t = 5)
dim(Cst)
EVst <- make_EV(Cst)
dim(EVst)
```

---

sim\_sar

*Simulate spatially autocorrelated data*

---

**Description**

Given a spatial weights matrix and degree of autocorrelation, returns autocorrelated data.

**Usage**

```
sim_sar(m = 1, mu = rep(0, nrow(w)), w, rho, sigma = 1, ...)
```

**Arguments**

m	The number of samples required. Defaults to $m=1$ to return an $n$ -length vector; if $m>1$ , an $m \times n$ matrix is returned (i.e. each row will contain a sample of correlated values).
mu	An $n$ -length vector of mean values. Defaults to a vector of zeros with length equal to $nrow(w)$ .
w	Row-standardized $n \times n$ spatial weights matrix.
rho	Spatial autocorrelation parameter in the range $(-1, 1)$ . Typically a scalar value; otherwise an $n$ -length numeric vector.
sigma	Scale parameter (standard deviation). Defaults to $\sigma = 1$ . Typically a scalar value; otherwise an $n$ -length numeric vector.
...	further arguments passed to <code>MASS::mvrnorm</code> .

**Details**

Calls `MASS::mvrnorm` internally to draw from the multivariate normal distribution. The covariance matrix is specified following the simultaneous autoregressive (SAR) model.

**Value**

If  $m = 1$  a vector of the same length as `mu`, otherwise an  $m \times \text{length}(\text{mu})$  matrix with one sample in each row.

**See Also**

[aple](#), [mc](#), [moran\\_plot](#), [lisa](#), [shape2mat](#)

**Examples**

```
data(georgia)
w <- shape2mat(georgia, "W")
x <- sim_sar(w = w, rho = 0.5)
aple(x, w)

x <- sim_sar(w = w, rho = 0.7, m = 10)
dim(x)
apply(x, 1, aple, w = w)
```

**Description**

Visual diagnostics for areal data and model residuals

**Usage**

```

sp_diag(
  y,
  shape,
  name = "y",
  plot = TRUE,
  mc_style = c("scatter", "hist"),
  style = c("W", "B"),
  w = shape2mat(shape, match.arg(style)),
  binwidth = function(x) 0.5 * sd(x, na.rm = TRUE),
  ...
)

## S3 method for class 'geostan_fit'
sp_diag(
  y,
  shape,
  name = "Residual",
  plot = TRUE,
  mc_style = c("scatter", "hist"),
  style = c("W", "B"),
  w = shape2mat(shape, match.arg(style)),
  binwidth = function(x) 0.5 * stats::sd(x, na.rm = TRUE),
  rates = TRUE,
  size = 0.15,
  ...
)

## S3 method for class 'numeric'
sp_diag(
  y,
  shape,
  name = "y",
  plot = TRUE,
  mc_style = c("scatter", "hist"),
  style = c("W", "B"),
  w = shape2mat(shape, match.arg(style)),
  binwidth = function(x) 0.5 * stats::sd(x, na.rm = TRUE),
  ...
)

```

**Arguments**

y	A numeric vector, or a fitted geostan model (class <code>geostan_fit</code> ).
shape	An object of class <code>sf</code> or another spatial object coercible to <code>sf</code> with <code>sf::st_as_sf</code> such as <code>SpatialPolygonsDataFrame</code> .
name	The name to use on the plot labels; default to "y" or, if y is a <code>geostan_fit</code> object, to "Residuals".



plot	If FALSE, return a list of gg plots.
mc_style	Character string indicating how to plot the residual Moran coefficient (only used if y is a fitted model): if mc = "scatter", then <code>moran_plot</code> will be used with the marginal residuals; if mc = "hist", then a histogram of Moran coefficient values will be returned, where each plotted value represents the degree of residual autocorrelation in a draw from the joint posterior distribution of model parameters.
style	Style of connectivity matrix; if w is not provided, style is passed to <code>shape2mat</code> and defaults to "W" for row-standardized.
w	An optional spatial connectivity matrix; if not provided, one will be created using <code>shape2mat</code> .
binwidth	A function with a single argument that will be passed to the binwidth argument in <code>geom_histogram</code> . The default is to set the width of bins to $0.5 * sd(x)$ .
...	Additional arguments passed to <code>residuals.geostan_fit</code> . For binomial and Poisson models, this includes the option to view the outcome variable as a rate (the default) rather than a count; for <code>stan_car</code> models with auto-Gaussian likelihood ( <code>fit\$family\$family = "auto_gaussian"</code> ), the residuals will be detrended by default, <code>trend = FALSE</code> .
rates	For Poisson and binomial models, convert the outcome variable to a rate before calculating residuals. Defaults to rates = TRUE.
size	Point size and linewidth for point-interval plot of observed vs. fitted values (passed to <code>geom_pointrange</code> ).

## Value

A grid of spatial diagnostic plots. When provided with a numeric vector, this function plots a histogram, Moran scatter plot, and map. When provided with a fitted geostan model, the function returns a point-interval plot of observed values against fitted values (mean and 95 percent credible interval), either a Moran scatter plot of residuals or a histogram of Moran coefficient values calculated from the joint posterior distribution of the residuals, and a map of the mean posterior residuals (means of the marginal distributions).

If `plot = TRUE`, the ggplots are drawn using `grid.arrange`; otherwise, they are returned in a list. For the `geostan_fit` method, the underlying data for the Moran coefficient will also be returned if `plot = FALSE`.

## See Also

[me\\_diag](#), [mc](#), [moran\\_plot](#), [aple](#)

## Examples

```
data(georgia)
sp_diag(georgia$college, georgia)

bin_fn <- function(y) mad(y, na.rm = TRUE)
sp_diag(georgia$college, georgia, binwidth = bin_fn)
```

```
fit <- stan_glm(log(rate.male) ~ log(income),
               data = georgia,
               chains = 2, iter = 800) # for speed only
sp_diag(fit, georgia)
```

---

 stan\_car

*Conditional autoregressive (CAR) models*


---

## Description

Use the CAR model as a prior on parameters, or fit data to an auto-Gaussian CAR model.

## Usage

```
stan_car(
  formula,
  slx,
  re,
  data,
  car_parts,
  C,
  family = gaussian(),
  prior = NULL,
  ME = NULL,
  centerx = FALSE,
  prior_only = FALSE,
  censor_point,
  chains = 4,
  iter = 2000,
  refresh = 500,
  keep_all = FALSE,
  pars = NULL,
  control = NULL,
  ...
)
```

## Arguments

- |         |  |
|---------|--|
| formula | A model formula, following the R <a href="#">formula</a> syntax. Binomial models can be specified by setting the left hand side of the equation to a data frame of successes and failures, as in <code>cbind(successes, failures) ~ x</code> .                               |
| slx     | Formula to specify any spatially-lagged covariates. As in, <code>~ x1 + x2</code> (the intercept term will be removed internally). When setting priors for beta, remember to include priors for any SLX terms.   |
| re      | To include a varying intercept (or "random effects") term, <code>alpha_re</code> , specify the grouping variable here using formula syntax, as in <code>~ ID</code> . Then, <code>alpha_re</code> is a vector of parameters added to the linear predictor of the model, and: |

```
alpha_re ~ N(0, alpha_tau)
alpha_tau ~ Student_t(d.f., location, scale).
```

With the CAR model, any `alpha_re` term should be at a *different* level or scale than the observations; that is, at a different scale than the autocorrelation structure of the CAR model itself.

<code>data</code>	A <code>data.frame</code> or an object coercible to a data frame by <code>as.data.frame</code> containing the model data.
<code>car_parts</code>	A list of data for the CAR model, as returned by <code>prep_car_data</code> .
<code>C</code>	Optional spatial connectivity matrix which will be used to calculate residual spatial autocorrelation as well as any user specified <code>slx</code> terms; it will automatically be row-standardized before calculating <code>slx</code> terms. See <code>shape2mat</code> .
<code>family</code>	The likelihood function for the outcome variable. Current options are <code>auto_gaussian()</code> , <code>binomial(link = "logit")</code> , and <code>poisson(link = "log")</code> ; if <code>family = gaussian()</code> is provided, it will automatically be converted to <code>auto_gaussian()</code> .
<code>prior</code>	A named list of parameters for prior distributions (see <code>priors</code> ): <ul style="list-style-type: none"> <li><b>intercept</b> The intercept is assigned a Gaussian prior distribution (see <code>normal</code>).</li> <li><b>beta</b> Regression coefficients are assigned Gaussian prior distributions. Variables must follow their order of appearance in the model formula. Note that if you also use <code>slx</code> terms (spatially lagged covariates), and you use custom priors for <code>beta</code>, then you have to provide priors for the <code>slx</code> terms. Since <code>slx</code> terms are <i>prepended</i> to the design matrix, the prior for the <code>slx</code> term will be listed first.</li> <li><b>car_scale</b> The scale of the CAR model, <code>car_scale</code>. The scale is assigned a Student's t prior model (constrained to be positive).</li> <li><b>car_rho</b> The spatial autocorrelation parameter in the CAR model, <code>rho</code>, is assigned a uniform prior distribution. By default, the prior will be uniform over all permissible values as determined by the eigenvalues of the connectivity matrix, <code>C</code>. The range of permissible values for <code>rho</code> is automatically printed to the console by <code>prep_car_data</code>.</li> <li><b>tau</b> The scale parameter for any varying intercepts (a.k.a exchangeable random effects, or partial pooling) terms. This scale parameter, <code>tau</code>, is assigned a Student's t prior (constrained to be positive).</li> </ul>
<code>ME</code>	To model observational uncertainty (i.e. measurement or sampling error) in any or all of the covariates, provide a list of data as constructed by the <code>prep_me_data</code> function.
<code>centerx</code>	To center predictors on their mean values, use <code>centerx = TRUE</code> . If the <code>ME</code> argument is used, the modeled covariate (i.e., latent variable), rather than the raw observations, will be centered. When using the <code>ME</code> argument, this is the recommended method for centering the covariates.
<code>prior_only</code>	Logical value; if <code>TRUE</code> , draw samples only from the prior distributions of parameters.
<code>censor_point</code>	Integer value indicating the maximum censored value; this argument is for modeling censored (suppressed) outcome data, typically disease case counts or deaths.
<code>chains</code>	Number of MCMC chains to use.

<code>iter</code>	Number of samples per chain.
<code>refresh</code>	Stan will print the progress of the sampler every <code>refresh</code> number of samples. Set <code>refresh=0</code> to silence this.
<code>keep_all</code>	If <code>keep_all = TRUE</code> then samples for all parameters in the Stan model will be kept; this is necessary if you want to do model comparison with Bayes factors and the <code>bridgesampling</code> package.
<code>pars</code>	Optional; specify any additional parameters you'd like stored from the Stan model.
<code>control</code>	A named list of parameters to control the sampler's behavior. See <a href="#">stan</a> for details.
<code>...</code>	Other arguments passed to <a href="#">sampling</a> . For multi-core processing, you can use <code>cores = parallel::detectCores()</code> , or run <code>options(mc.cores = parallel::detectCores())</code> first.

## Details

CAR models are discussed in Cressie and Wikle (2011, p. 184-88), Cressie (2015, Ch. 6-7), and Haining and Li (2020, p. 249-51).

The Stan code for this implementation of the CAR model first introduced in Donegan et al. (2021, supplementary material) for models of small area survey data.

Details and results depend on the `family` argument, as well as on the particular CAR specification chosen (see [prep\\_car\\_data](#)).

### Auto-Gaussian:

When `family = auto_gaussian()`, the CAR model is specified as follows:

```
Y ~ MVGauss(Mu, Sigma)
Sigma = (I - rho C)^-1 * M * tau^2
```

where `Mu` is the mean vector (with intercept, covariates, etc.), `C` is a spatial connectivity matrix, and `M` is a known diagonal matrix with diagonal entries proportional to the conditional variances. `C` and `M` are provided by [prep\\_car\\_data](#).

The covariance matrix of the CAR model, `Sigma`, contains two parameters: `car_rho` (`rho`), which controls the degree of spatial autocorrelation, and the scale parameter, `car_scale` (`tau`). The range of permissible values for `rho` depends on the specification of `C` and `M`; for options, see [prep\\_car\\_data](#) and Cressie and Wikle (2011, pp. 184-188).

The auto-Gaussian model contains an implicit spatial trend (i.e., autocorrelation) component which is calculated as follows (Cressie 2015, p. 564):

$$\text{trend} = \rho * C * (Y - \text{Mu}).$$

This term can be extracted from a fitted auto-Gaussian model using the [spatial](#) method.

When applied to a fitted auto-Gaussian model, the [residuals.geostan\\_fit](#) method returns 'de-trended' residuals by default. That is,

$$\text{residual} = Y - \text{Mu} - \text{trend}.$$

To obtain "raw" residuals ( $Y - \text{Mu}$ ), use `residuals(fit, detrend = FALSE)`.

**Poisson:**

For family = poisson(), the model is specified as:

```
Y ~ Poisson(exp(offset + lambda))
lambda ~ MVGauss(Mu, Sigma)
Sigma = (I - rho C)^-1 * M * tau^2
```

These models are most often used to calculate small area incidence rates (mortality or disease incidence rates); the user provided offset should be, then, the natural logarithm of the denominator in the rates, e.g., log-population at risk.

For Poisson models, the `spatial` method returns the parameter vector `phi`, which is the log-risk minus the intercept and any covariates:

```
phi = lambda - Mu.
```

This is the spatial autocorrelation component. This is equivalent to specifying the model as:

```
Y ~ Poisson(exp(offset + Mu + phi))
phi ~ MVGauss(0, Sigma)
Sigma = (I - rho C)^-1 * M * tau^2.
```

In the Poisson CAR model, `phi` contains a latent spatial trend as well as additional variation around it. If you would like to extract the latent/implicit spatial trend from `phi`, you can do so by calculating (following Cressie 2015, p. 564):

```
trend = rho * C * phi.
```

**Binomial:**

For family = binomial(), the model is specified as:

```
Y ~ Binomial(N, theta)
logit(theta) ~ MVGauss(Mu, Sigma)
Sigma = (I - rho C)^-1 * M * tau^2
```

where outcome data `Y` are counts, `N` is the number of trials, and `theta` is the 'success' rate. Note that the model formula should be structured as: `cbind(succeses, failures) ~ x`, such that `trials = succeses + failures`.

For fitted Binomial models, the `spatial` method will return the parameter vector `phi`, equivalent to:

```
phi = logit(theta) - Mu.
```

**Spatially lagged covariates (SLX):**

The `slx` argument is a convenience function for including SLX terms. For example,

```
stan_glm(y ~ x1 + x2, slx = ~ x1, \...)
```

is a shortcut for

```
stan_glm(y ~ I(W \%*\% x1) + x1 + x2, \...)
```

where `W` is a row-standardized spatial weights matrix (see [shape2mat](#)). SLX terms will always be *pre-pended* to the design matrix, as above, which is important to know when setting prior distributions for regression coefficients.

For measurement error (ME) models, the SLX argument is the only way to include spatially lagged covariates since the SLX term needs to be re-calculated on each iteration of the MCMC algorithm.

**Measurement error (ME) models:**

The ME models are designed for surveys with spatial sampling designs, such as the American Community Survey (ACS) estimates. With estimates,  $x$ , and their standard errors,  $se$ , the ME models have one of the the following two specifications, depending on the user input:

```
x ~ Gauss(x_true, se)
x_true ~ MVGauss(mu, Sigma)
Sigma = (I - rho C)^(-1) M * tau^2
mu ~ Gauss(0, 100)
tau ~ student_t(10, 0, 40)
rho ~ uniform(lower_bound, upper_bound)
```

where the covariance matrix,  $\Sigma$ , has the conditional autoregressive specification, and  $\tau$  is the scale parameter. For non-spatial ME models, the following is used instead:

```
x ~ Gauss(x_true, se)
x_true ~ student_t(df, mu, sigma)
df ~ gamma(3, 0.2)
mu ~ Gauss(0, 100)
sigma ~ student_t(10, 0, 40)
```

For strongly skewed variables, such census tract poverty rates, it can be advantageous to apply a logit transformation to  $x\_true$  before applying the CAR or Student t prior model. When the `logit` argument is used, the model becomes:

```
x ~ Gauss(x_true, se)
logit(x_true) ~ MVGauss(mu, Sigma)
```

and similar for the Student t model.

**Censored counts:**

Vital statistics systems and disease surveillance programs typically suppress case counts when they are smaller than a specific threshold value. In such cases, the observation of a censored count is not the same as a missing value; instead, you are informed that the value is an integer somewhere between zero and the threshold value. For Poisson models (`family = poisson()`), you can use the `sensor_point` argument to encode this information into your model.

Internally, `geostan` will keep the index values of each censored observation, and the index value of each of the fully observed outcome values. For all observed counts, the likelihood statement will be:

$$p(y_i \mid \text{data}, \text{model}) = \text{Poisson}(y_i \mid \text{fitted}_i),$$

as usual. For each censored count, the likelihood statement will equal the cumulative Poisson distribution function for values zero through the sensor point:

$$p(y_j \mid \text{data}, \text{model}) = \sum_{m=0}^{\text{sensor\_point}} \text{Poisson}(c_m \mid \text{fitted}_j),$$

For example, the US Centers for Disease Control and Prevention's CDC WONDER database censors all death counts between 0 and 9. To model CDC WONDER mortality data, you could provide `sensor_point = 9` and then the likelihood statement for censored counts would equal the summation of the Poisson probability mass function over each integer ranging from zero through 9 (inclusive), conditional on the fitted values (i.e., all model parameters). See Donegan (2021) for additional discussion, references, and Stan code.

**Value**

An object of class `geostan_fit` (a list) containing:

**summary** Summaries of the main parameters of interest; a data frame.

**diagnostic** Widely Applicable Information Criteria (WAIC) with a measure of effective number of parameters (`eff_pars`) and mean log pointwise predictive density (`lpd`), and mean residual spatial autocorrelation as measured by the Moran coefficient.

**stanfit** an object of class `stanfit` returned by `rstan::stan`

**data** a data frame containing the model data

**family** the user-provided or default family argument used to fit the model

**formula** The model formula provided by the user (not including CAR component)

**slx** The `slx` formula

**re** A list containing `re`, the varying intercepts (`re`) formula if provided, and `Data` a data frame with columns `id`, the grouping variable, and `idx`, the index values assigned to each group.

**priors** Prior specifications.

**x\_center** If covariates are centered internally (`center_x = TRUE`), then `x_center` is a numeric vector of the values on which covariates were centered.

**spatial** A data frame with the name of the spatial component parameter (either "phi" or, for auto Gaussian models, "trend") and method ("CAR")

**ME** A list indicating if the object contains an ME model; if so, the user-provided ME list is also stored here.

**C** Spatial connectivity matrix (in sparse matrix format).

**Author(s)**

Connor Donegan, <Connor.Donegan@UTDallas.edu>

**Source**

Cressie, Noel (2015 (1993)). *Statistics for Spatial Data*. Wiley Classics, Revised Edition.

Cressie, Noel and Wikle, Christopher (2011). *Statistics for Spatio-Temporal Data*. Wiley.

Donegan, Connor and Chun, Yongwan and Griffith, Daniel A. (2021). Modeling community health with areal data: Bayesian inference with survey standard errors and spatial structure. *Int. J. Env. Res. and Public Health* 18 (13): 6856. DOI: 10.3390/ijerph18136856 Data and code: <https://github.com/ConnorDonegan/survey-HBM>.

Donegan, Connor (2021). Spatial conditional autoregressive models in Stan. *OSF Preprints*. doi:10.31219/osf.io/3ey65.

Haining, Robert and Li, Guangquan (2020). *Modelling Spatial and Spatio-Temporal Data: A Bayesian Approach*. CRC Press.

**Examples**

```

# for automatic parallel processing
#options(mc.cores = parallel::detectCores())

# model mortality rates
data(georgia)
C <- shape2mat(georgia, style = "B")
cp <- prep_car_data(C)

fit <- stan_car(deaths.male ~ offset(log(pop.at.risk.male)),
               car_parts = cp,
               data = georgia,
               family = poisson())

rstan::stan_rhat(fit$stanfit)
rstan::stan_mcse(fit$stanfit)
print(fit)
sp_diag(fit, georgia)

# censored count outcomes
sum(is.na(georgia$deaths.female))
fit <- stan_car(deaths.female ~ offset(log(pop.at.risk.female)),
               car_parts = cp,
               data = georgia,
               family = poisson(),
               censor_point = 9)

## DCAR specification (inverse-distance based)
library(sf)
A <- shape2mat(georgia, "B")
D <- sf::st_distance(sf::st_centroid(georgia))
A <- D * A
cp <- prep_car_data(A, "DCAR", k = 1)

fit <- stan_car(deaths.male ~ offset(log(pop.at.risk.male)),
               data = georgia,
               car = cp,
               family = poisson())

print(fit)

```

---

stan\_esf

*Spatial filtering*


---

**Description**

Fit a spatial regression model using eigenvector spatial filtering (ESF).



**Usage**

```
stan_esf(
  formula,
  slx,
  re,
  data,
  C,
  EV = make_EV(C, nsa = nsa, threshold = threshold),
  nsa = FALSE,
  threshold = 0.25,
  family = gaussian(),
  prior = NULL,
  ME = NULL,
  centerx = FALSE,
  censor_point,
  prior_only = FALSE,
  chains = 4,
  iter = 2000,
  refresh = 500,
  keep_all = FALSE,
  pars = NULL,
  control = NULL,
  ...
)
```

**Arguments**

formula	A model formula, following the R <a href="#">formula</a> syntax. Binomial models are specified by setting the left hand side of the equation to a data frame of successes and failures, as in <code>cbind(successes, failures) ~ x</code> .
slx	Formula to specify any spatially-lagged covariates. As in, <code>~ x1 + x2</code> (the intercept term will be removed internally). When setting priors for beta, remember to include priors for any SLX terms.
re	To include a varying intercept (or "random effects") term, <code>alpha_re</code> , specify the grouping variable here using formula syntax, as in <code>~ ID</code> . Then, <code>alpha_re</code> is a vector of parameters added to the linear predictor of the model, and:  $\text{alpha\_re} \sim N(0, \text{alpha\_tau})$ $\text{alpha\_tau} \sim \text{Student\_t}(\text{d.f.}, \text{location}, \text{scale}).$
data	A <code>data.frame</code> or an object coercible to a data frame by <code>as.data.frame</code> containing the model data.
C	Spatial connectivity matrix which will be used to calculate eigenvectors, if EV is not provided by the user. Typically, the binary connectivity matrix is best for calculating eigenvectors (i.e., using <code>C = shape2mat(shape, style = "B")</code> ). This matrix will also be used to calculate residual spatial autocorrelation and any user specified <code>slx</code> terms; it will be row-standardized before calculating <code>slx</code> terms. See <a href="#">shape2mat</a> .

EV	A matrix of eigenvectors from any (transformed) connectivity matrix, presumably spatial (see <a href="#">make_EV</a> ). If EV is provided, still also provide a spatial weights matrix C for other purposes; threshold and nsa are ignored for user provided EV.
nsa	Include eigenvectors representing negative spatial autocorrelation? Defaults to nsa = FALSE. This is ignored if EV is provided.
threshold	Eigenvectors with standardized Moran coefficient values below this threshold value will be excluded from the candidate set of eigenvectors, EV. This defaults to threshold = 0.25, and is ignored if EV is provided.
family	The likelihood function for the outcome variable. Current options are family = gaussian(), student_t() and poisson(link = "log"), and binomial(link = "logit").
prior	A named list of parameters for prior distributions (see <a href="#">priors</a> ): <ul style="list-style-type: none"> <li><b>intercept</b> The intercept is assigned a Gaussian prior distribution (see <a href="#">normal</a>).</li> <li><b>beta</b> Regression coefficients are assigned Gaussian prior distributions. Variables must follow their order of appearance in the model formula. Note that if you also use slx terms (spatially lagged covariates), and you use custom priors for beta, then you have to provide priors for the slx terms. Since slx terms are <i>prepended</i> to the design matrix, the prior for the slx term will be listed first.</li> <li><b>sigma</b> For family = gaussian() and family = student_t() models, the scale parameter, sigma, is assigned a (half-) Student's t prior distribution. The half-Student's t prior for sigma is constrained to be positive.</li> <li><b>nu</b> nu is the degrees of freedom parameter in the Student's t likelihood (only used when family = student_t()). nu is assigned a gamma prior distribution. The default prior is prior = list(nu = gamma(alpha = 3, beta = 0.2)).</li> <li><b>tau</b> The scale parameter for random effects, or varying intercepts, terms. This scale parameter, tau, is assigned a half-Student's t prior. To set this, use, e.g., prior = list(tau = student_t(df = 20, location = 0, scale = 20)).</li> <li><b>beta_ev</b> The eigenvector coefficients are assigned the horseshoe prior (Piiroinen and Vehtari, 2017), parameterized by global_scale (to control overall prior sparsity), plus the degrees of freedom and scale of a Student's t model for any large coefficients (see <a href="#">priors</a>). To allow the spatial filter to account for a greater amount of spatial autocorrelation (i.e., if you find the residuals contain spatial autocorrelation), increase the global scale parameter (to a maximum of global_scale = 1).</li> </ul>
ME	To model observational uncertainty (i.e. measurement or sampling error) in any or all of the covariates, provide a list of data as constructed by the <a href="#">prep_me_data</a> function.
centerx	To center predictors on their mean values, use centerx = TRUE. If the ME argument is used, the modeled covariate (i.e., latent variable), rather than the raw observations, will be centered. When using the ME argument, this is the recommended method for centering the covariates.
censor_point	Integer value indicating the maximum censored value; this argument is for modeling censored (suppressed) outcome data, typically disease case counts or deaths.

	For example, the US Centers for Disease Control and Prevention censors (does not report) death counts that are nine or fewer, so if you're using CDC WONDER mortality data you could provide <code>sensor_point = 9</code> .
<code>prior_only</code>	Draw samples from the prior distributions of parameters only.
<code>chains</code>	Number of MCMC chains to estimate. Default <code>chains = 4</code> .
<code>iter</code>	Number of samples per chain. Default <code>iter = 2000</code> .
<code>refresh</code>	Stan will print the progress of the sampler every <code>refresh</code> number of samples. Defaults to 500; set <code>refresh=0</code> to silence this.
<code>keep_all</code>	If <code>keep_all = TRUE</code> then samples for all parameters in the Stan model will be kept; this is necessary if you want to do model comparison with Bayes factors and the <code>bridgesampling</code> package.
<code>pars</code>	Optional; specify any additional parameters you'd like stored from the Stan model.
<code>control</code>	A named list of parameters to control the sampler's behavior. See <a href="#">stan</a> for details.
<code>...</code>	Other arguments passed to <a href="#">sampling</a> .

## Details

Eigenvector spatial filtering (ESF) is a method for spatial regression analysis. ESF is extensively covered in Griffith et al. (2019). This function implements the methodology introduced in Donegan et al. (2020), which uses Pironen and Vehtari's (2017) regularized horseshoe prior.

ESF decomposes spatial autocorrelation into a linear combination of various patterns, typically at different scales (such as local, regional, and global trends). By adding a spatial filter to a regression model, any spatial autocorrelation is shifted from the residuals to the spatial filter. ESF models take the spectral decomposition of a transformed spatial connectivity matrix,  $C$ . The resulting eigenvectors,  $EV$ , are mutually orthogonal and uncorrelated map patterns. The spatial filter is  $EV * beta\_ev$ , where  $beta\_ev$  is a vector of coefficients.

ESF decomposes the data into a global mean,  $alpha$ , global patterns contributed by covariates,  $X * beta$ , spatial trends,  $EV * beta\_ev$ , and residual variation. Thus, for `family=gaussian()`,

```
Y ~ Gauss(alpha + X * beta + EV * beta_ev, sigma).
```

An ESF component can be incorporated into the linear predictor of any generalized linear model. For example, a spatial Poisson model for rare disease incidence may be specified as follows:

```
Y ~ Poisson(exp(offset + Mu))
Mu = alpha + EV * beta_ev + A
A ~ Gauss(0, tau)
tau ~ student(20, 0, 2)
beta_ev ~ horseshoe(.)
```

The [spatial.geostan\\_fit](#) method will return  $EV * beta$ .

The model can also be extended to the space-time domain; see [shape2mat](#) to specify a space-time connectivity matrix.

The coefficients `beta_ev` are assigned the regularized horseshoe prior (Pironen and Vehtari, 2017), resulting in a relatively sparse model specification. In addition, numerous eigenvectors are automatically dropped because they represent trace amounts of spatial autocorrelation (this is controlled by the `threshold` argument). By default, `stan_esf` will drop all eigenvectors representing negative spatial autocorrelation patterns. You can change this behavior using the `nsa` argument.

### Spatially lagged covariates (SLX):

The `slx` argument is a convenience function for including SLX terms. For example,

```
stan_glm(y ~ x1 + x2, slx = ~ x1, ...)
```

is a shortcut for

```
stan_glm(y ~ I(W %*% x1) + x1 + x2, ...)
```

where `W` is a row-standardized spatial weights matrix (see [shape2mat](#)). SLX terms will always be *prepended* to the design matrix, as above, which is important to know when setting prior distributions for regression coefficients.

For measurement error (ME) models, the SLX argument is the only way to include spatially lagged covariates since the SLX term needs to be re-calculated on each iteration of the MCMC algorithm.

### Measurement error (ME) models:

The ME models are designed for surveys with spatial sampling designs, such as the American Community Survey (ACS) estimates (Donegan et al. 2021; Donegan 2021). With estimates, `x`, and their standard errors, `se`, the ME models have one of the the following two specifications, depending on the user input:

```
x ~ Gauss(x_true, se)
x_true ~ MVGauss(mu, Sigma)
Sigma = (I - rho * C)^(-1) M * tau^2
mu ~ Gauss(0, 100)
tau ~ student_t(10, 0, 40)
rho ~ uniform(lower_bound, upper_bound)
```

where the covariance matrix, `Sigma`, has the conditional autoregressive specification, and `tau` is the scale parameter. For non-spatial ME models, the following is used instead:

```
x ~ Gauss(x_true, se)
x_true ~ student_t(df, mu, sigma)
df ~ gamma(3, 0.2)
mu ~ Gauss(0, 100)
sigma ~ student_t(10, 0, 40)
```

For strongly skewed variables, such census tract poverty rates, it can be advantageous to apply a logit transformation to `x_true` before applying the CAR or Student `t` prior model. When the `logit` argument is used, the model becomes:

```
x ~ Gauss(x_true, se)
logit(x_true) ~ MVGauss(mu, Sigma)
```

and similar for the Student `t` model.

**Censored counts:**

Vital statistics systems and disease surveillance programs typically suppress case counts when they are smaller than a specific threshold value. In such cases, the observation of a censored count is not the same as a missing value; instead, you are informed that the value is an integer somewhere between zero and the threshold value. For Poisson models (`family = poisson()`), you can use the `sensor_point` argument to encode this information into your model.

Internally, `geostan` will keep the index values of each censored observation, and the index value of each of the fully observed outcome values. For all observed counts, the likelihood statement will be:

$$p(y_i \mid \text{data}, \text{model}) = \text{Poisson}(y_i \mid \text{fitted}_i),$$

as usual. For each censored count, the likelihood statement will equal the cumulative Poisson distribution function for values zero through the censor point:

$$p(y_j \mid \text{data}, \text{model}) = \sum_{m=0}^{\text{sensor\_point}} \text{Poisson}(c_m \mid \text{fitted}_j),$$

For example, the US Centers for Disease Control and Prevention's CDC WONDER database censors all death counts between 0 and 9. To model CDC WONDER mortality data, you could provide `sensor_point = 9` and then the likelihood statement for censored counts would equal the summation of the Poisson probability mass function over each integer ranging from zero through 9 (inclusive), conditional on the fitted values (i.e., all model parameters). See Donegan (2021) for additional discussion, references, and Stan code.

**Value**

An object of class `class geostan_fit` (a list) containing:

**summary** Summaries of the main parameters of interest; a data frame

**diagnostic** Widely Applicable Information Criteria (WAIC) with a measure of effective number of parameters (`eff_pars`) and mean log pointwise predictive density (`lpd`), and mean residual spatial autocorrelation as measured by the Moran coefficient.

**data** a data frame containing the model data

**EV** A matrix of eigenvectors created with `w` and `geostan::make_EV`

**C** The spatial weights matrix used to construct EV

**family** the user-provided or default `family` argument used to fit the model

**formula** The model formula provided by the user (not including ESF component)

**slx** The `slx` formula

**re** A list containing `re`, the random effects (varying intercepts) formula if provided, and data a data frame with columns `id`, the grouping variable, and `idx`, the index values assigned to each group.

**priors** Prior specifications.

**x\_center** If covariates are centered internally (`center_x = TRUE`), then `x_center` is a numeric vector of the values on which covariates were centered.

**ME** The ME data list, if one was provided by the user for measurement error models.

**spatial** A data frame with the name of the spatial component parameter ("`esf`") and method ("`ESF`")

**stanfit** an object of class `stanfit` returned by `rstan::stan`

**Author(s)**

Connor Donegan, <Connor.Donegan@UTDallas.edu>

**Source**

Chun, Y., D. A. Griffith, M. Lee and P. Sinha (2016). Eigenvector selection with stepwise regression techniques to construct eigenvector spatial filters. *Journal of Geographical Systems*, 18(1), 67-85. doi:10.1007/s1010901502253.

Dray, S., P. Legendre & P. R. Peres-Neto (2006). Spatial modelling: a comprehensive framework for principal coordinate analysis of neighbour matrices (PCNM). *Ecological Modeling*, 196(3-4), 483-493.

Donegan, C., Y. Chun and A. E. Hughes (2020). Bayesian estimation of spatial filters with Moran's Eigenvectors and hierarchical shrinkage priors. *Spatial Statistics*. doi:10.1016/j.spasta.2020.100450 (open access: doi:10.31219/osf.io/fah3z).

Donegan, Connor and Chun, Yongwan and Griffith, Daniel A. (2021). Modeling community health with areal data: Bayesian inference with survey standard errors and spatial structure. *Int. J. Env. Res. and Public Health* 18 (13): 6856. DOI: 10.3390/ijerph18136856 Data and code: <https://github.com/ConnorDonegan/survey-HBM>.

Donegan, Connor (2021). Spatial conditional autoregressive models in Stan. *OSF Preprints*. doi:10.31219/osf.io/3ey65.

Griffith, Daniel A., and P. R. Peres-Neto (2006). Spatial modeling in ecology: the flexibility of eigenfunction spatial analyses. *Ecology* 87(10), 2603-2613.

Griffith, D., and Y. Chun (2014). Spatial autocorrelation and spatial filtering, Handbook of Regional Science. Fischer, MM and Nijkamp, P. eds.

Griffith, D., Chun, Y. and Li, B. (2019). *Spatial Regression Analysis Using Eigenvector Spatial Filtering*. Elsevier.

Piironen, J and A. Vehtari (2017). Sparsity information and regularization in the horseshoe and other shrinkage priors. In *Electronic Journal of Statistics*, 11(2):5018-5051.

**Examples**

```
data(sentencing)
# spatial weights matrix with binary coding scheme
C <- shape2mat(sentencing, style = "B")

# log-expected number of sentences
## expected counts are based on county racial composition and mean sentencing rates
log_e <- log(sentencing$expected_sents)

# fit spatial Poisson model with ESF + unstructured 'random effects'
fit.esf <- stan_esf(sents ~ offset(log_e),
  re = ~ name,
  family = poisson(),
  data = sentencing,
  C = C,
  chains = 2, iter = 800) # for speed only
```

```

# spatial diagnostics
sp_diag(fit.esf, sentencing)
plot(fit.esf)

# plot marginal posterior distributions of beta_ev (eigenvector coefficients)
plot(fit.esf, pars = "beta_ev")

# plot the marginal posterior distributions of the spatial filter
plot(fit.esf, pars = "esf")

# calculate log-standardized incidence ratios
library(ggplot2)
library(sf)
f <- fitted(fit.esf, rates = FALSE)$mean
SSR <- f / sentencing$expected_sents
log.SSR <- log( SSR, base = 2 )

# map the log-SSRs
st_as_sf(sentencing) %>%
  ggplot() +
  geom_sf(aes(fill = log.SSR)) +
  scale_fill_gradient2(
    midpoint = 0,
    name = NULL,
    breaks = seq(-3, 3, by = 0.5)
  ) +
  labs(title = "Log-Standardized Sentencing Ratios",
        subtitle = "log( Fitted/Expected ), base 2"
  ) +
  theme_void()

```

---

stan\_glm

*Generalized linear models*


---

## Description

Fit a generalized linear model.

## Usage

```

stan_glm(
  formula,
  slx,
  re,
  data,
  C,
  family = gaussian(),
  prior = NULL,

```

```

ME = NULL,
centerx = FALSE,
prior_only = FALSE,
censor_point,
chains = 4,
iter = 2000,
refresh = 1000,
keep_all = FALSE,
pars = NULL,
control = NULL,
...
)

```

## Arguments

- |         |   |
|---------|---|
| formula | A model formula, following the R <a href="#">formula</a> syntax. Binomial models are specified by setting the left hand side of the equation to a data frame of successes and failures, as in <code>cbind(successes, failures) ~ x</code> .   |
| slx     | Formula to specify any spatially-lagged covariates. As in, <code>~ x1 + x2</code> (the intercept term will be removed internally). When setting priors for beta, remember to include priors for any SLX terms.  |
| re      | To include a varying intercept (or "random effects") term, <code>alpha_re</code> , specify the grouping variable here using formula syntax, as in <code>~ ID</code> . Then, <code>alpha_re</code> is a vector of parameters added to the linear predictor of the model, and:<br><br><pre>alpha_re ~ N(0, alpha_tau) alpha_tau ~ Student_t(d.f., location, scale).</pre>   |
| data    | A <code>data.frame</code> or an object coercible to a data frame by <code>as.data.frame</code> containing the model data.   |
| C       | Optional spatial connectivity matrix which will be used to calculate residual spatial autocorrelation as well as any user specified <code>slx</code> terms; it will automatically be row-standardized before calculating <code>slx</code> terms. See <a href="#">shape2mat</a> .  |
| family  | The likelihood function for the outcome variable. Current options are <code>poisson(link = "log")</code> , <code>binomial(link = "logit")</code> , <code>student_t()</code> , and the default <code>gaussian()</code> .   |
| prior   | A named list of parameters for prior distributions (see <a href="#">priors</a> ):<br><br><p><b>intercept</b> The intercept is assigned a Gaussian prior distribution (see <a href="#">normal</a>).</p> <p><b>beta</b> Regression coefficients are assigned Gaussian prior distributions. Variables must follow their order of appearance in the model formula. Note that if you also use <code>slx</code> terms (spatially lagged covariates), and you use custom priors for beta, then you have to provide priors for the <code>slx</code> terms. Since <code>slx</code> terms are <i>prepended</i> to the design matrix, the prior for the <code>slx</code> term will be listed first.</p> <p><b>sigma</b> For <code>family = gaussian()</code> and <code>family = student_t()</code> models, the scale parameter, <code>sigma</code>, is assigned a (half-) Student's t prior distribution. The half-Student's t prior for <code>sigma</code> is constrained to be positive.</p> |



	<p><b>nu</b> nu is the degrees of freedom parameter in the Student's t likelihood (only used when <code>family = student_t()</code>). nu is assigned a gamma prior distribution. The default prior is <code>prior = list(nu = gamma(alpha = 3, beta = 0.2))</code>.</p> <p><b>tau</b> The scale parameter for random effects, or varying intercepts, terms. This scale parameter, tau, is assigned a half-Student's t prior. To set this, use, e.g., <code>prior = list(tau = student_t(df = 20, location = 0, scale = 20))</code>.</p>
ME	To model observational uncertainty (i.e. measurement or sampling error) in any or all of the covariates, provide a list of data as constructed by the <a href="#">prep_me_data</a> function.
centerx	To center predictors on their mean values, use <code>centerx = TRUE</code> . If the ME argument is used, the modeled covariate (i.e., latent variable), rather than the raw observations, will be centered. When using the ME argument, this is the recommended method for centering the covariates.
prior_only	Draw samples from the prior distributions of parameters only.
sensor_point	Integer value indicating the maximum censored value; this argument is for modeling censored (suppressed) outcome data, typically disease case counts or deaths. For example, the US Centers for Disease Control and Prevention censors (does not report) death counts that are nine or fewer, so if you're using CDC WONDER mortality data you could provide <code>sensor_point = 9</code> .
chains	Number of MCMC chains to estimate.
iter	Number of samples per chain.
refresh	Stan will print the progress of the sampler every refresh number of samples; set <code>refresh=0</code> to silence this.
keep_all	If <code>keep_all = TRUE</code> then samples for all parameters in the Stan model will be kept; this is necessary if you want to do model comparison with Bayes factors and the <a href="#">bridgesampling</a> package.
pars	Specify any additional parameters you'd like stored from the Stan model.
control	A named list of parameters to control the sampler's behavior. See <a href="#">stan</a> for details.
...	Other arguments passed to <a href="#">sampling</a> . For multi-core processing, you can use <code>cores = parallel::detectCores()</code> , or run <code>options(mc.cores = parallel::detectCores())</code> first.

## Details

Fit a generalized linear model using the R formula interface. Default prior distributions are designed to be weakly informative relative to the data. Much of the functionality intended for spatial models, such as the ability to add spatially lagged covariates and observational error models, are also available in `stan_glm`. All of `geostan`'s spatial models build on top of the same Stan code used in `stan_glm`.

### Poisson models and disease mapping:

In spatial statistics, Poisson models are often used to calculate incidence rates (mortality rates, or disease incidence rates) for administrative areas like counties or census tracts. If  $Y$  are counts of

cases, and  $P$  are populations at risk, then the crude rates are  $Y/P$ . The purpose is to model risk,  $\eta$ , for which crude rates are a (noisy) indicator. Our analysis should also respect the fact that the amount of information contained in the observations,  $Y/P$ , increases with  $P$ . Hierarchical Poisson models are often the best way to incorporate all of this information.

For the Poisson model,  $Y$  is specified as the outcome and the log of the population at risk,  $\log(P)$ , needs to be provided as an offset term. For such a case, disease incidence across the collection of areas could be modeled as:

```
Y ~ Poisson(exp(log(P) + eta))
eta = alpha + A
A ~ Guass(0, tau)
tau ~ student(20, 0, 2),
```

where  $\alpha$  is the mean log-risk (incidence rate) and  $A$  is a vector of (so-called) random effects, which enable partial pooling of information across observations. Covariates can be added to the model for the log-rates, such that  $\eta = \alpha + X * \beta + A$ . See the example section of this document for a demonstration (where the denominator of the outcome is the expected count, rather than population at risk).

Note that the denominator for the rates is specified as a log-offset to provide a consistent, formula-line interface to the model. An equivalent, and perhaps more intuitive, specification is the following:

```
Y ~ Poisson(P * exp(eta))
```

where  $P$  is still the population at risk and  $\exp(\eta)$  is the incidence rate (risk).

### Spatially lagged covariates (SLX):

The `slx` argument is a convenience function for including SLX terms. For example,

```
stan_glm(y ~ x1 + x2, slx = ~ x1, ...)
```

is a shortcut for

```
stan_glm(y ~ I(W %*% x1) + x1 + x2, ...)
```

where  $W$  is a row-standardized spatial weights matrix (see [shape2mat](#)). SLX terms will always be *pre-pended* to the design matrix, as above, which is important to know when setting prior distributions for regression coefficients.

For measurement error (ME) models, the SLX argument is the only way to include spatially lagged covariates since the SLX term needs to be re-calculated on each iteration of the MCMC algorithm.

### Measurement error (ME) models:

The ME models are designed for surveys with spatial sampling designs, such as the American Community Survey (ACS) estimates (Donegan et al. 2021; Donegan 2021). With estimates,  $x$ , and their standard errors,  $se$ , the ME models have one of the the following two specifications, depending on the user input:

```
x ~ Guass(x_true, se)
x_true ~ MVGauss(mu, Sigma)
Sigma = (I - rho * C)^(-1) M * tau^2
mu ~ Guass(0, 100)
tau ~ student_t(10, 0, 40)
rho ~ uniform(lower_bound, upper_bound)
```

where the covariance matrix,  $\Sigma$ , has the conditional autoregressive specification, and  $\tau$  is the scale parameter. For non-spatial ME models, the following is used instead:

```
x ~ Gauss(x_true, se)
x_true ~ student_t(df, mu, sigma)
df ~ gamma(3, 0.2)
mu ~ Gauss(0, 100)
sigma ~ student_t(10, 0, 40)
```

For strongly skewed variables, such as census tract poverty rates, it can be advantageous to apply a logit transformation to  $x\_true$  before applying the CAR or Student t prior model. When the `logit` argument is used, the model becomes:

```
x ~ Gauss(x_true, se)
logit(x_true) ~ MVGauss(mu, Sigma)
```

and similar for the Student t model.

### Censored counts:

Vital statistics systems and disease surveillance programs typically suppress case counts when they are smaller than a specific threshold value. In such cases, the observation of a censored count is not the same as a missing value; instead, you are informed that the value is an integer somewhere between zero and the threshold value. For Poisson models (`family = poisson()`), you can use the `sensor_point` argument to encode this information into your model.

Internally, `geostan` will keep the index values of each censored observation, and the index value of each of the fully observed outcome values. For all observed counts, the likelihood statement will be:

```
p(y_i | data, model) = Poisson(y_i | fitted_i),
```

as usual. For each censored count, the likelihood statement will equal the cumulative Poisson distribution function for values zero through the censor point:

```
p(y_j | data, model) = sum_{m=0}^{sensor_point} Poisson(c_m | fitted_j),
```

For example, the US Centers for Disease Control and Prevention's CDC WONDER database censors all death counts between 0 and 9. To model CDC WONDER mortality data, you could provide `sensor_point = 9` and then the likelihood statement for censored counts would equal the summation of the Poisson probability mass function over each integer ranging from zero through 9 (inclusive), conditional on the fitted values (i.e., all model parameters). See Donegan (2021) for additional discussion, references, and Stan code.

### Value

An object of class `class geostan_fit` (a list) containing:

**summary** Summaries of the main parameters of interest; a data frame

**diagnostic** Widely Applicable Information Criteria (WAIC) with a measure of effective number of parameters (`eff_pars`) and mean log pointwise predictive density (`lpd`), and mean residual spatial autocorrelation as measured by the Moran coefficient.

**stanfit** an object of class `stanfit` returned by `rstan::stan`

**data** a data frame containing the model data

- family** the user-provided or default family argument used to fit the model
- formula** The model formula provided by the user (not including ESF component)
- slx** The slx formula
- re** A list containing re, the random effects (varying intercepts) formula if provided, and Data a data frame with columns id, the grouping variable, and idx, the index values assigned to each group.
- priors** Prior specifications.
- x\_center** If covariates are centered internally (centerx = TRUE), then x\_center is a numeric vector of the values on which covariates were centered.
- ME** The ME data list, if one was provided by the user for measurement error models.
- spatial** NA, slot is maintained for use in geostan\_fit methods.

### Author(s)

Connor Donegan, <Connor.Donegan@UTDallas.edu>

### Source

Donegan, Connor and Chun, Yongwan and Griffith, Daniel A. (2021). Modeling community health with areal data: Bayesian inference with survey standard errors and spatial structure. *Int. J. Env. Res. and Public Health* 18 (13): 6856. DOI: 10.3390/ijerph18136856 Data and code: <https://github.com/ConnorDonegan/survey-HBM>.

Donegan, Connor (2021). Spatial conditional autoregressive models in Stan. *OSF Preprints*. doi:10.31219/osf.io/3ey65.

### Examples

```
data(sentencing)

sentencing$log_e <- log(sentencing$expected_sents)
fit.pois <- stan_glm(sents ~ offset(log_e),
                   re = ~ name,
                   family = poisson(),
                   data = sentencing,
                   chains = 2, iter = 800) # for speed only

# MCMC diagnostics plot: Rhat values should all be very near 1
rstan::stan_rhat(fit.pois$stanfit)

# effective sample size for all parameters and generated quantities
# (including residuals, predicted values, etc.)
rstan::stan_ess(fit.pois$stanfit)

# or for a particular parameter
rstan::stan_ess(fit.pois$stanfit, "alpha_re")

# Spatial autocorrelation/residual diagnostics
sp_diag(fit.pois, sentencing)
```

```
## Posterior predictive distribution
yrep <- posterior_predict(fit.pois, S = 65)
y <- sentencing$sents
plot(density(yrep[1,]))
for (i in 2:nrow(yrep)) lines(density(yrep[i,]), col = "gray30")
lines(density(sentencing$sents), col = "darkred", lwd = 2)
```

---

stan\_icar

*Intrinsic autoregressive models*


---

### Description

The intrinsic conditional auto-regressive (ICAR) model for spatial count data. Options include the BYM model, the BYM2 model, and a solo ICAR term.

### Usage

```
stan_icar(
  formula,
  slx,
  re,
  data,
  C,
  family = poisson(),
  type = c("icar", "bym", "bym2"),
  scale_factor = NULL,
  prior = NULL,
  ME = NULL,
  centerx = FALSE,
  censor_point,
  prior_only = FALSE,
  chains = 4,
  iter = 2000,
  refresh = 500,
  keep_all = FALSE,
  pars = NULL,
  control = NULL,
  ...
)
```

### Arguments

formula	A model formula, following the R <a href="#">formula</a> syntax. Binomial models can be specified by setting the left hand side of the equation to a data frame of successes and failures, as in <code>cbind(successes, failures) ~ x</code> .
slx	Formula to specify any spatially-lagged covariates. As in, <code>~ x1 + x2</code> (the intercept term will be removed internally). When setting priors for beta, remember to include priors for any SLX terms.

re	<p>To include a varying intercept (or "random effects") term, <code>alpha_re</code>, specify the grouping variable here using formula syntax, as in <code>~ ID</code>. Then, <code>alpha_re</code> is a vector of parameters added to the linear predictor of the model, and:</p> <pre>alpha_re ~ N(0, alpha_tau) alpha_tau ~ Student_t(d.f., location, scale).</pre> <p>Before using this term, read the <code>Details</code> section and the <code>type</code> argument. Specifically, if you use <code>type = bym</code>, then an observational-level <code>re</code> term is already included in the model. (Similar for <code>type = bym2</code>.)</p>
data	A data frame or an object coercible to a data frame by <code>as.data.frame</code> containing the model data.
C	Spatial connectivity matrix which will be used to construct an edge list for the ICAR model, and to calculate residual spatial autocorrelation as well as any user specified <code>slx</code> terms. It will automatically be row-standardized before calculating <code>slx</code> terms. <code>C</code> must be a binary symmetric $n \times n$ matrix.
family	The likelihood function for the outcome variable. Current options are <code>binomial(link = "logit")</code> and <code>poisson(link = "log")</code> .
type	Defaults to "icar" (partial pooling of neighboring observations through parameter <code>phi</code> ); specify "bym" to add a second parameter vector <code>theta</code> to perform partial pooling across all observations; specify "bym2" for the innovation introduced by Riebler et al. (2016). See <code>Details</code> for more information.
scale_factor	For the BYM2 model, optional. If missing, this will be set to a vector of ones. See <code>Details</code> .
prior	<p>A named list of parameters for prior distributions (see <a href="#">priors</a>):</p> <p><b>intercept</b> The intercept is assigned a Gaussian prior distribution (see <a href="#">normal</a>).</p> <p><b>beta</b> Regression coefficients are assigned Gaussian prior distributions. Variables must follow their order of appearance in the model formula. Note that if you also use <code>slx</code> terms (spatially lagged covariates), and you use custom priors for <code>beta</code>, then you have to provide priors for the <code>slx</code> terms. Since <code>slx</code> terms are <i>prepended</i> to the design matrix, the prior for the <code>slx</code> term will be listed first.</p> <p><b>sigma</b> For <code>family = gaussian()</code> and <code>family = student_t()</code> models, the scale parameter, <code>sigma</code>, is assigned a (half-) Student's t prior distribution. The half-Student's t prior for <code>sigma</code> is constrained to be positive.</p> <p><b>nu</b> <code>nu</code> is the degrees of freedom parameter in the Student's t likelihood (only used when <code>family = student_t()</code>). <code>nu</code> is assigned a gamma prior distribution. The default prior is <code>prior = list(nu = gamma(alpha = 3, beta = 0.2))</code>.</p> <p><b>tau</b> The scale parameter for random effects, or varying intercepts, terms. This scale parameter, <code>tau</code>, is assigned a half-Student's t prior. To set this, use, e.g., <code>prior = list(tau = student_t(df = 20, location = 0, scale = 20))</code>.</p>
ME	To model observational uncertainty (i.e. measurement or sampling error) in any or all of the covariates, provide a list of data as constructed by the <a href="#">prep_me_data</a> function.

centerx	To center predictors on their mean values, use <code>centerx = TRUE</code> . If the <code>ME</code> argument is used, the modeled covariate (i.e., latent variable), rather than the raw observations, will be centered. When using the <code>ME</code> argument, this is the recommended method for centering the covariates.
sensor_point	Integer value indicating the maximum censored value; this argument is for modeling censored (suppressed) outcome data, typically disease case counts or deaths. For example, the US Centers for Disease Control and Prevention censors (does not report) death counts that are nine or fewer, so if you're using CDC WONDER mortality data you could provide <code>sensor_point = 9</code> .
prior_only	Draw samples from the prior distributions of parameters only.
chains	Number of MCMC chains to estimate.
iter	Number of samples per chain. .
refresh	Stan will print the progress of the sampler every <code>refresh</code> number of samples; set <code>refresh=0</code> to silence this.
keep_all	If <code>keep_all = TRUE</code> then samples for all parameters in the Stan model will be kept; this is necessary if you want to do model comparison with Bayes factors and the <code>bridgesampling</code> package.
pars	Optional; specify any additional parameters you'd like stored from the Stan model.
control	A named list of parameters to control the sampler's behavior. See <a href="#">stan</a> for details.
...	Other arguments passed to <a href="#">sampling</a> . For multi-core processing, you can use <code>cores = parallel::detectCores()</code> , or run <code>options(mc.cores = parallel::detectCores())</code> first.

## Details

The Stan code for the ICAR component of the model and the `BYM2` option is from Morris et al. (2019) with adjustments to enable non-binary weights and disconnected graph structures (see Freni-Sterrantino (2018) and Donegan (2021)).

The exact specification depends on the `type` argument.

### 'icar':

For Poisson models for count data, `y`, the basic model specification (`type = "icar"`) is:

```
y ~ Poisson(exp(offset + mu + phi))
phi ~ ICAR(spatial_scale)
spatial_scale ~ Gaussian(0, 1)
```

where `mu` contains an intercept and potentially covariates. The spatial trend, `phi`, has a mean of zero and a single scale parameter, `spatial_scale`.

The ICAR prior model is a CAR model that has a spatial autocorrelation parameter `car_alpha` equal to 1 (see [stan\\_car](#)). Thus the ICAR prior places high probability on a smooth spatially (or temporally) varying mean. This is rarely sufficient to model the amount of variation present in social and health data.

**'bym':**

Often, an observational-level random effect term,  $\theta$ , is added to capture (heterogeneous or unstructured) deviations from  $\mu + \phi$ . The combined term is referred to as a convolution term:

```
convolution = phi + theta.
```

This is known as the BYM model (Besag et al. 1991), and can be specified using `type = "bym"`:

```
y ~ Poisson(exp(offset + mu + phi + theta))
phi ~ ICAR(spatial_scale)
theta ~ Gaussian(0, theta_scale)
spatial_scale ~ Gaussian(0, 1)
theta_scale ~ Gaussian(0, 1)
```

**'bym2':**

Riebler et al. (2016) introduce a variation on the BYM model (`type = "bym2"`). This specification combines  $\phi$  and  $\theta$  using a mixing parameter,  $\rho$ , that controls the proportion of the variation that is attributable to the spatially autocorrelated term,  $\phi$ , rather than the spatially unstructured term,  $\theta$ . The terms share a single scale parameter:

```
convolution = [sqrt(rho/scale_factor) * phi_tilde + sqrt(1 - rho) * theta_tilde] * spatial_scale.
phi_tilde ~ Gaussian(0, 1)
theta_tilde ~ Gaussian(0, 1)
spatial_scale ~ Gaussian(0, 1)
```

The two `_tilde` terms are standard normal deviates,  $\rho$  is restricted to values between zero and one, and `scale_factor` is a constant term provided by the user. By default, `scale_factor` is equal to one, so that it does nothing. Riebler et al. (2016) argue that the interpretation or meaning of the scale of the ICAR model depends on the graph structure,  $C$ . This implies that the same prior distribution assigned to the `spatial_scale` will differ in its implications if  $C$  is changed; in other words, the priors are not transportable across models, and models that use the same nominal prior actually have different priors assigned to `spatial_scale`.

Borrowing R code from Morris (2017) and following Freni-Sterrantino et al. (2018), the following R code can be used to create the `scale_factor` for the BYM2 model (note, this requires the INLA R package), given a spatial adjacency matrix,  $C$ :

```
## create a list of data for stan_icar
icar.data <- geostan::prep_icar_data(C)
## calculate scale_factor for each of k connected group of nodes
k <- icar.data$k
scale_factor <- vector(mode = "numeric", length = k)
for (j in 1:k) {
  g.idx <- which(icar.data$comp_id == j)
  if (length(g.idx) == 1) {
    scale_factor[j] <- 1
    next
  }
  Cg <- C[g.idx, g.idx]
  scale_factor[j] <- scale_c(Cg)
}
```



This code adjusts for 'islands' or areas with zero neighbors, and it also handles disconnected graph structures (see Donegan 2021). Following Freni-Sterrantino (2018), disconnected components of the graph structure are given their own intercept term; however, this value is added to  $\phi$  automatically inside the Stan model. Therefore, the user never needs to make any adjustments for this term. (If you want to avoid complications from a disconnected graph structure, see `stan_car`). Note, the code above requires the `scale_c` function; it has package dependencies that are not included in `geostan`. To use `scale_c`, you have to load the following R function:

```
#' compute scaling factor for adjacency matrix, accounting for differences in spatial connectivity
#
#' @param C connectivity matrix
#
#' @details
#
#' Requires the following packages:
#
#' library(Matrix)
#' library(INLA);
#' library(spdep)
#' library(igraph)
#
#' @source
#
#' Morris, Mitzi (2017). Spatial Models in Stan: Intrinsic Auto-Regressive Models for Areal Data. <ht
#
scale_c <- function(C) {
  geometric_mean <- function(x) exp(mean(log(x)))
  N = dim(C)[1]
  Q = Diagonal(N, rowSums(C)) - C
  Q_pert = Q + Diagonal(N) * max(diag(Q)) * sqrt(.Machine$double.eps)
  Q_inv = inla.qinv(Q_pert, constr=list(A = matrix(1,1,N),e=0))
  scaling_factor <- geometric_mean(Matrix::diag(Q_inv))
  return(scaling_factor)
}
```

### Spatially lagged covariates (SLX):

The `slx` argument is a convenience function for including SLX terms. For example,

```
stan_glm(y ~ x1 + x2, slx = ~ x1, ...)
```

is a shortcut for

```
stan_glm(y ~ I(W %*% x1) + x1 + x2, ...)
```

where  $W$  is a row-standardized spatial weights matrix (see [shape2mat](#)). SLX terms will always be *prepended* to the design matrix, as above, which is important to know when setting prior distributions for regression coefficients.

For measurement error (ME) models, the SLX argument is the only way to include spatially lagged covariates since the SLX term needs to be re-calculated on each iteration of the MCMC algorithm.

**Measurement error (ME) models:**

The ME models are designed for surveys with spatial sampling designs, such as the American Community Survey (ACS) estimates (Donegan et al. 2021; Donegan 2021). With estimates,  $x$ , and their standard errors,  $se$ , the ME models have one of the the following two specifications, depending on the user input:

```
x ~ Gauss(x_true, se)
x_true ~ MVGauss(mu, Sigma)
Sigma = (I - rho * C)^(-1) M * tau^2
mu ~ Gauss(0, 100)
tau ~ student_t(10, 0, 40)
rho ~ uniform(lower_bound, upper_bound)
```

where the covariance matrix,  $\Sigma$ , has the conditional autoregressive specification, and  $\tau$  is the scale parameter. For non-spatial ME models, the following is used instead:

```
x ~ Gauss(x_true, se)
x_true ~ student_t(df, mu, sigma)
df ~ gamma(3, 0.2)
mu ~ Gauss(0, 100)
sigma ~ student_t(10, 0, 40)
```

For strongly skewed variables, such census tract poverty rates, it can be advantageous to apply a logit transformation to  $x\_true$  before applying the CAR or Student t prior model. When the logit argument is used, the model becomes:

```
x ~ Gauss(x_true, se)
logit(x_true) ~ MVGauss(mu, Sigma)
```

and similar for the Student t model.

**Censored counts:**

Vital statistics systems and disease surveillance programs typically suppress case counts when they are smaller than a specific threshold value. In such cases, the observation of a censored count is not the same as a missing value; instead, you are informed that the value is an integer somewhere between zero and the threshold value. For Poisson models (`family = poisson()`), you can use the `sensor_point` argument to encode this information into your model.

Internally, `geostan` will keep the index values of each censored observation, and the index value of each of the fully observed outcome values. For all observed counts, the likelihood statement will be:

$$p(y_i | \text{data}, \text{model}) = \text{Poisson}(y_i | \text{fitted}_i),$$

as usual. For each censored count, the likelihood statement will equal the cumulative Poisson distribution function for values zero through the sensor point:

$$p(y_j | \text{data}, \text{model}) = \sum_{m=0}^{\text{sensor\_point}} \text{Poisson}(c_m | \text{fitted}_j),$$

For example, the US Centers for Disease Control and Prevention's CDC WONDER database censors all death counts between 0 and 9. To model CDC WONDER mortality data, you could provide `sensor_point = 9` and then the likelihood statement for censored counts would equal the summation of the Poisson probability mass function over each integer ranging from zero through 9 (inclusive), conditional on the fitted values (i.e., all model parameters). See Donegan (2021) for additional discussion, references, and Stan code.

**Value**

An object of class `geostan_fit` (a list) containing:

**summary** Summaries of the main parameters of interest; a data frame

**diagnostic** Widely Applicable Information Criteria (WAIC) with a measure of effective number of parameters (`eff_pars`) and mean log pointwise predictive density (`lpd`), and mean residual spatial autocorrelation as measured by the Moran coefficient.

**stanfit** an object of class `stanfit` returned by `rstan::stan`

**data** a data frame containing the model data

**edges** The edge list representing all unique sets of neighbors and the weight attached to each pair (i.e., their corresponding element in the connectivity matrix `C`)

**family** the user-provided or default family argument used to fit the model

**formula** The model formula provided by the user (not including ICAR component)

**slx** The `slx` formula

**re** A list with two name elements, `formula` and `Data`, containing the formula `re` and a data frame with columns `id` (the grouping variable) and `idx` (the index values assigned to each group).

**priors** Prior specifications.

**x\_center** If covariates are centered internally (`center_x = TRUE`), then `x_center` is a numeric vector of the values on which covariates were centered.

**spatial** A data frame with the name of the spatial parameter ("`phi`" if `type = "icar"` else "`convolution`") and method (`toupper(type)`).

**Author(s)**

Connor Donegan, <Connor.Donegan@UTDallas.edu>

**Source**

Besag, J. (1974). Spatial interaction and the statistical analysis of lattice systems. *Journal of the Royal Statistical Society: Series B (Methodological)*, 36(2), 192-225.

Besag, J., York, J., & Mollié, A. (1991). Bayesian image restoration, with two applications in spatial statistics. *Annals of the institute of statistical mathematics*, 43(1), 1-20.

Donegan, Connor. 2021. Flexible functions for ICAR, BYM, and BYM2 models in Stan. Code repository. <https://github.com/ConnorDonegan/Stan-IAR>

Donegan, Connor and Chun, Yongwan and Griffith, Daniel A. (2021). Modeling community health with areal data: Bayesian inference with survey standard errors and spatial structure. *Int. J. Env. Res. and Public Health* 18 (13): 6856. DOI: 10.3390/ijerph18136856 Data and code: <https://github.com/ConnorDonegan/survey-HBM>.

Donegan, Connor (2021). Spatial conditional autoregressive models in Stan. *OSF Preprints*. doi:10.31219/osf.io/3ey65.

Freni-Sterrantino, Anna, Massimo Ventrucci, and Håvard Rue. 2018. A Note on Intrinsic Conditional Autoregressive Models for Disconnected Graphs. *Spatial and Spatio-Temporal Epidemiology* 26: 25–34.

Morris, M., Wheeler-Martin, K., Simpson, D., Mooney, S. J., Gelman, A., & DiMaggio, C. (2019). Bayesian hierarchical spatial models: Implementing the Besag York Mollié model in stan. *Spatial and spatio-temporal epidemiology*, 31, 100301.

Riebler, A., Sorbye, S. H., Simpson, D., & Rue, H. (2016). An intuitive Bayesian spatial model for disease mapping that accounts for scaling. *Statistical Methods in Medical Research*, 25(4), 1145-1165.

### See Also

[shape2mat](#), [stan\\_car](#), [stan\\_esf](#), [stan\\_glm](#), [prep\\_icar\\_data](#)

### Examples

```
# for parallel processing of models:
#options(mc.cores = parallel::detectCores())
data(sentencing)
C <- shape2mat(sentencing, "B")
log_e <- log(sentencing$expected_sents)
fit.bym <- stan_icar(sents ~ offset(log_e),
                    family = poisson(),
                    data = sentencing,
                    type = "bym",
                    C = C,
                    chains = 2, iter = 800) # for speed only

# spatial diagnostics
sp_diag(fit.bym, sentencing)

# check effective sample size and convergence
library(rstan)
rstan::stan_ess(fit.bym$stanfit)
rstan::stan_rhat(fit.bym$stanfit)

# calculate log-standardized incidence ratios
# (observed/expected case counts)
library(ggplot2)
library(sf)

f <- fitted(fit.bym, rates = FALSE)$mean
SSR <- f / sentencing$expected_sents
log.SSR <- log( SSR, base = 2)

ggplot( st_as_sf(sentencing) ) +
  geom_sf(aes(fill = log.SSR)) +
  scale_fill_gradient2(
    low = "navy",
    high = "darkred"
  ) +
  labs(title = "Log-standardized sentencing ratios",
       subtitle = "log( Fitted/Expected), base 2") +
  theme_void() +
```

```

theme(
  legend.position = "bottom",
  legend.key.height = unit(0.35, "cm"),
  legend.key.width = unit(1.5, "cm")
)

```

---

waic

*Widely Applicable Information Criteria (WAIC)*


---

### Description

Widely Application Information Criteria (WAIC) for model comparison

### Usage

```
waic(fit, pointwise = FALSE, digits = 2)
```

### Arguments

<code>fit</code>	An <code>geostan_fit</code> object or any Stan model with a parameter named "log_lik", the pointwise log likelihood of the observations.
<code>pointwise</code>	Logical (defaults to FALSE), should a vector of values for each observation be returned?
<code>digits</code>	Round results to this many digits.

### Value

A vector of length 3 with WAIC, a rough measure of the effective number of parameters estimated by the model `Eff_pars`, and log predictive density `Lpd`. If `pointwise = TRUE`, results are returned in a `data.frame`.

### Source

Watanabe, S. (2010). Asymptotic equivalence of Bayes cross validation and widely application information criterion in singular learning theory. *Journal of Machine Learning Research* 11, 3571-3594.

### See Also

[waic\\_loo](#)

### Examples

```

data(georgia)
fit <- stan_glm(log(rate.male) ~ 1, data = georgia,
               chains = 2, iter = 800) # for speed only
waic(fit)

```

# Index

- \* **datasets**
  - georgia, [7](#)
  - sentencing, [35](#)
  
- [apple](#), [3](#), [13](#), [16](#), [17](#), [19](#), [20](#), [39](#), [41](#)
- as.array.geostan\_fit
  - (print.geostan\_fit), [27](#)
- as.data.frame.geostan\_fit
  - (print.geostan\_fit), [27](#)
- as.matrix.geostan\_fit
  - (print.geostan\_fit), [27](#)
- auto\_gaussian, [4](#)
  
- edges, [5](#), [25](#), [38](#)
- expected\_mc, [6](#)
  
- fitted.geostan\_fit (print.geostan\_fit),  
[27](#)
- formula, [42](#), [49](#), [56](#), [61](#)
  
- gamma (priors), [31](#)
- geom\_histogram, [17](#), [41](#)
- geom\_point, [19](#)
- geom\_pointrange, [41](#)
- georgia, [7](#)
- geostan (geostan-package), [3](#)
- geostan-package, [3](#)
- get\_shp, [8](#)
- gr, [9](#), [13](#), [16](#)
- grid.arrange, [41](#)
  
- hs (priors), [31](#)
  
- lg, [11](#), [13](#), [16](#)
- lisa, [4](#), [12](#), [16](#), [19](#), [39](#)
- loo, [69](#)
  
- make\_EV, [14](#), [50](#)
- mc, [4](#), [13](#), [14](#), [15](#), [17](#), [19](#), [39](#), [41](#)
- me\_diag, [16](#), [41](#)
- moran\_plot, [4](#), [13](#), [16](#), [17](#), [18](#), [39](#), [41](#)
  
- n\_eff, [20](#)
- normal, [43](#), [50](#), [56](#), [62](#)
- normal (priors), [31](#)
  
- plot.geostan\_fit (print.geostan\_fit), [27](#)
- poly2nb, [37](#)
- posterior\_predict, [21](#), [30](#)
- predict.geostan\_fit
  - (print.geostan\_fit), [27](#)
- prep\_car\_data, [22](#), [25](#), [26](#), [38](#), [43](#), [44](#)
- prep\_icar\_data, [5](#), [24](#), [38](#), [68](#)
- prep\_me\_data, [25](#), [43](#), [50](#), [57](#), [62](#)
- print.geostan\_fit, [27](#)
- priors, [26](#), [31](#), [43](#), [50](#), [56](#), [62](#)
  
- residuals.geostan\_fit, [41](#), [44](#)
- residuals.geostan\_fit
  - (print.geostan\_fit), [27](#)
- row\_standardize, [34](#)
  
- sampling, [44](#), [51](#), [57](#), [63](#)
- scale, [29](#)
- se\_log, [36](#)
- sentencing, [35](#)
- set.seed, [21](#)
- shape2mat, [4](#), [5](#), [9](#), [11](#), [12](#), [14](#), [15](#), [17](#), [25](#), [37](#),  
[39](#), [41](#), [43](#), [45](#), [49](#), [51](#), [52](#), [56](#), [58](#), [65](#),  
[68](#)
- sim\_sar, [4](#), [20](#), [38](#)
- sp\_diag, [17](#), [39](#)
- spatial, [44](#), [45](#)
- spatial (print.geostan\_fit), [27](#)
- spatial.geostan\_fit, [51](#)
- stan, [44](#), [51](#), [57](#), [63](#)
- stan\_car, [5](#), [21–23](#), [29](#), [30](#), [41](#), [42](#), [63](#), [65](#), [68](#)
- stan\_esf, [14](#), [30](#), [32](#), [37](#), [48](#), [68](#)
- stan\_glm, [30](#), [55](#), [68](#)
- stan\_icar, [5](#), [24](#), [25](#), [30](#), [61](#)
- student\_t (priors), [31](#)
  
- uniform (priors), [31](#)

waic, [69](#), [69](#)