# Package 'gnm' 

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Title Generalized Nonlinear Models

## Version 1.1-2

Description Functions to specify and fit generalized nonlinear models, including models with multiplicative interaction terms such as the UNIDIFF model from sociology and the AMMI model from crop science, and many others. Over-parameterized representations of models are used throughout; functions are provided for inference on estimable parameter combinations, as well as standard methods for diagnostics etc.

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```
gnm-package Generalized Nonlinear Models
```


## Description

Functions to specify, fit and evaluate generalized nonlinear models.

## Details

gnm provides functions to fit generalized nonlinear models by maximum likelihood. Such models extend the class of generalized linear models by allowing nonlinear terms in the predictor.

Some special cases are models with multiplicative interaction terms, such as the UNIDIFF and rowcolumn association models from sociology and the AMMI and GAMMI models from crop science; stereotype models for ordered categorical response, and diagonal reference models for dependence on a square two-way classification.
gnm is a major re-working of an earlier Xlisp-Stat package, "Llama". Over-parameterized representations of models are used throughout; functions are provided for inference on estimable parameter combinations, as well as standard methods for diagnostics etc.
The following documentation provides further information on the gnm package:
gnmOverview vignette("gnmOverview", package = "gnm")
NEWS file.show(system.file("NEWS", package = "gnm"))

## Author(s)

Heather Turner and David Firth
Maintainer: Heather Turner [ht@heatherturner.net](mailto:ht@heatherturner.net)

## References

http://www.warwick.ac.uk/go/gnm

## See Also

gnm for the model fitting function, with links to associated functions.

## Examples

```
demo(gnm)
```


## Description

Compute an analysis of deviance table for one or more generalized nonlinear models

## Usage

\#\# S3 method for class 'gnm'
anova(object, ..., dispersion $=$ NULL, test $=$ NULL)

## Arguments

object an object of class gnm
... additional objects of class gnm or glm
dispersion the dispersion parameter for the fitting family. By default it is derived from object
test (optional) a character string, (partially) matching one of "Chisq", "F", or "Cp". See stat.anova.

## Details

Specifying a single object gives a sequential analysis of deviance table for that fit. The rows of the table show the reduction in the residual deviance and the current residual deviance as each term in the formula is added in turn.
If more than one object is specified, the rows of the table show the residual deviance of the current model and the change in the residual deviance from the previous model. (This only makes statistical sense if the models are nested.) It is conventional to list the models from smallest to largest, but this is up to the user.

If test is specified, the table will include test statistics and/or $p$ values for the reduction in deviance. For models with known dispersion (e.g., binomial and Poisson fits) the chi-squared test is most appropriate, and for those with dispersion estimated by moments (e.g., 'gaussian', 'quasibinomial' and 'quasipoisson' fits) the F test is most appropriate. Mallows' Cp statistic is the residual deviance plus twice the estimate of $\sigma^{2}$ times the residual degrees of freedom, which is closely related to AIC (and a multiple of it if the dispersion is known).

## Value

An object of class "anova" inheriting from class "data.frame".

## Warning

The comparison between two or more models will only be valid if they are fitted to the same dataset. This may be a problem if there are missing values and R's default of na. action = na.omit is used; an error will be given in this case.

## Author(s)

Modification of anova.glm by the R Core Team. Adapted for "gnm" objects by Heather Turner.

## See Also

gnm, anova

## Examples

```
set.seed(1)
## Fit a uniform association model separating diagonal effects
Rscore <- scale(as.numeric(row(occupationalStatus)), scale = FALSE)
Cscore <- scale(as.numeric(col(occupationalStatus)), scale = FALSE)
Uniform <- glm(Freq ~ origin + destination + Diag(origin, destination) +
                                    Rscore:Cscore, family = poisson, data = occupationalStatus)
## Fit an association model with homogeneous row-column effects
RChomog <- gnm(Freq ~ origin + destination + Diag(origin, destination) +
                                    MultHomog(origin, destination), family = poisson,
                                    data = occupationalStatus)
## Fit an association model with separate row and column effects
RC <- gnm(Freq ~ origin + destination + Diag(origin, destination) +
            Mult(origin, destination), family = poisson,
            data = occupationalStatus)
anova(RC, test = "Chisq")
anova(Uniform, RChomog, RC, test = "Chisq")
```

asGnm

Coerce Linear Model to gnm Object

## Description

asGnm is a generic function which coerces objects of class "glm" or "lm" to an object of class "gnm".

## Usage

asGnm(object, ...)

## Arguments

object
an object of class "glm" or "lm".
additional arguments for method functions.

## Details

Components are added to or removed from object to produce an object of class "gnm". This can be useful in model building, see examples.

## Value

An object of class "gnm" - see gnm for full description.

## Author(s)

Heather Turner

## References

Vargas, M, Crossa, J, van Eeuwijk, F, Sayre, K D and Reynolds, M P (2001). Interpreting treatment by environment interaction in agronomy trials. Agronomy Journal 93, 949-960.

## See Also

gnm, glm, lm

## Examples

```
set.seed(1)
## Scale yields to reproduce analyses reported in Vargas et al (2001)
yield.scaled <- wheat$yield * sqrt(3/1000)
treatment <- interaction(wheat$tillage, wheat$summerCrop, wheat$manure,
            wheat$N, sep = "")
## Fit linear model
mainEffects <- lm(yield.scaled ~ year + treatment, data = wheat)
## Convert to gnm object to allow addition of Mult() term
svdStart <- residSVD(mainEffects, year, treatment, 3)
bilinear1 <- update(asGnm(mainEffects), . ~ . +
    Mult(year, treatment),
    start = c(coef(mainEffects), svdStart[,1]))
```

backPain Data on Back Pain Prognosis, from Anderson (1984)

## Description

Data from a study of patients suffering from back pain. Prognostic variables were recorded at presentation and progress was categorised three weeks after treatment.

## Usage

backPain

## Format

A data frame with 101 observations on the following 4 variables.
$\mathbf{x 1}$ length of previous attack.
$\mathbf{x} 2$ pain change.
x3 lordosis.
pain an ordered factor describing the progress of each patient with levels worse < same < slight.improvement < moderate.improvement < marked.improvement < complete.relief.

## Source

https://ideas.repec.org/c/boc/bocode/s419001.html

## References

Anderson, J. A. (1984) Regression and Ordered Categorical Variables. J. R. Statist. Soc. B, 46(1), 1-30.

## Examples

```
set.seed(1)
summary(backPain)
### Re-express as count data
backPainLong <- expandCategorical(backPain, "pain")
### Fit models described in Table 5 of Anderson (1984)
### Logistic family models
noRelationship <- gnm(count ~ pain, eliminate = id,
    family = "poisson", data = backPainLong)
## stereotype model
oneDimensional <- update(noRelationship,
    ~ . + Mult(pain, x1 + x2 + x3))
## multinomial logistic
threeDimensional <- update(noRelationship, ~ . + pain:(x1 + x2 + x3))
### Models to determine distinguishability in stereotype model
## constrain scale of category-specific multipliers
oneDimensional <- update(noRelationship,
    ~ . + Mult(pain, offset(x1) + x2 + x3))
## obtain identifiable contrasts & id possibly indistinguishable slopes
getContrasts(oneDimensional, pickCoef(oneDimensional, "[.]pain"))
## Not run:
## (this part not needed for package testing)
## fit simpler models and compare
.pain <- backPainLong$pain
```

```
    levels(.pain)[2:3] <- paste(levels(.pain)[2:3], collapse = " | ")
    fiveGroups <- update(noRelationship,
    ~ . + Mult(.pain, x1 + x2 + x3))
    levels(.pain)[4:5] <- paste(levels(.pain)[4:5], collapse = " | ")
    fourGroups <- update(fiveGroups)
    levels(.pain)[2:3] <- paste(levels(.pain)[2:3], collapse = " | ")
    threeGroups <- update(fourGroups)
    ### Grouped continuous model, aka proportional odds model
    library(MASS)
    sixCategories <- polr(pain ~ x1 + x2 + x3, data = backPain)
    ### Obtain number of parameters and log-likelihoods for equivalent
    ### multinomial models as presented in Anderson (1984)
    logLikMultinom <- function(model, size){
        object <- get(model)
        if (inherits(object, "gnm")) {
            l <- sum(object$y * log(object$fitted/size))
            c(nParameters = object$rank - nlevels(object$eliminate),
                logLikelihood = 1)
    }
    else
            c(nParameters = object$edf, logLikelihood = -deviance(object)/2)
}
size <- tapply(backPainLong$count, backPainLong$id, sum)[backPainLong$id]
models <- c("threeDimensional", "oneDimensional", "noRelationship",
                            "fiveGroups", "fourGroups", "threeGroups", "sixCategories")
t(sapply(models, logLikMultinom, size))
## End(Not run)
```

barley Jenkyn's Data on Leaf-blotch on Barley

## Description

Incidence of $R$. secalis on the leaves of ten varieties of barley grown at nine sites.

## Usage

barley

## Format

A data frame with 90 observations on the following 3 variables.
$\mathbf{y}$ the proportion of leaf affected (values in $[0,1]$ )
site a factor with 9 levels A to I
variety a factor with 10 levels $\mathrm{c}(1: 9$, " X ")

## Note

This dataset was used in Wedderburn's original paper (1974) on quasi-likelihood.

## Source

Originally in an unpublished Aberystwyth PhD thesis by J F Jenkyn.

## References

Gabriel, K R (1998). Generalised bilinear regression. Biometrika 85, 689-700.
McCullagh, P and Nelder, J A (1989) Generalized Linear Models (2nd ed). Chapman and Hall.
Wedderburn, R W M (1974). Quasilikelihood functions, generalized linear models and the GaussNewton method. Biometrika 61, 439-47.

## Examples

```
set.seed(1)
### Fit Wedderburn's logit model with variance proportional to [mu(1-mu)]^2
logitModel <- glm(y ~ site + variety, family = wedderburn, data = barley)
fit <- fitted(logitModel)
print(sum((barley$y - fit)^2 / (fit * (1-fit))^2))
## Agrees with the chi-squared value reported in McCullagh and Nelder
## (1989, p331), which differs slightly from Wedderburn's reported value.
### Fit the biplot model as in Gabriel (1998, p694)
biplotModel <- gnm(y ~ -1 + instances(Mult(site, variety), 2),
    family = wedderburn, data = barley)
barleySVD <- svd(matrix(biplotModel$predictors, 10, 9))
A <- sweep(barleySVD$v, 2, sqrt(barleySVD$d), "*")[, 1:2]
B <- sweep(barleySVD$u, 2, sqrt(barleySVD$d), "*")[, 1:2]
## These are essentially A and B as in Gabriel (1998, p694), from which
## the biplot is made by
plot(rbind(A, B), pch = c(levels(barley$site), levels(barley$variety)))
## Fit the double-additive model as in Gabriel (1998, p697)
variety.binary <- factor(match(barley$variety, c(2,3,6), nomatch = 0) > 0,
                            labels = c("rest", "2,3,6"))
doubleAdditive <- gnm(y ~ variety + Mult(site, variety.binary),
                            family = wedderburn, data = barley)
## It is unclear why Gabriel's chi-squared statistics differ slightly
## from the ones produced in these fits. Possibly Gabriel adjusted the
## data somehow prior to fitting?
```

barleyHeights Heights of Barley Plants

## Description

Average heights for 15 genotypes of barley recorded over 9 years.

## Usage

barleyHeights

## Format

A data frame with 135 observations on the following 3 variables.
height average height over 4 replicates (cm)
year a factor with 9 levels 1974 to 1982
genotype a factor with 15 levels $1: 15$

## Source

Aastveit, A. H. <br>\& Martens, H. (1986). ANOVA interactions interpreted by partial least squares regression. Biometrics, 42, 829-844.

## References

Chadoeuf, J <br>\& Denis, J B (1991). Asymptotic variances for the multiplicative interaction model. J. App. Stat. 18(3), 331-353.

## Examples

```
set.seed(1)
## Fit AMMI-1 model
barleyModel <- gnm(height ~ year + genotype + Mult(year, genotype),
    data = barleyHeights)
## Get row and column scores with se's
gamma <- getContrasts(barleyModel, pickCoef(barleyModel, "[.]y"),
        ref = "mean", scaleWeights = "unit")
delta <- getContrasts(barleyModel, pickCoef(barleyModel, "[.]g"),
        ref = "mean", scaleWeights = "unit")
## Corresponding CI's similar to Chadoeuf & Denis (1991) Table 8
## (allowing for change in sign)
gamma[[2]][,1] + (gamma[[2]][,2]) %o% c(-1.96, 1.96)
delta[[2]][,1] + (delta[[2]][,2]) %o% c(-1.96, 1.96)
## Multiplier of row and column scores
height <- matrix(scale(barleyHeights$height, scale = FALSE), 15, 9)
```

```
R <- height - outer(rowMeans(height), colMeans(height), "+")
svd(R)$d[1]
```

cautres Data on Class, Religion and Vote in France

## Description

A 4-way contingency table of vote by class by religion in four French elections

## Usage

cautres

## Format

A table of counts, with classifying factors vote (levels 1:2), class (levels 1:6) and religion (levels 1:4) and election (levels 1:4).

## Source

Bruno Cautres

## References

Cautres, B, Heath, A F and Firth, D (1998). Class, religion and vote in Britain and France. La Lettre de la Maison Francaise 8.

## Examples

```
set.seed(1)
## Fit a "double UNIDIFF" model with the religion-vote and class-vote
## interactions both modulated by nonnegative election-specific multipliers
doubleUnidiff <- gnm(Freq ~ election*vote + election*class*religion +
            Mult(Exp(election), religion:vote) +
            Mult(Exp(election), class:vote),
            family = poisson, data = cautres)
## Deviance should be 133.04
## Examine the multipliers of the class-vote log odds ratios
ofInterest(doubleUnidiff) <- pickCoef(doubleUnidiff, "class:vote[).]")
coef(doubleUnidiff)
## Coefficients of interest:
## Mult(Exp(.), class:vote).election1
## -0.38357138
## Mult(Exp(.), class:vote).election2
## 0.29816599
## Mult(Exp(.), class:vote).election3
## 0.06580307
```

```
## Mult(Exp(.), class:vote).election4
## -0.02174104
## Re-parameterize by setting Mult2.Factor1.election1 to zero
getContrasts(doubleUnidiff, ofInterest(doubleUnidiff))
## estimate SE
## Mult(Exp(.), class:vote).election1 0.0000000 0.0000000
## Mult(Exp(.), class:vote).election2 0.6817374 0.2401644
## Mult(Exp(.), class:vote).election3 0.4493745 0.2473521
## Mult(Exp(.), class:vote).election4 0.3618301 0.2534754
## quasiSE quasiVar
## Mult(Exp(.), class:vote).election1 0.22854401 0.052232363
## Mult(Exp(.), class:vote).election2 0.07395886 0.005469913
## Mult(Exp(.), class:vote).election3 0.09475938 0.008979340
## Mult(Exp(.), class:vote).election4 0.10934798 0.011956981
## Same thing but with election 4 as reference category:
getContrasts(doubleUnidiff, rev(ofInterest(doubleUnidiff)))
## estimate SE
## Mult(Exp(.), class:vote).election4 0.00000000 0.0000000
## Mult(Exp(.), class:vote).election3 0.08754436 0.1446833
## Mult(Exp(.), class:vote).election2 0.31990727 0.1320022
## Mult(Exp(.), class:vote).election1 -0.36183013 0. 2534754
## quasiSE quasiVar
## Mult(Exp(.), class:vote).election4 0.10934798 0.011956981
## Mult(Exp(.), class:vote).election3 0.09475938 0.008979340
## Mult(Exp(.), class:vote).election2 0.07395886 0.005469913
## Mult(Exp(.), class:vote).election1 0.22854401 0.052232363
```

checkEstimable Check Whether One or More Parameter Combinations in a gnm
Model are Identified

## Description

For each of a specified set of linear combinations of parameters from a gnm model, checks numerically whether the combination's estimate is invariant to re-parameterization of the model.

## Usage

```
checkEstimable(model, combMatrix = diag(length(coef(model))),
                        tolerance = NULL)
```


## Arguments

model a model object of class "gnm"
combMatrix numeric: either a vector of length the same as length(coef(model)), or a matrix with that number of rows. Coefficients of one or more linear combinations of the model's parameters.
tolerance numeric: a threshold value for detection of non-estimability. If NULL, the default value of the tol argument to rankMatrix is used.

## Value

A logical vector of length equal to the number of parameter combinations tested; NA where a parameter combination is identically zero.

## Author(s)

David Firth and Heather Turner

## References

Catchpole, E.A. and Morgan, B.J.T. (1997). Detecting parameter redundancy. Biometrika, 84, 187-196.

## See Also

gnm, se.gnm, getContrasts

## Examples

```
set.seed(1)
## Fit the "UNIDIFF" mobility model across education levels
unidiff <- gnm(Freq ~ educ*orig + educ*dest +
    Mult(Exp(educ), orig:dest), family = poisson,
    data = yaish, subset = (dest != 7))
## Check whether multiplier contrast educ4 - educ5 is estimable
ofInterest(unidiff) <- pickCoef(unidiff, "[.]educ")
mycontrast <- numeric(length(coef(unidiff)))
mycontrast[ofInterest(unidiff)[4:5]] <- c(1, -1)
checkEstimable(unidiff, mycontrast)
## should be TRUE
## Check whether multiplier educ4 itself is estimable
mycontrast[ofInterest(unidiff)[5]] <- 0
checkEstimable(unidiff, mycontrast)
## should be FALSE -- only *differences* are identified here
```

Compute Confidence Intervals of Parameters in a Generalized Nonlinear Model

## Description

Computes confidence intervals for one or more parameters in a generalized nonlinear model, based on the profiled deviance.

## Usage

```
\#\# S3 method for class 'gnm'
confint(object, parm = ofInterest(object), level = 0.95,
        trace = FALSE, ...)
    \#\# S3 method for class 'profile.gnm'
    confint(object, parm = names(object), level = 0.95, ...)
```


## Arguments

object an object of class "gnm" or "profile.gnm"
parm (optional) either a numeric vector of indices or a character vector of names, specifying the parameters for which confidence intervals are to be estimated. If parm is NULL, confidence intervals are found for all parameters.
level the confidence level required.
trace a logical value indicating whether profiling should be traced.
. . . arguments passed to or from other methods

## Details

These are methods for the generic function confint in the base package.
For "gnm" objects, profile.gnm is first called to profile the deviance over each parameter specified by parm, or over all parameters in the model if parm is NULL.

The method for "profile.gnm" objects is then called, which interpolates the deviance profiles to estimate the limits of the confidence interval for each parameter, see profile.gnm for more details.
If a "profile.gnm" object is passed directly to confint, parameters specified by parm must be a subset of the profiled parameters.

For unidentified parameters a confidence interval cannot be calculated and the limits will be returned as NA. If the deviance curve has an asymptote and a limit of the confidence interval cannot be reached, the limit will be returned as -Inf or Inf appropriately. If the range of the profile does not extend far enough to estimate a limit of the confidence interval, the limit will be returned as NA. In such cases, it may be desirable create a profile object directly, see profile.gnm for more details.

## Value

A matrix (or vector) with columns giving lower and upper confidence limits for each parameter. These will be labelled as (1-level)/2 and 1 - (1-level)/2 in \% (by default $2.5 \%$ and $97.5 \%$ ).

## Author(s)

Modification of MASS: : : confint.glm by W. N. Venables and B. D. Ripley. Adapted for "gnm" objects by Heather Turner.

## See Also

profile.gnm, gnm, confint.glm, profile.glm

## Examples

```
### Example in which profiling doesn't take too long
count <- with(voting, percentage/100 * total)
yvar <- cbind(count, voting$total - count)
classMobility <- gnm(yvar ~ -1 + Dref(origin, destination),
                constrain = "delta1", family = binomial,
                data = voting)
## profile diagonal effects
confint(classMobility, parm = 3:7, trace = TRUE)
## Not run:
### Profiling takes much longer here, but example more interesting!
unidiff <- gnm(Freq ~ educ*orig + educ*dest +
    Mult(Exp(educ), orig:dest),
    ofInterest = "[.]educ", constrain = "[.]educ1",
    family = poisson, data = yaish, subset = (dest != 7))
## Letting 'confint' compute profile
confint(unidiff, trace = TRUE)
## 2.5% 97.5 %
## Mult(Exp(.), orig:dest).educ1 NA NA
## Mult(Exp(.), orig:dest).educ2 -0.5978901 0.1022447
## Mult(Exp(.), orig:dest).educ3 -1.4836854 -0.2362378
## Mult(Exp(.), orig:dest).educ4 -2.5792398 -0.2953420
## Mult(Exp(.), orig:dest).educ5 -Inf -0.7007616
## Creating profile object first with user-specified stepsize
prof <- profile(unidiff, trace = TRUE, stepsize = 0.1)
confint(prof, ofInterest(unidiff)[2:5])
## 2.5 % 97.5 %
## Mult(Exp(.), orig:dest).educ2 -0.5978324 0.1022441
## Mult(Exp(.), orig:dest).educ3 -1.4834753 -0.2362138
## Mult(Exp(.), orig:dest).educ4 NA -0.2950790
## Mult(Exp(.), orig:dest).educ5 NA NA
## For 95% confidence interval, need to estimate parameters for which
## z = +/- 1.96. Profile has not gone far enough for last two parameters
range(prof[[4]]$z)
## -1.566601 2.408650
range(prof[[5]]$z)
## -0.5751376 1.1989487
## End(Not run)
```

Const

Specify a Constant in a "nonlin" Function Predictor

## Description

A symbolic wrapper to specify a constant in the predictor of a "nonlin" function.

## Usage

Const (const)

## Arguments

const a numeric value.

## Value

A call to rep used to create a variable representing the constant in the model frame.

## Note

Const may only be used in the predictor of a "nonlin" function. Use offset to specify a constant in the model formula.

## Author(s)

Heather Turner

## See Also

gnm, formula, offset

## Examples

```
## One way to fit the logistic function without conditional
## linearity as in ?nls
library(gnm)
set.seed(1)
DNase1 <- subset(DNase, Run == 1)
test <- gnm(density ~ -1 +
    Mult(1, Inv(Const(1) + Exp(Mult(1 + offset(-log(conc)),
                                    Inv(1))))),
    start = c(NA, 0, 1), data = DNase1, trace = TRUE)
coef(test)
```

Diag Equality of Two or More Factors

## Description

Converts two or more factors into a new factor whose value is 0 where the original factors are not all equal, and nonzero otherwise.

## Usage

Diag(..., binary = FALSE)

## Arguments

$$
\begin{array}{ll}
\ldots & \text { One or more factors } \\
\text { binary } & \text { Logical }
\end{array}
$$

## Details

Used mainly in regression models for data classified by two or more factors with the same levels. By default, operates on $k$-level factors to produce a new factor having $k+1$ levels; if binary = TRUE is specified, the result is a coarser binary variable equal to 1 where all of the input factors are equal and 0 otherwise.

If the original levels are identical the levels of the factor created in the binary = FALSE case will be in the same order, with "." added as the first level. Otherwise the levels of the new factor will be ". " followed by the sorted combined levels.

## Value

Either a factor (if binary $=$ FALSE) or a 0-1 numeric vector (if binary $=T R U E$ ).

## Author(s)

David Firth and Heather Turner

## See Also

Symm

## Examples

```
rowfac <- gl(4, 4, 16)
colfac <- gl(4, 1, 16)
diag4by4 <- Diag(rowfac, colfac)
matrix(Diag(rowfac, colfac, binary = TRUE), 4, 4)
```

Dref

Specify a Diagonal Reference Term in a gnm Model Formula

## Description

Dref is a function of class "nonlin" to specify a diagonal reference term in the formula argument to gnm.

## Usage

$$
\operatorname{Dref}(\ldots, \operatorname{delta}=\sim 1)
$$

## Arguments

.. a comma-separated list of two or more factors.
delta a formula with no left-hand-side specifying the model for each factor weight.

## Details

Dref specifies diagonal reference terms as introduced by Sobel $(1981,1985)$. Such terms comprise an additive component for each factor of the form

$$
w_{f} \gamma_{l}
$$

where $w_{f}$ is the weight for factor $f, \gamma_{l}$ is the diagonal effect for level $l$ and $l$ is the level of factor $f$ for the given data point.
The weights are constrained to be nonnegative and to sum to one as follows

$$
w_{f}=\frac{e^{\delta_{f}}}{\sum_{i} e^{\delta_{i}}}
$$

and the $\delta_{f}$ are modelled as specified by the delta argument (constant weights by default). The returned parameters are those in the model for $\delta_{f}$, rather than the implied weights $w_{f}$. The DrefWeights function will take a fitted gnm model and return the weights $w_{f}$, along with their standard errors.
If the factors passed to Dref do not have exactly the same levels, the set of levels in the diagonal reference term is taken to be the union of the factor levels, sorted into increasing order.

## Value

A list with the anticipated components of a "nonlin" function:

| predictors | the factors passed to Dref and the formulae for the weights. |
| :--- | :--- |
| common | an index to specify that common effects are to be estimated across the factors. |
| term | a function to create a deparsed mathematical expression of the term, given labels <br> for the predictors. |
| start | a function to generate starting values for the parameters. <br> call |
|  | the call to use as a prefix for parameter labels. |

## Author(s)

Heather Turner

## References

Sobel, M. E. (1981), Diagonal mobility models: A substantively motivated class of designs for the analysis of mobility effects. American Sociological Review 46, 893-906.
Sobel, M. E. (1985), Social mobility and fertility revisited: Some new models for the analysis of the mobility effects hypothesis. American Sociological Review 50, 699-712.
Clifford, P. and Heath, A. F. (1993) The Political Consequences of Social Mobility. J. Roy. Stat. Soc. A, 156(1), 51-61.

Van der Slik, F. W. P., De Graaf, N. D and Gerris, J. R. M. (2002) Conformity to Parental Rules: Asymmetric Influences of Father's and Mother's Levels of Education. European Sociological Review 18(4), 489 - 502.

## See Also

gnm, formula, nonlin.function

## Examples

```
### Examples from Clifford and Heath paper
### (Results differ slightly - possible transcription error in
### published data?)
set.seed(1)
## reconstruct counts voting Labour/non-Labour
count <- with(voting, percentage/100 * total)
yvar <- cbind(count, voting$total - count)
## fit diagonal reference model with constant weights
classMobility <- gnm(yvar ~ -1 + Dref(origin, destination),
    family = binomial, data = voting)
DrefWeights(classMobility)
## create factors indicating movement in and out of salariat (class 1)
upward <- with(voting, origin != 1 & destination == 1)
downward <- with(voting, origin == 1 & destination != 1)
## fit separate weights for the "socially mobile" groups
socialMobility <- gnm(yvar ~ -1 + Dref(origin, destination,
                                    delta = ~ 1 + downward + upward),
    family = binomial, data = voting)
DrefWeights(socialMobility)
## fit separate weights for downwardly mobile groups only
downwardMobility <- gnm(yvar ~ -1 + Dref(origin, destination,
                                    delta = ~ 1 + downward),
    family = binomial, data = voting)
DrefWeights(downwardMobility)
## Not run:
### Examples from Van der Slik paper
### For illustration only - data not publically available
### Using data in data.frame named 'conformity', with variables
### MCFM - mother's conformity score
### FCFF - father's conformity score
### MOPLM - a factor describing the mother's education with 7 levels
### FOPLF - a factor describing the father's education with 7 levels
### AGEM - mother's birth cohort
### MRMM - mother's traditional role model
### FRMF - father's traditional role model
### MWORK - mother's employment
### MFCM - mother's family conflict score
### FFCF - father's family conflict score
set.seed(1)
```

```
## Models for mothers' conformity score as specified in Figure 1
A <- gnm(MCFM ~ -1 + AGEM + MRMM + FRMF + MWORK + MFCM +
        Dref(MOPLM, FOPLF), family = gaussian, data = conformity,
        verbose = FALSE)
A
## Call:
## gnm(formula = MCFM ~ -1 + AGEM + MRMM + FRMF + MWORK + MFCM +
## Dref(MOPLM, FOPLF), family = gaussian, data = conformity,
        verbose = FALSE)
##
Coefficients:
## AGEM MRMM
## 0.06363 -0.32425
                                FRMF MWORK
        -0.25324 -0.06430
        MFCM Dref(MOPLM, FOPLF)delta1
        -0.06043 -0.33731
    Dref(MOPLM, FOPLF)delta2 Dref(., .).MOPLM|FOPLF1
        -0.02505 4.95121
    Dref(., .).MOPLM|FOPLF2 Dref(., .).MOPLM|FOPLF3
            4.86329 4.86458
    Dref(., .).MOPLM|FOPLF4 Dref(., .).MOPLM|FOPLF5
            4.72343 4.43516
    Dref(., .).MOPLM|FOPLF6 Dref(., .).MOPLM|FOPLF7
            4.18873 4.43378
    ##
    ## Deviance: 425.3389
## Pearson chi-squared: 425.3389
## Residual df: 576
## Weights as in Table 4
DrefWeights(A)
## Refitting with parameters of first Dref weight constrained to zero
## $MOPLM
## weight se
## 0.4225636 0.1439829
##
## $FOPLF
## weight se
## 0.5774364 0.1439829
F <- gnm(MCFM ~ -1 + AGEM + MRMM + FRMF + MWORK + MFCM +
                Dref(MOPLM, FOPLF, delta = ~1 + MFCM), family = gaussian,
        data = conformity, verbose = FALSE)
F
## Call:
## gnm(formula = MCFM ~ -1 + AGEM + MRMM + FRMF + MWORK + MFCM +
## Dref(MOPLM, FOPLF, delta = ~1 + MFCM), family = gaussian,
## data = conformity, verbose = FALSE)
##
##
## Coefficients:
##
 den

\section*{Description}

Intergenerational class mobility among the male populations of England and Wales; France, and Sweden.

\section*{Usage}
erikson

\section*{Format}

A table of counts, with classifying factors origin (father's class; levels I, II, III, IVa, IVb, IVc, V/VI, VIIa, VIIb) destination (son's class; levels as before), and country (son's country of residence; levels EW, F, S).

\section*{Source}

Hauser, R. M. (1984) Vertical Class Mobility in England, France and Sweden. Acta Sociol., 27(2), 87-110.

\section*{References}

Erikson, R., Goldthorpe, J. H. and Portocarero, L. (1982) Social Fluidity in Industrial Nations: England, France and Sweden. Brit. J. Sociol. 33(1), 1-34.
Xie, Y. (1992) The Log-multiplicative Layer Effect Model for Comparing Mobility Tables. Am. Sociol. Rev. 57(3), 380-395.

\section*{Examples}
```

set.seed(1)

### Collapse to 7 by 7 table as in Erikson (1982)

erikson <- as.data.frame(erikson)
lvl <- levels(erikson$origin)
levels(erikson$origin) <- levels(erikson\$destination) <-
c(rep(paste(lvl[1:2], collapse = " + "), 2), lvl[3],
rep(paste(lvl[4:5], collapse = " + "), 2), lvl[6:9])
erikson <- xtabs(Freq ~ origin + destination + country, data = erikson)

### Fit the models given in first half of Table 3 of Xie (1992)

## Null association between origin and destination

nullModel <- gnm(Freq ~ country*origin + country*destination,
family = poisson, data = erikson)

```
```

    ## Full interaction, common to all countries
    commonInteraction <- update(nullModel, ~ . + origin:destination)
    ## Full Interaction, different multiplier for each country
    multInteraction <- update(nullModel,
    ~ . + Mult(Exp(country), origin:destination))
    
### Create array of interaction levels as in Table 2 of Xie (1992)

levelMatrix <- matrix(c(2, 3, 4, 6, 5, 6, 6,
3, 3, 4, 6, 4, 5, 6,
4, 4, 2, 5, 5, 5, 5,
6, 6, 5, 1, 6, 5, 2,
4, 4, 5, 6, 3, 4, 5,
5, 4, 5, 5, 3, 3, 5,
6, 6, 5, 3, 5, 4, 1), 7, 7, byrow = TRUE)

### Fit models in second half of Table 3 in Xie (1992)

## Interaction specified by levelMatrix, common to all countries

commonTopo <- update(nullModel, ~ . +
Topo(origin, destination, spec = levelMatrix))

## Interaction specified by levelMatrix, different multiplier for

## each country

multTopo <- update(nullModel, ~ . +
Mult(Exp(country),
Topo(origin, destination, spec = levelMatrix)))

## Interaction specified by levelMatrix, different effects for

## each country

separateTopo <- update(nullModel, ~ . +
country:Topo(origin, destination,
spec = levelMatrix))

```
    exitInfo Print Exit Information for gnm Fit

\section*{Description}

A utility function to print information on final iteration in gnm fit, intended for use when gnm has not converged.

\section*{Usage}
exitInfo(object)

\section*{Arguments}
object
a gnm object.

\section*{Details}

If gnm has not converged within the pre-specified maximum number of iterations, it may be because the algorithm has converged to a non-solution of the likelihood equations. In order to determine appropriate action, it is necessary to differentiate this case from one of near-convergence to the solution.
exitInfo prints the absolute score and the corresponding convergence criterion for all parameters which failed to meet the convergence criterion at the last iteration. Clearly a small number of parameters with scores close to the criterion suggests near-convergence.

\section*{Author(s)}

Heather Turner

\section*{References}

Vargas, M, Crossa, J, van Eeuwijk, F, Sayre, K D and Reynolds, M P (2001). Interpreting treatment by environment interaction in agronomy trials. Agronomy Journal 93, 949-960.

\section*{See Also}
gnm

\section*{Examples}
```


## Fit a "double UNIDIFF" model with low iterMax for illustration!

set.seed(1)
doubleUnidiff <- gnm(Freq ~ election*vote + election*class*religion +
Mult(Exp(election), religion:vote) +
Mult(Exp(election), class:vote),
family = poisson, data = cautres, iterMax = 10)
exitInfo(doubleUnidiff)

```

Exp Specify the Exponential of a Predictor in a gnm Model Formula

\section*{Description}

A function of class "nonlin" to specify the exponential of a predictor in the formula argument to gnm.

\section*{Usage}

Exp(expression, inst \(=\) NULL)

\section*{Arguments}
expression a symbolic expression representing the (possibly nonlinear) predictor.
inst (optional) an integer specifying the instance number of the term.

\section*{Details}

The expression argument is interpreted as the right hand side of a formula in an object of class "formula", except that an intercept term is not added by default. Any function of class "nonlin" may be used in addition to the usual operators and functions.

\section*{Value}

A list with the components required of a "nonlin" function:
\begin{tabular}{ll} 
predictors & the expression argument passed to Exp \\
term & \begin{tabular}{l} 
a function to create a deparsed mathematical expression of the term, given a \\
label for the predictor.
\end{tabular} \\
call & the call to use as a prefix for parameter labels.
\end{tabular}

\section*{Author(s)}

Heather Turner and David Firth

\section*{See Also}
gnm, formula, nonlin.function

\section*{Examples}
```

set.seed(1)

## Using 'Mult' with 'Exp' to constrain the first constituent multiplier

## to be non-negative

## Fit the "UNIDIFF" mobility model across education levels

unidiff <- gnm(Freq ~ educ*orig + educ*dest +
Mult(Exp(educ), orig:dest),
family = poisson, data = yaish, subset = (dest != 7))

```

\section*{Description}

Expands the rows of a data frame by re-expressing observations of a categorical variable specified by catvar, such that the column(s) corresponding to catvar are replaced by a factor specifying the possible categories for each observation and a vector of \(0 / 1\) counts over these categories.

\section*{Usage}
expandCategorical(data, catvar, sep = ".", countvar = "count", idvar = "id", as.ordered = FALSE, group = TRUE)

\section*{Arguments}
\begin{tabular}{ll} 
data & a data frame. \\
catvar & \begin{tabular}{l} 
a character vector specifying factors in data whose interaction will form the \\
basis of the expansion.
\end{tabular} \\
sep & \begin{tabular}{l} 
a character string used to separate the concatenated values of catvar in the name \\
of the new interaction factor.
\end{tabular} \\
(optional) a character string to be used for the name of the new count variable. \\
idvar & \begin{tabular}{l} 
(optional) a character string to be used for the name of the new factor identifying \\
the original rows (cases).
\end{tabular} \\
as.ordered & \begin{tabular}{l} 
logical - whether the new interaction factor should be of class "ordered". \\
group
\end{tabular} \\
\begin{tabular}{l} 
logical: whether or not to group individuals with common values over all co- \\
variates.
\end{tabular}
\end{tabular}

\section*{Details}

Each row of the data frame is replicated \(c\) times, where \(c\) is the number of levels of the interaction of the factors specified by catvar. In the expanded data frame, the columns specified by catvar are replaced by a factor specifying the \(r\) possible categories for each case, named by the concatenated values of catvar separated by sep. The ordering of factor levels will be preserved in the creation of the new factor, but this factor will not be of class "ordered" unless the argument as.ordered \(=\) TRUE. A variable with name countvar is added to the data frame which is equal to 1 for the observed category in each case and 0 elsewhere. Finally a factor with name idvar is added to index the cases.

\section*{Value}

The expanded data frame as described in Details.

\section*{Note}

Re-expressing categorical data in this way allows a multinomial response to be modelled as a poisson response, see examples.

\section*{Author(s)}

Heather Turner

\section*{References}

Anderson, J. A. (1984) Regression and Ordered Categorical Variables. J. R. Statist. Soc. B, 46(1), 1-30.

\section*{See Also}
```

gnm, multinom, reshape

```

\section*{Examples}
```

    ### Example from help(multinom, package = "nnet")
    library(MASS)
    example(birthwt)
    library(nnet)
    bwt.mu <- multinom(low ~ ., data = bwt)
    ## Equivalent using gnm - include unestimable main effects in model so
    ## that interactions with low0 automatically set to zero, else could use
    ## 'constrain' argument.
    bwtLong <- expandCategorical(bwt, "low", group = FALSE)
    bwt.po <- gnm(count ~ low*(. - id), eliminate = id, data = bwtLong, family =
        "poisson")
    summary(bwt.po) # same deviance; df reflect extra id parameters
    ### Example from ?backPain
    set.seed(1)
    summary(backPain)
    backPainLong <- expandCategorical(backPain, "pain")
    ## Fit models described in Table 5 of Anderson (1984)
    noRelationship <- gnm(count ~ pain, eliminate = id,
    family = "poisson", data = backPainLong)
    oneDimensional <- update(noRelationship,
                            ~ . + Mult(pain, x1 + x2 + x3))
    ```
    friend \(\quad\) Occupation of Respondents and Their Closest Friend

\section*{Description}

Cross-classification of the occupation of respondent and that of their closest friend. Data taken from wave 10 (year 2000) of the British Household Panel Survey.

\section*{Usage}
friend

\section*{Format}

A table of counts, with classifying factors \(r\) (respondent's occupational category; levels \(1: 31\) ) and c (friend's occupational category; levels 1:31).

\section*{Source}

Chan, T.W. and Goldthorpe, J.H. (2004) Is there a status order in contemporary British society: Evidence from the occupational structure of friendship, European Sociological Review, 20, 383401.

\section*{Examples}
```

set.seed(1)

### Fit an association model with homogeneous row-column effects

rc1 <- gnm(Freq ~ r + c + Diag(r,c) + MultHomog(r, c),
family = poisson, data = friend)
rc1

## Not run:

### Extend to two-component interaction

rc2 <- update(rc1, . ~ . + MultHomog(r, c, inst = 2),
etastart = rc1\$predictors)
rc2
\#\# End(Not run)

```
getContrasts

Estimated Contrasts and Standard Errors for Parameters in a gnm Model

\section*{Description}

Computes contrasts or scaled contrasts for a set of (non-eliminated) parameters from a gnm model, and computes standard errors for the estimated contrasts. Where possible, quasi standard errors are also computed.

\section*{Usage}
getContrasts(model, set = NULL, ref = "first", scaleRef = "mean", scaleWeights \(=\) NULL, dispersion \(=\) NULL, check \(=\) TRUE, ...)

\section*{Arguments}
\begin{tabular}{ll} 
model & a model object of class "gnm". \\
set & \begin{tabular}{l} 
a vector of indices (numeric) or coefficient names (character). If NULL, a dialog \\
will open for parameter selection.
\end{tabular} \\
ref & \begin{tabular}{l} 
either a single numeric index, or a vector of real numbers which sum to 1, or \\
one of the character strings "first", "last" or "mean". \\
as for ref
\end{tabular} \\
scaleRef & \begin{tabular}{l} 
either NULL, a vector of real numbers, "unit" or "setLength". \\
scaleWeights \\
dispersion
\end{tabular} \\
either NULL, or a positive number by which the model's variance-covariance \\
matrix should be scaled.
\end{tabular}

\section*{Details}

The indices in set must all be in 1 :length (coef (object)). If set \(=\) NULL, a dialog is presented for the selection of indices (model coefficients).

For the set of coefficients selected, contrasts and their standard errors are computed. A check is performed first on the estimability of all such contrasts (if check \(=\) TRUE) or on a specified subset (if check is a numeric index vector). The specific contrasts to be computed are controlled by the choice of ref: this may be "first" (the default), for contrasts with the first of the selected coefficients, or "last" for contrasts with the last, or "mean" for contrasts with the arithmetic mean of the coefficients in the selected set; or it may be an arbitrary vector of weights (summing to 1 , not necessarily all non-negative) which specify a weighted mean against which contrasts are taken; or it may be a single index specifying one of the coefficients with which all contrasts should be taken. Thus, for example, ref \(=1\) is equivalent to ref = "first", and ref \(=c(1 / 3,1 / 3,1 / 3)\) is equivalent to ref \(=\) "mean" when there are three coefficients in the selected set.

The contrasts may be scaled by
\[
\frac{1}{\sqrt{\sum_{r} v_{r} * d_{r}^{2}}}
\]
where \(d_{r}\) is a contrast of the \(r\) 'th coefficient in set with the reference level specified by scaleRef and \(v\) is a vector of weights (of the same length as set) specified by scaleWeights. If scaleWeights is NULL (the default), scaleRef is ignored and no scaling is performed. Other options for scaleWeights are "unit" for weights equal to one and "setLength" for weights equal to the reciprocal of length (set). If scaleRef is the same as ref, these options constrain the sum of squared contrasts to 1 and length(set) respectively.

Quasi-variances (and corresponding quasi standard errors) are reported for unscaled contrasts where possible. These statistics are invariant to the choice of ref, see Firth (2003) or Firth and Menezes (2004) for more details.

\section*{Value}

An object of class qv - see qvcalc.

\section*{Author(s)}

David Firth and Heather Turner

\section*{References}

Firth, D (2003). Overcoming the reference category problem in the presentation of statistical models. Sociological Methodology 33, 1-18.

Firth, D and Menezes, R X de (2004). Quasi-variances. Biometrika 91, 65-80.

\section*{See Also}
```

gnm, se.gnm, checkEstimable, qvcalc, ofInterest

```

\section*{Examples}
```

    ### Unscaled contrasts ###
    set.seed(1)
    ## Fit the "UNIDIFF" mobility model across education levels -- see ?yaish
    unidiff <- gnm(Freq ~ educ*orig + educ*dest +
                Mult(Exp(educ), orig:dest),
                        ofInterest = "[.]educ", family = poisson,
                        data = yaish, subset = (dest != 7))
    
## Examine the education multipliers (differences on the log scale):

unidiffContrasts <- getContrasts(unidiff, ofInterest(unidiff))
plot(unidiffContrasts,
main = "Unidiff multipliers (log scale): intervals based on
quasi standard errors",
xlab = "Education level", levelNames = 1:5)
\#\#\# Scaled contrasts (elliptical contrasts) \#\#\#
set.seed(1)
\#\# Goodman Row-Column association model fits well (deviance 3.57, df 8)
mentalHealth$MHS <- C(mentalHealth$MHS, treatment)
mentalHealth$SES <- C(mentalHealth$SES, treatment)
RC1model <- gnm(count ~ SES + MHS + Mult(SES, MHS),
family = poisson, data = mentalHealth)
\#\# Row scores and column scores are both unnormalized in this
\#\# parameterization of the model
\#\# The scores can be normalized as in Agresti's eqn (9.15):
rowProbs <- with(mentalHealth, tapply(count, SES, sum) / sum(count))
colProbs <- with(mentalHealth, tapply(count, MHS, sum) / sum(count))
mu <- getContrasts(RC1model, pickCoef(RC1model, "[.]SES"),
ref = rowProbs, scaleRef = rowProbs,
scaleWeights = rowProbs)
nu <- getContrasts(RC1model, pickCoef(RC1model, "[.]MHS"),
ref = colProbs, scaleRef = colProbs,
scaleWeights = colProbs)
all.equal(sum(mu$qv[,1] * rowProbs), 0)
    all.equal(sum(nu$qv[,1] * colProbs), 0)
all.equal(sum(mu$qv[,1]^2 * rowProbs), 1)
    all.equal(sum(nu$qv[,1]^2 * colProbs), 1)

```

\section*{Description}
gnm fits generalised nonlinear models using an over-parameterized representation. Nonlinear terms are specified by calls to functions of class "nonlin".

\section*{Usage}
```

gnm(formula, eliminate = NULL, ofInterest = NULL, constrain = numeric(0),
constrainTo = numeric(length(constrain)), family = gaussian,
data = NULL, subset, weights, na.action, method = "gnmFit",
checkLinear = TRUE, offset, start = NULL, etastart = NULL,
mustart = NULL, tolerance = 1e-06, iterStart = 2, iterMax = 500,
trace = FALSE, verbose = TRUE, model = TRUE, x = TRUE,
termPredictors = FALSE, ridge = 1e-08, ...)

```

\section*{Arguments}
\begin{tabular}{ll} 
formula & a symbolic description of the nonlinear predictor. \\
eliminate & \begin{tabular}{l} 
a factor to be included as the first term in the model. gnm will exploit the struc- \\
ture of this factor to improve computational efficiency. See details.
\end{tabular} \\
of Interest & \begin{tabular}{l} 
optional coefficients of interest, specified by a regular expression, a numeric \\
vector of indices, a character vector of names, or "[?]" to select from a Tk dialog. \\
If NULL, it is assumed that all non-eliminated coefficients are of interest. \\
(non-eliminated) coefficients to constrain, specified by a regular expression, a \\
numeric vector of indices, a logical vector, a character vector of names, or "[?]" \\
to select from a Tk dialog.
\end{tabular} \\
constrain \\
constrainTo & \begin{tabular}{l} 
a numeric vector of the same length as constrain specifying the values to con- \\
strain to. By default constrained parameters will be set to zero.
\end{tabular} \\
family & \begin{tabular}{l} 
a specification of the error distribution and link function to be used in the model.
\end{tabular} \\
This can be a character string naming a family function; a family function, or \\
the result of a call to a family function. See family and wedderburn for possi- \\
bilities. \\
an optional data frame containing the variables in the model. If not found in \\
data, the variables are taken from environment (formula), typically the envi- \\
ronment from which gnm is called.
\end{tabular}
\begin{tabular}{ll} 
start & \begin{tabular}{l} 
a vector of starting values for the parameters in the model; if a starting value is \\
NA, the default starting value will be used. Starting values need not be specified \\
for eliminated parameters.
\end{tabular} \\
etastart & \begin{tabular}{l} 
starting values for the linear predictor. \\
mustart
\end{tabular} \\
starting values for the vector of means. \\
iterStart & \begin{tabular}{l} 
a positive numeric value specifying the tolerance level for convergence. \\
a positive integer specifying the number of start-up iterations to perform.
\end{tabular} \\
iterMax & \begin{tabular}{l} 
a positive integer specifying the maximum number of main iterations to perform. \\
a logical value indicating whether the deviance should be printed after each it- \\
eration.
\end{tabular} \\
verbose & \begin{tabular}{l} 
logical: if TRUE and model includes nonlinear terms, progress indicators are \\
printed as the model is fitted, including a diagnostic error message if the algo- \\
rithm fails. \\
logical: if TRUE the model frame is returned.
\end{tabular} \\
model & \begin{tabular}{l} 
logical: if TRUE the local design matrix from the last iteration is included as a \\
component of returned model object.
\end{tabular} \\
x & \begin{tabular}{l} 
logical: if TRUE, a matrix is returned with a column for each term in the model, \\
containing the additive contribution of that term to the predictor.
\end{tabular} \\
ridge & \begin{tabular}{l} 
numeric, a positive value for the ridge constant to be used in the fitting algorithm \\
further arguments passed to fitting function.
\end{tabular}
\end{tabular}

\section*{Details}

Models for gnm are specified by giving a symbolic description of the nonlinear predictor, of the form response \(\sim\) terms. The response is typically a numeric vector, see later in this section for alternatives. The usual symbolic language may be used to specify any linear terms, see formula for details.
Nonlinear terms may be specified by calls to functions of class "nonlin". There are several "nonlin" functions in the gnm package. Some of these specify simple mathematical functions of predictors: Exp, Mult, and Inv. Others specify more specialised nonlinear terms, in particular MultHomog specifies homogeneous multiplicative interactions and Dref specifies diagonal reference terms. Users may also define their own "nonlin" functions, see nonlin. function for details.
The eliminate argument may be used to specify a factor that is to be included as the first term in the model (since an intercept is then redundant, none is fitted). The structure of the factor is exploited to improve computational efficiency - substantially so if the eliminated factor has a large number of levels. Use of eliminate is designed for factors that are required in the model but are not of direct interest (e.g., terms needed to fit multinomial-response models as conditional Poisson models). See backPain for an example.
The of Interest argument may be used to specify coefficients of interest, the indices of which are returned in the of Interest component of the model object. print() displays of the model object or its components obtained using accessor functions such as coef() etc, will only show these coefficients. In addition methods for "gnm" objects which may be applied to a subset of the parameters are by default applied to the coefficients of interest. See ofInterest for accessor and replacement functions.

For contingency tables, the data may be provided as an object of class "table" from which the frequencies will be extracted to use as the response. In this case, the response should be specified as Freq in the model formula. The "predictors", "fitted.values", "residuals", "prior. weights", "weights", " \(y\) " and "offset" components of the returned gnm fit will be tables with the same format as the data, completed with NAs where necessary.
For binomial models, the response may be specified as a factor in which the first level denotes failure and all other levels denote success, as a two-column matrix with the columns giving the numbers of successes and failures, or as a vector of the proportions of successes.

The gnm fitting algorithm consists of two stages. In the start-up iterations, any nonlinear parameters that are not specified by either the start argument of gnm or a plug-in function are updated one parameter at a time, then the linear parameters are jointly updated before the next iteration. In the main iterations, all the parameters are jointly updated, until convergence is reached or the number or iterations reaches iterMax. To solve the (typically rank-deficient) least squares problem at the heart of the gnm fitting algorithm, the design matrix is standardized and regularized (in the Levenberg-Marquardt sense) prior to solving; the ridge argument provides a degree of control over the regularization performed (smaller values may sometimes give faster convergence but can lead to numerical instability).

Convergence is judged by comparing the squared components of the score vector with corresponding elements of the diagonal of the Fisher information matrix. If, for all components of the score vector, the ratio is less than tolerance^2, or the corresponding diagonal element of the Fisher information matrix is less than 1e-20, iterations cease. If the algorithm has not converged by iterMax iterations, exitInfo can be used to print information on the parameters which failed the convergence criteria at the last iteration.

By default, gnm uses an over-parameterized representation of the model that is being fitted. Only minimal identifiability constraints are imposed, so that in general a random parameterization is obtained. The parameter estimates are ordered so that those for any linear terms appear first.
getContrasts may be used to obtain estimates of specified scaled contrasts, if these contrasts are identifiable. For example, getContrasts may be used to estimate the contrasts between the first level of a factor and the rest, and obtain standard errors.

If appropriate constraints are known in advance, or have been determined from a gnm fit, the model may be (re-)fitted using the constrain argument to specify coefficients which should be set to values specified by constrainTo. Constraints should only be specified for non-eliminated parameters. update provides a convenient way of re-fitting a gnm model with new constraints.

\section*{Value}

If method = "gnmFit", gnm returns NULL if the algorithm has failed and an object of class "gnm" otherwise. A "gnm" object inherits first from "glm" then "lm" and is a list containing the following components:
call the matched call.
formula the formula supplied.
constrain a numeric vector specifying any coefficients that were constrained in the fitting process.
constrainTo a numeric vector of the same length as constrain specifying the values which constrained parameters were set to.
```

family the family object used.
prior.weights the case weights initially supplied.
terms the terms object used.
data the data argument.
na.action the na.action attribute of the model frame
xlevels a record of the levels of the factors used in fitting.
y the response used.
offset the offset vector used.
coefficients a named vector of non-eliminated coefficients, with an attribute "eliminated"
specifying the eliminated coefficients if eliminate is non-NULL.
eliminate the eliminate argument.
ofInterest a named numeric vector of indices corresponding to non-eliminated coefficients,
or NULL.
predictors the fitted values on the link scale.
fitted.values the fitted mean values, obtained by transforming the predictors by the inverse of
the link function.
deviance up to a constant, minus twice the maximised log-likelihood. Where sensible, the
constant is chosen so that a saturated model has deviance zero.
aic Akaike's An Information Criterion, minus twice the maximized log-likelihood
plus twice the number of parameters (so assuming that the dispersion is known).
iter the number of main iterations.
conv logical indicating whether the main iterations converged, with an attribute for
use by exitInfo if FALSE.
weights the working weights, that is, the weights used in the last iteration.
residuals the working residuals, that is, the residuals from the last iteration.
df.residual the residual degrees of freedom.
rank the numeric rank of the fitted model.

```

The list may also contain the components model, \(x\), or termPredictors if requested in the arguments to gnm.

If a table was passed to data and the default for na. action was not overridden, the list will also contain a table. attr component, for use by the extractor functions.
If a binomial gnm model is specified by giving a two-column response, the weights returned by prior.weights are the total numbers of cases (factored by the supplied case weights) and the component \(y\) of the result is the proportion of successes.
The function summary.gnm may be used to obtain and print a summary of the results, whilst plot.gnm may be used for model diagnostics.
The generic functions formula, family, terms, coefficients, fitted.values, deviance, extractAIC, weights, residuals, df.residual, model.frame, model.matrix, vcov and termPredictors maybe used to extract components from the object returned by gnm or to construct the relevant objects where necessary.

Note that the generic functions weights and residuals do not act as straight-forward accessor functions for gnm objects, but return the prior weights and deviance residuals respectively, as for glm objects.

\section*{Note}

Regular expression matching is performed using grep with default settings.

\section*{Author(s)}

Heather Turner and David Firth

\section*{References}

Cautres, B, Heath, A F and Firth, D (1998). Class, religion and vote in Britain and France. La Lettre de la Maison Francaise 8.

\section*{See Also}
formula for the symbolic language used to specify formulae.
Diag and Symm for specifying special types of interaction.
Exp, Mult, Inv, MultHomog, Dref and nonlin. function for incorporating nonlinear terms in the formula argument to gnm.
residuals.glm and the generic functions coef, fitted, etc. for extracting components from gnm objects.
exitInfo to print more information on last iteration when gnm has not converged.
getContrasts to estimate (identifiable) scaled contrasts from a gnm model.

\section*{Examples}
```


### Analysis of a 4-way contingency table

set.seed(1)
print(cautres)

## Fit a "double UNIDIFF" model with the religion-vote and class-vote

## interactions both modulated by nonnegative election-specific

## multipliers.

doubleUnidiff <- gnm(Freq ~ election:vote + election:class:religion
+ Mult(Exp(election), religion:vote) +
Mult(Exp(election), class:vote), family = poisson,
data = cautres)

```
```


## Examine the multipliers of the class-vote log odds ratios

```
## Examine the multipliers of the class-vote log odds ratios
ofInterest(doubleUnidiff) <- pickCoef(doubleUnidiff, "class:vote[).]")
ofInterest(doubleUnidiff) <- pickCoef(doubleUnidiff, "class:vote[).]")
coef(doubleUnidiff)
coef(doubleUnidiff)
## Coefficients of interest:
## Coefficients of interest:
## Mult(Exp(.), class:vote).election1
## Mult(Exp(.), class:vote).election1
## -0.38357138
## -0.38357138
## Mult(Exp(.), class:vote).election2
## Mult(Exp(.), class:vote).election2
## 0.29816599
## 0.29816599
## Mult(Exp(.), class:vote).election3
## Mult(Exp(.), class:vote).election3
## 0.06580307
## 0.06580307
## Mult(Exp(.), class:vote).election4
## Mult(Exp(.), class:vote).election4
## -0.02174104
```


## -0.02174104

```
```


## Re-parameterize by setting first multiplier to zero

getContrasts(doubleUnidiff, ofInterest(doubleUnidiff))

## estimate SE

## Mult(Exp(.), class:vote).election1 0.0000000 0.0000000

## Mult(Exp(.), class:vote).election2 0.6817374 0.2401644

## Mult(Exp(.), class:vote).election3 0.4493745 0.2473521

## Mult(Exp(.), class:vote).election4 0.3618301 0.2534754

## quasiSE quasiVar

## Mult(Exp(.), class:vote).election1 0.22854401 0.052232363

## Mult(Exp(.), class:vote).election2 0.07395886 0.005469913

## Mult(Exp(.), class:vote).election3 0.09475938 0.008979340

## Mult(Exp(.), class:vote).election4 0.10934798 0.011956981

## Same thing but with last multiplier as reference category:

getContrasts(doubleUnidiff, rev(ofInterest(doubleUnidiff)))

## estimate SE

## Mult(Exp(.), class:vote).election4 0.00000000 0.0000000

## Mult(Exp(.), class:vote).election3 0.08754436 0.1446833

## Mult(Exp(.), class:vote).election2 0.31990727 0.1320022

## Mult(Exp(.), class:vote).election1 -0.36183013 0.2534754

## quasiSE quasiVar

## Mult(Exp(.), class:vote).election4 0.10934798 0.011956981

## Mult(Exp(.), class:vote).election3 0.09475938 0.008979340

## Mult(Exp(.), class:vote).election2 0.07395886 0.005469913

## Mult(Exp(.), class:vote).election1 0.22854401 0.052232363

## Re-fit model with first multiplier set to zero

doubleUnidiffConstrained <-
update(doubleUnidiff, constrain = ofInterest(doubleUnidiff)[1])

## Examine the multipliers of the class-vote log odds ratios

coef(doubleUnidiffConstrained)[ofInterest(doubleUnidiff)]

## ...as using 'getContrasts' (to 4 d.p.).

```

\section*{Description}

The voting record of every representative in the 2001 House, on 20 roll calls selected by Americans for Democratic Action. Each row is the record of one representative; the first column records the representative's registered party allegiance.

\section*{Usage}

House2001

\section*{Format}

A data frame with 439 observations on the following 21 variables.
party a factor with levels D I N R
HR333. BankruptcyOverhaul. Yes a numeric vector
SJRes6.ErgonomicsRuleDisapproval.No a numeric vector
HR3. IncomeTaxReduction. No a numeric vector
HR6.MarriageTaxReduction. Yes a numeric vector
HR8.EstateTaxRelief.Yes a numeric vector
HR503. FetalProtection. No a numeric vector
HR1.SchoolVouchers.No a numeric vector
HR1836. TaxCutReconciliationBill. No a numeric vector
HR2356. CampaignFinanceReform. No a numeric vector
HJRes36.FlagDesecration. No a numeric vector
HR7.FaithBasedInitiative. Yes a numeric vector
HJRes50.ChinaNormalizedTradeRelations. Yes a numeric vector
HR4.ANWRDrillingBan. Yes a numeric vector
HR2563. PatientsRightsHMOLiability. No a numeric vector
HR2563. PatientsBillOfRights. No a numeric vector
HR2944. DomesticPartnerBenefits.No a numeric vector
HR2586.USMilitaryPersonnelOverseasAbortions.Yes a numeric vector
HR2975.AntiTerrorismAuthority. No a numeric vector
HR3090.EconomicStimulus. No a numeric vector
HR3000. TradePromotionAuthorityFastTrack. No a numeric vector

\section*{Details}

Coding of the votes is as described in ADA (2002).

\section*{Source}

Originally printed in ADA (2002). Kindly supplied in electronic format by Jan deLeeuw, who used the data to illustrate methods developed in deLeeuw (2006).

\section*{References}

Americans for Democratic Action, ADA (2002). 2001 voting record: Shattered promise of liberal progress. ADA Today 57(1), 1-17.
deLeeuw, J (2006). Principal component analysis of binary data by iterated singular value decomposition. Computational Statistics and Data Analysis 50, 21-39.

\section*{Examples}
```


## Not run:

## This example takes some time to run!

summary(House2001)

## Put the votes in a matrix, and discard members with too many NAs etc:

House2001m <- as.matrix(House2001[-1])
informative <- apply(House2001m, 1, function(row){
valid <- !is.na(row)
validSum <- if (any(valid)) sum(row[valid]) else 0
nValid <- sum(valid)
uninformative <- (validSum == nValid) || (validSum == 0) || (nValid < 10)
!uninformative})
House2001m <- House2001m[informative, ]

## Make a vector of colours, blue for Republican and red for Democrat:

parties <- House2001\$party[informative]
partyColors <- rep("black", length(parties))
partyColors <- ifelse(parties == "D", "red", partyColors)
partyColors <- ifelse(parties == "R", "blue", partyColors)

## Expand the data for statistical modelling:

House2001v <- as.vector(House2001m)
House2001f <- data.frame(member = rownames(House2001m),
party = parties,
rollCall = factor(rep((1:20),
rep(nrow(House2001m), 20))),
vote = House2001v)

## Now fit an "empty" model, in which all members vote identically:

baseModel <- glm(vote ~ -1 + rollCall, family = binomial, data = House2001f)

## From this, get starting values for a one-dimensional multiplicative term:

Start <- residSVD(baseModel, rollCall, member)

## 

## Now fit the logistic model with one multiplicative term.

## For the response variable, instead of vote=0,1 we use 0.03 and 0.97,

## corresponding approximately to a bias-reducing adjustment of p/(2n),

## where p is the number of parameters and n the number of observations.

## 

voteAdj <- 0.5 + 0.94*(House2001f\$vote - 0.5)
House2001model1 <- gnm(voteAdj ~ Mult(rollCall, member),
eliminate = rollCall,
family = binomial, data = House2001f,
na.action = na.exclude, trace = TRUE, tolerance = 1e-03,
start = -Start)

## Deviance is 2234.847, df = 5574

## 

## Plot the members' positions as estimated in the model:

## 

memberParameters <- pickCoef(House2001model1, "member")
plot(coef(House2001model1)[memberParameters], col = partyColors,
xlab = "Alphabetical index (Abercrombie 1 to Young 301)",
ylab = "Member's relative position, one-dimensional model")

## Can do the same thing with two dimensions, but gnm takes around 40

## slow iterations to converge (there are more than 600 parameters):

Start2 <- residSVD(baseModel, rollCall, member, d = 2)

```
```

    House2001model2 <- gnm(
            voteAdj ~ instances(Mult(rollCall - 1, member - 1), 2),
            eliminate = rollCall,
            family = binomial, data = House2001f,
            na.action = na.exclude, trace = TRUE, tolerance = 1e-03,
            start = Start2, lsMethod = "qr")
    
## Deviance is 1545.166, df = 5257

## 

memberParameters1 <- pickCoef(House2001model2, "1).member")
memberParameters2 <- pickCoef(House2001model2, "2).member")
plot(coef(House2001model2)[memberParameters1],
coef(House2001model2)[memberParameters2],
col = partyColors,
xlab = "Dimension 1",
ylab = "Dimension 2",
main = "House2001 data: Member positions, 2-dimensional model")

## 

## The second dimension is mainly due to rollCall 12, which does not

## correlate well with the rest -- look at the coefficients of

## House2001model1, or at the 12th row of

cormat <- cor(na.omit(House2001m))

## End(Not run)

```
instances Specify Multiple Instances of a Nonlinear Term in a gnm Model Formula

\section*{Description}

A symbolic wrapper, for use in the formula argument to gnm, to specify multiple instances of a term specified by a function with an inst argument.

\section*{Usage}
instances(term, instances = 1)

\section*{Arguments}
\begin{tabular}{ll} 
term & a call to a function with an inst argument, which specifies some term. \\
instances & the desired number of instances of the term.
\end{tabular}

\section*{Value}

A deparsed expression representing the summation of term specified with inst \(=1\), inst \(=2, \ldots\), inst = instances, which is used to create an expanded formula.

\section*{Author(s)}

Heather Turner

\section*{See Also}
gnm, formula, nonlin.function, Mult, MultHomog

\section*{Examples}
```


## Not run:

## (this example can take quite a while to run)

## 

## Fitting two instances of a multiplicative interaction (i.e. a

## two-component interaction)

yield.scaled <- wheat$yield * sqrt(3/1000)
treatment <- factor(paste(wheat$tillage, wheat$summerCrop, wheat$manure,
wheat\$N, sep = ""))
bilinear2 <- gnm(yield.scaled ~ year + treatment +
instances(Mult(year, treatment), 2),
family = gaussian, data = wheat)

## End(Not run)

```

Inv Specify the Reciprocal of a Predictor in a gnm Model Formula

\section*{Description}

A function of class "nonlin" to specify the reciprocal of a predictor in the formula argument to gnm.

\section*{Usage}

Inv(expression, inst = NULL)

\section*{Arguments}
expression a symbolic expression representing the (possibly nonlinear) predictor.
inst (optional) an integer specifying the instance number of the term.

\section*{Details}

The expression argument is interpreted as the right hand side of a formula in an object of class "formula", except that an intercept term is not added by default. Any function of class "nonlin" may be used in addition to the usual operators and functions.

\section*{Value}

A list with the components required of a "nonlin" function:
\begin{tabular}{ll} 
predictors & the expression argument passed to Inv \\
term & \begin{tabular}{l} 
a function to create a deparsed mathematical expression of the term, given a \\
label for the predictor.
\end{tabular} \\
call & the call to use as a prefix for parameter labels.
\end{tabular}

\section*{Author(s)}

Heather Turner

\section*{See Also}
gnm, formula, nonlin.function

\section*{Examples}
```


## One way to fit the logistic function without conditional

## linearity as in ?nls

library(gnm)
set.seed(1)
DNase1 <- subset(DNase, Run == 1)
test <- gnm(density ~ -1 +
Mult(1, Inv(Const(1) + Exp(Mult(1 + offset(-log(conc)),
Inv(1))))),
start = c(NA, 0, 1), data = DNase1, trace = TRUE)
coef(test)

```
meanResiduals

Average Residuals within Factor Levels

\section*{Description}

Computes the mean working residuals from a model fitted using Iterative Weighted Least Squares for each level of a factor or interaction of factors.

\section*{Usage}
meanResiduals(object, by, standardized=TRUE, as.table=TRUE, ...)

\section*{Arguments}
object model object for which object\$residuals gives the working residuals and object\$weights gives the working weights.
by either a formula specifying a factor or interaction of factors (recommended), or a list of factors (the elements of which must correspond exactly to observations in the model frame). When a list of factors is specified, their interaction is used to specify the grouping factor.
standardized logical: if TRUE, the mean residuals are standardized to be approximately standard normal.
as.table logical: logical: if TRUE and by specifies an interaction of factors, the result is returned as a table cross-classified by these factors.
... currently ignored

\section*{Details}

For level \(i\) of the grouping factor \(A\) the mean working residual is defined as
\[
\frac{r_{i j} * w_{i j}}{\sum_{j=1}^{n_{i}} w_{i j}}
\]
where \(r_{i j}\) is the \(j\) 'th residual for level \(i, w_{i j}\) is the corresponding working weight and \(n_{i}\) is the number of observations for level \(i\). The denominator gives the weight corresponding to mean residual.
For non-aggregated residuals, i.e. when the factor has one level per observation, the residuals are the same as Pearson residuals.

\section*{Value}

An object of class "meanResiduals", for which print and summary methods are provided. A "meanResiduals" object is a list containing the following elements:
call the call used to create the model object from which the mean residuals are derived.
by a label for the grouping factor.
residuals the mean residuals.
df the degrees of freedom associated with the mean residuals.
standardized the standardized argument.
weights the weights corresponding to the mean residuals.

\section*{Author(s)}

Heather Turner

\section*{Examples}
```


## Fit a conditional independence model, leaving out

## the uninformative subtable for dest == 7:

CImodel <- gnm(Freq ~ educ*orig + educ*dest, family = poisson,
data = yaish, subset = (dest != 7))

## compute mean residuals over origin and destination

meanRes <- meanResiduals(CImodel, ~ orig:dest)
meanRes
summary(meanRes)

## Not run:

## requires vcdExtra package

## display mean residuals for origin and destination

library(vcdExtra)
mosaic(CImodel, ~orig+dest)

## End(Not run)

## non-aggregated residuals

```
```

res1 <- meanResiduals(CImodel, ~ educ:orig:dest)
res2 <- residuals(CImodel, type = "pearson")
all.equal(as.numeric(res1), as.numeric(res2))

```
```

mentalHealth Data on Mental Health and Socioeconomic Status

```

\section*{Description}

A 2-way contingency table from a sample of residents of Manhattan. Classifying variables are child's mental impairment (MHS) and parents' socioeconomic status (SES).

\section*{Usage}
mentalHealth

\section*{Format}

A data frame with 24 observations on the following 3 variables.
count a numeric vector
SES an ordered factor with levels \(A<B<C<D<E<F\)
MHS an ordered factor with levels well < mild < moderate < impaired

\section*{Source}

From Agresti (2002, p381); originally in Srole et al. (1978, p289).

\section*{References}

Agresti, A. (2002). Categorical Data Analysis (2nd edn). New York: Wiley.
Srole, L, Langner, T. S., Michael, S. T., Opler, M. K. and Rennie, T. A. C. (1978), Mental Health in the Metropolis: The Midtown Manhattan Study. New York: NYU Press.

\section*{Examples}
```

set.seed(1)

## Goodman Row-Column association model fits well (deviance 3.57, df 8)

mentalHealth$MHS <- C(mentalHealth$MHS, treatment)
mentalHealth$SES <- C(mentalHealth$SES, treatment)
RC1model <- gnm(count ~ SES + MHS + Mult(SES, MHS),
family = poisson, data = mentalHealth)

## Row scores and column scores are both unnormalized in this

## parameterization of the model

## The scores can be normalized as in Agresti's eqn (9.15):

rowProbs <- with(mentalHealth, tapply(count, SES, sum) / sum(count))
colProbs <- with(mentalHealth, tapply(count, MHS, sum) / sum(count))

```
```

mu <- getContrasts(RC1model, pickCoef(RC1model, "[.]SES"),
ref = rowProbs, scaleRef = rowProbs,
scaleWeights = rowProbs)
nu <- getContrasts(RC1model, pickCoef(RC1model, "[.]MHS"),
ref = colProbs, scaleRef = colProbs,
scaleWeights = colProbs)
all.equal(sum(mu$qv[,1] * rowProbs), 0)
all.equal(sum(nu$qv[,1] * colProbs), 0)
all.equal(sum(mu$qv[,1]^2 * rowProbs), 1)
all.equal(sum(nu$qv[,1]^2 * colProbs), 1)

```
model.matrix.gnm Local Design Matrix for a Generalized Nonlinear Model

\section*{Description}

This method extracts or evaluates a local design matrix for a generalized nonlinear model

\section*{Usage}
\#\# S3 method for class 'gnm'
model.matrix(object, coef \(=\) NULL, ...)

\section*{Arguments}
object an object of class gnm.
coef if specified, the vector of (non-eliminated) coefficients at which the local design matrix is evaluated.
... further arguments.

\section*{Value}

If coef \(=\) NULL, the local design matrix with columns corresponding to the non-eliminated parameters evaluated at coef (object) (extracted from object if possible).
Otherwise, the local design matrix evaluated at coef.

\section*{Author(s)}

Heather Turner

\section*{See Also}
gnm, model.matrix

\section*{Examples}
```

example(mentalHealth)
model.matrix(RC1model)
model.matrix(RC1model, coef = seq(coef(RC1model)))

```
MPinv Moore-Penrose Pseudoinverse of a Real-valued Matrix

\section*{Description}

Computes the Moore-Penrose generalized inverse.

\section*{Usage}

MPinv(mat, tolerance = 100*.Machine\$double.eps, rank = NULL, method = "svd")

\section*{Arguments}
\(\begin{array}{ll}\text { mat } & \text { a real matrix. } \\ \text { tolerance } & \begin{array}{l}\text { A positive scalar which determines the tolerance for detecting zeroes among the } \\ \text { singular values. }\end{array} \\ \text { rank } & \begin{array}{l}\text { Either NULL, in which case the rank of mat is determined numerically; or an } \\ \text { integer specifying the rank of mat if it is known. No check is made on the } \\ \text { validity of any non-NULL value. }\end{array} \\ \text { method } & \begin{array}{l}\text { Character, one of "svd", "chol". The specification method }=" c h o l " ~ i s ~ v a l i d ~ \\ \text { only for symmetric matrices. }\end{array}\end{array}\)

\section*{Details}

Real-valuedness is not checked, neither is symmetry when method \(=\) "chol".

\section*{Value}

A matrix, with an additional attribute named "rank" containing the numerically determined rank of the matrix.

\section*{Author(s)}

David Firth and Heather Turner

\section*{References}

Harville, D. A. (1997). Matrix Algebra from a Statistician's Perspective. New York: Springer.
Courrieu, P. (2005). Fast computation of Moore-Penrose inverse matrices. Neural Information Processing 8, 25-29

\section*{See Also}
ginv

\section*{Examples}
```

A <- matrix(c(1, 1, 0,
1, 1, 0,
2, 3, 4), 3, 3)
B <- MPinv(A)
A %*% B %*% A - A \# essentially zero
B %*% A %*% B - B \# essentially zero
attr(B, "rank") \# here 2

## demonstration that "svd" and "chol" deliver essentially the same

## results for symmetric matrices:

A <- crossprod(A)
MPinv(A) - MPinv(A, method = "chol") \#\# (essentially zero)

```
\begin{tabular}{ll} 
MultHomog & \begin{tabular}{l} 
Specify a Multiplicative Interaction with Homogeneous Effects in a \\
gnm Model Formula
\end{tabular}
\end{tabular}

\section*{Description}

A function of class "nonlin" to specify a multiplicative interaction with homogeneous effects in the formula argument to gnm.

\section*{Usage}

MultHomog(..., inst = NULL)

\section*{Arguments}
... a comma-separated list of two or more factors.
inst (optional) an integer specifying the instance number of the term.

\section*{Details}

MultHomog specifies instances of a multiplicative interaction in which the constituent multipliers are the effects of two or more factors and the effects of these factors are constrained to be equal when the factor levels are equal. Thus the interaction effect would be
\[
\gamma_{i} \gamma_{j} \ldots
\]
for an observation with level \(i\) of the first factor, level \(j\) of the second factor and so on, where \(\gamma_{l}\) is the effect for level \(l\) of the homogeneous multiplicative factor.

If the factors passed to MultHomog do not have exactly the same levels, the set of levels is taken to be the union of the factor levels, sorted into increasing order.

\section*{Value}

A list with the anticipated components of a "nonlin" function:
\begin{tabular}{ll} 
predictors & the factors passed to MultHomog \\
common & an index to specify that common effects are to be estimated across the factors \\
term & \begin{tabular}{l} 
a function to create a deparsed mathematical expression of the term, given labels \\
for the predictors.
\end{tabular} \\
call & \begin{tabular}{l} 
the call to use as a prefix for parameter labels.
\end{tabular}
\end{tabular}

\section*{Note}

Currently, MultHomog can only be used to specify a one-dimensional interaction. See examples for a workaround to specify interactions with more than one dimension.

\section*{Author(s)}

Heather Turner

\section*{References}

Goodman, L. A. (1979) Simple Models for the Analysis of Association in Cross-Classifications having Ordered Categories. J. Am. Stat. Assoc., 74(367), 537-552.

\section*{See Also}
gnm, formula, instances, nonlin.function, Mult

\section*{Examples}
```

set.seed(1)

### Fit an association model with homogeneous row-column effects

rc1 <- gnm(Freq ~ r + c + Diag(r,c) + MultHomog(r, c),
family = poisson, data = friend)
rc1

## Not run:

### Extend to two-component interaction

rc2 <- update(rc1, . ~ . + MultHomog(r, c, inst = 2),
etastart = rc1\$predictors)
rc2

## End(Not run)

### For factors with a large number of levels, save time by

### setting diagonal elements to NA rather than fitting exactly;

### skipping start-up iterations may also save time

dat <- as.data.frame(friend)
id <- with(dat, r == c)
dat[id,] <- NA

```
```

rc2 <- gnm(Freq ~ r + c + instances(MultHomog(r, c), 2),
family = poisson, data = dat, iterStart = 0)

```
Multiplicative interaction
Specify a Product of Predictors in a gnm Model Formula

\section*{Description}

A function of class "nonlin" to specify a multiplicative interaction in the formula argument to gnm.

\section*{Usage}

Mult (..., inst \(=\) NULL)

\section*{Arguments}
... a comma-separated list of two or more symbolic expressions representing the constituent multipliers in the interaction.
inst a positive integer specifying the instance number of the term.

\section*{Details}

Mult specifies instances of a multiplicative interaction, i.e. a product of the form
\[
m_{1} m_{2} \ldots m_{n}
\]
where the constituent multipliers \(m_{1}, m_{2}, \ldots, m_{n}\) are linear or nonlinear predictors.
Models for the constituent multipliers are specified symbolically as unspecified arguments to Mult. These symbolic expressions are interpreted in the same way as the right hand side of a formula in an object of class "formula", except that an intercept term is not added by default. Offsets can be added to constituent multipliers, using offset.
The family of multiplicative interaction models include row-column association models for contingency tables (e.g., Agresti, 2002, Sec 9.6), log-multiplicative or UNIDIFF models (Erikson and Goldthorpe, 1992; Xie, 1992), and GAMMI models (van Eeuwijk, 1995).

\section*{Value}

A list with the required components of a "nonlin" function:
\begin{tabular}{ll} 
predictors & the expressions passed to Mult \\
term & \begin{tabular}{l} 
a function to create a deparsed mathematical expression of the term, given labels \\
for the predictors.
\end{tabular} \\
call & the call to use as a prefix for parameter labels.
\end{tabular}

\section*{Author(s)}

Heather Turner

\section*{References}

Agresti, A (2002). Categorical Data Analysis (2nd ed.) New York: Wiley.
Erikson, R and Goldthorpe, J H (1992). The Constant Flux. Oxford: Clarendon Press.
van Eeuwijk, F A (1995). Multiplicative interaction in generalized linear models. Biometrics 51, 1017-1032.

Vargas, M, Crossa, J, van Eeuwijk, F, Sayre, K D and Reynolds, M P (2001). Interpreting treatment by environment interaction in agronomy trials. Agronomy Journal 93, 949-960.

Xie, Y (1992). The log-multiplicative layer effect model for comparing mobility tables. American Sociological Review 57, 380-395.

\section*{See Also}
gnm, formula, instances, nonlin.function, MultHomog

\section*{Examples}
```

set.seed(1)

## Using 'Mult' with 'Exp' to constrain the first constituent multiplier

## to be non-negative

## Fit the "UNIDIFF" mobility model across education levels

unidiff <- gnm(Freq ~ educ*orig + educ*dest +
Mult(Exp(educ), orig:dest),
family = poisson, data = yaish, subset = (dest != 7))

## Not run:

## (this example can take quite a while to run)

## 

## Fitting two instances of a multiplicative interaction (i.e. a

## two-component interaction))

yield.scaled <- wheat$yield * sqrt(3/1000)
treatment <- factor(paste(wheat$tillage, wheat$summerCrop, wheat$manure,
wheat\$N, sep = ""))
bilinear2 <- gnm(yield.scaled ~ year + treatment +
instances(Mult(year, treatment), 2),
family = gaussian, data = wheat)
formula(bilinear2)

## yield.scaled ~ year + treatment + Mult(year, treatment, inst = 1) +

## Mult(year, treatment, inst = 2)

## End(Not run)

```

\section*{Description}

Nonlinear terms maybe be specified in the formula argument to gnm by a call to a function of class "nonlin". A "nonlin" function takes a list of arguments and returns a list of arguments for the internal nonlinTerms function.

\section*{Arguments}
\[
\begin{array}{ll}
\ldots & \begin{array}{l}
\text { arguments required to define the term, e.g. symbolic representations of predic- } \\
\text { tors in the term. }
\end{array} \\
\text { inst } & \begin{array}{l}
\text { (optional) an integer specifying the instance number of the term - for compati- } \\
\text { bility with instances. }
\end{array}
\end{array}
\]

\section*{Value}

The function should return a list with the following components:
\begin{tabular}{|c|c|}
\hline predictors & a list of symbolic expressions or formulae with no left hand side which represent (possibly nonlinear) predictors that form part of the term. Intercepts will be added by default to predictors specified by formulae. If predictors are named, these names will be used as a prefix for parameter labels or the parameter label itself in the single parameter case (in either case, prefixed by the call if supplied.) Predictors that may include an intercept should always be named or matched to a call. \\
\hline variables & an optional list of expressions representing variables in the term. \\
\hline term & a function which takes the arguments predLabels and varLabels, which are vectors of labels defined by gnm that correspond to the specified predictors and variables, and returns a deparsed mathematical expression of the full term. Only functions recognised by deriv should be used in the expression, e.g. + rather than sum. \\
\hline common & an optional numeric index of predictors with duplicated indices identifying single factor predictors for which homologous effects are to be estimated. \\
\hline call & an optional call to be used as a prefix for parameter labels, specified as an R expression. \\
\hline match & (if call is non-NULL) a numeric index of predictors specifying which arguments of call the predictors match to - zero indicating no match. If NULL, predictors will not be matched. It is recommended that matches are specified wherever possible, to ensure parameter labels are well-defined. Parameters in matched predictors are labelled using "dot-style" labelling, see examples. \\
\hline start & an optional function which takes a named vector of parameters corresponding to the predictors and returns a vector of starting values for those parameters. This function is ignored if the term is nested within another nonlinear term. \\
\hline
\end{tabular}

\section*{Author(s)}

Heather Turner

\section*{See Also}

Const to specify a constant, Dref to specify a diagonal reference term, Exp to specify the exponential of a predictor, Inv to specify the reciprocal of a predictor,
Mult to specify a multiplicative interaction, MultHomog to specify a homogeneous multiplicative interaction,

\section*{Examples}
```


### Equivalent of weighted.MM function in ?nls

weighted.MM <- function(resp, conc){
list(predictors = list(Vm = substitute(conc), K = 1),
variables = list(substitute(resp), substitute(conc)),
term = function(predictors, variables) {
pred <- paste("(", predictors[1], "/(", predictors[2],
" + ", variables[2], "))", sep = "")
pred <- paste("(", variables[1], " - ", pred, ")/sqrt(",
pred, ")", sep = "")
})
}
class(weighted.MM) <- "nonlin"

## use to fitted weighted Michaelis-Menten model

Treated <- Puromycin[Puromycin\$state == "treated", ]
Pur.wt.2 <- gnm( ~ -1 + weighted.MM(rate, conc), data = Treated,
start = c(Vm = 200, K = 0.1), verbose = FALSE)
Pur.wt.2

## 

## Call:

## gnm(formula = ~-1 + weighted.MM(rate, conc), data = Treated,

## start = c(Vm = 200, K = 0.1), verbose = FALSE)

## 

## Coefficients:

## Vm K

## 206.83477 0.05461

## 

## Deviance: 14.59690

## Pearson chi-squared: 14.59690

## Residual df: 10

### The definition of MultHomog

MultHomog <- function(..., inst = NULL){
dots <- match.call(expand.dots = FALSE)[["..."]]
list(predictors = dots,
common = rep(1, length(dots)),
term = function(predictors, ...) {
paste("(", paste(predictors, collapse = ")*("), ")", sep = "")
},

```
```

    call = as.expression(match.call()))
    }
class(MultHomog) <- "nonlin"

## use to fit homogeneous multiplicative interaction

set.seed(1)
RChomog <- gnm(Freq ~ origin + destination + Diag(origin, destination) +
MultHomog(origin, destination), ofInterest = "MultHomog",
family = poisson, data = occupationalStatus,
verbose = FALSE)
RChomog

## 

## Call:

## 

## gnm(formula = Freq ~ origin + destination + Diag(origin, destination) +

## MultHomog(origin, destination), ofInterest = "MultHomog", family = poisson,

## data = occupationalStatus, verbose = FALSE)

## 

## Coefficients of interest:

## MultHomog(origin, destination)1

## -1.50089

## MultHomog(origin, destination)2

## -1.28260

## MultHomog(origin, destination)3

## -0.68443

## MultHomog(origin, destination)4

## -0.10055

## MultHomog(origin, destination)5

## -0.08338

## MultHomog(origin, destination)6

## 0.42838

## MultHomog(origin, destination)7

## 0.84452

## MultHomog(., .).`origin|destination`8

## 1.08809

## 

## Deviance: 32.56098

## Pearson chi-squared: 31.20716

## Residual df: 34

## 

## the definition of Exp

Exp <- function(expression, inst = NULL){
list(predictors = list(substitute(expression)),
term = function(predictors, ...) {
paste("exp(", predictors, ")", sep = "")
},
call = as.expression(match.call()),
match = 1)
}
class(Exp) <- "nonlin"

## use to fit exponentional model

```
```

x <- 1:100
y <- exp(- x / 10)
set.seed(4)
exp1 <- gnm(y ~ Exp (1 + x), verbose = FALSE)
exp1

## 

## Call:

## gnm(formula = y ~ Exp (1 + x), verbose = FALSE)

## 

## Coefficients:

## (Intercept) Exp(. + x).(Intercept)

## Exp(1 + .).x

## -1.000e-01

## 

## Deviance: 9.342418e-20

## Pearson chi-squared: 9.342418e-20

## Residual df: 97

```
of Interest Coefficients of Interest in a Generalized Nonlinear Model

\section*{Description}

Retrieve or set the "ofInterest" component of a "gnm" (generalized nonlinear model) object.

\section*{Usage}
ofInterest(object)
ofInterest(object) <- value

\section*{Arguments}
object an object of class "gnm".
value a numeric vector of indices specifying the subset of (non-eliminated) coefficients of interest, or NULL to specify that all non-eliminated coefficients are of interest.

\section*{Details}

The "ofInterest" component of a "gnm" object is a named numeric vector of indices specifying a subset of the non-eliminated coefficients which are of specific interest.
If the "ofInterest" component is non-NULL, printed summaries of the model only show the coefficients of interest. In addition methods for "gnm" objects which may be applied to a subset of the parameters are by default applied to the coefficients of interest.

These functions provide a way of extracting and replacing the "ofInterest" component. The replacement function prints the replacement value to show which parameters have been specified by value.

\section*{Value}

A named vector of indices, or NULL.

\section*{Note}

Regular expression matching is performed using grep with default settings.

\section*{Author(s)}

Heather Turner

\section*{See Also}
grep, gnm, se.gnm, getContrasts,profile.gnm, confint.gnm

\section*{Examples}
```

set.seed(1)

## Fit the "UNIDIFF" mobility model across education levels

unidiff <- gnm(Freq ~ educ*orig + educ*dest +
Mult(Exp(educ), orig:dest),
ofInterest = "[.]educ", family = poisson,
data = yaish, subset = (dest != 7))
ofInterest(unidiff)

## Get all of the contrasts with educ1 in the UNIDIFF multipliers

getContrasts(unidiff, ofInterest(unidiff))

## Get estimate and se for the contrast between educ4 and educ5 in the

## UNIDIFF multiplier

mycontrast <- numeric(length(coef(unidiff)))
mycontrast[ofInterest(unidiff)[4:5]] <- c(1, -1)
se(unidiff, mycontrast)

```
parameters Extract Constrained and Estimated Parameters from a gnm Object

\section*{Description}

A function to extract non-eliminated parameters from a "gnm" object, including parameters that were constrained.

\section*{Usage}
parameters(object)

\section*{Arguments}
object an object of class "gnm".

\section*{Details}
parameters acts like coefficients except that for constrained parameters, the value at which the parameter was constrained is returned instead of NA.

\section*{Value}

A vector of parameters.

\section*{Author(s)}

Heather Turner

\section*{See Also}
```

coefficients, gnm

```

\section*{Examples}
```

RChomog <- gnm(Freq ~ origin + destination + Diag(origin, destination) +
MultHomog(origin, destination), family = poisson,
data = occupationalStatus, ofInterest = "MultHomog",
constrain = "MultHomog.*1")
coefficients(RChomog)
parameters(RChomog)

```
```

pickCoef Get Indices or Values of Selected Model Coefficients

```

\section*{Description}

Get the indices or values of a subset of non-eliminated coefficients selected via a Tk dialog or by pattern matching.

\section*{Usage}
pickCoef(object, pattern = NULL, value = FALSE, ...)

\section*{Arguments}
object
a model object.
pattern character string containing a regular expression or (with fixed \(=\) TRUE \()\) a pattern to be matched exactly. If NULL, a Tk dialog will open for coefficient selection.
value if FALSE, a named vector of indices, otherwise the value of the selected coefficients.
... arguments to pass on to pickFrom if pattern is missing, otherwise grep. In particular, fixed \(=\) TRUE specifies that pattern is a string to be matched as is.

\section*{Value}

If value \(=\) FALSE (the default), a named vector of indices, otherwise the values of the selected coefficients. If no coefficients are selected the returned value will be NULL.

\section*{Author(s)}

Heather Turner

\section*{See Also}
regexp, grep, pickFrom, ofInterest

\section*{Examples}
```

set.seed(1)

### Extract indices for use with ofInterest

## fit the "UNIDIFF" mobility model across education levels

unidiff <- gnm(Freq ~ educ*orig + educ*dest +
Mult(Exp(educ), orig:dest),
family = poisson, data = yaish, subset = (dest != 7))

## set coefficients in first constituent multiplier as 'ofInterest'

## using regular expression

ofInterest(unidiff) <- pickCoef(unidiff, "[.]educ")

## summarise model, only showing coefficients of interest

summary(unidiff)

## get contrasts of these coefficients

getContrasts(unidiff, ofInterest(unidiff))

### Extract coefficients to use as starting values

## fit diagonal reference model with constant weights

set.seed(1)

## reconstruct counts voting Labour/non-Labour

count <- with(voting, percentage/100 * total)
yvar <- cbind(count, voting\$total - count)
classMobility <- gnm(yvar ~ -1 + Dref(origin, destination),
family = binomial, data = voting)

## create factors indicating movement in and out of salariat (class 1)

upward <- with(voting, origin != 1 \& destination == 1)
downward <- with(voting, origin == 1 \& destination != 1)

## extract diagonal effects from first model to use as starting values

diagCoef <- pickCoef(classMobility, "Dref(., .)", fixed = TRUE,
value = TRUE)

```
```


## fit separate weights for the "socially mobile" groups

## -- there are now 3 parameters for each weight

socialMobility <- gnm(yvar ~ -1 + Dref(origin, destination,
delta = ~ 1 + downward + upward),
family = binomial, data = voting,
start = c(rep(NA, 6), diagCoef))

```
    plot.gnm Plot Diagnostics for a gnm Object

\section*{Description}

Five plots are available: a plot of residuals against fitted values, a Scale-Location plot of \(\sqrt{\mid \text { residuals } \mid}\) against fitted values, a Normal Q-Q plot, a plot of Cook's distances versus row labels, and a plot of residuals against leverages. By default, all except the fourth are produced.

\section*{Usage}
```


## S3 method for class 'gnm'

plot(x, which = c(1:3, 5), caption = c("Residuals vs Fitted",
"Normal Q-Q", "Scale-Location", "Cook's distance",
"Residuals vs Leverage"),
panel = if (add.smooth) panel.smooth else points,
sub.caption = NULL, main = "",
ask = prod(par("mfcol")) < length(which) \&\& dev.interactive(),
..., id.n = 3, labels.id = names(residuals(x)), cex.id = 0.75,
qqline = TRUE, cook.levels = c(0.5, 1),
add.smooth = getOption("add.smooth"), label.pos = c(4, 2),
cex.caption = 1)

```

\section*{Arguments}
x
which
caption
panel panel function. The useful alternative to points, panel.smooth can be chosen by add. smooth \(=\) TRUE.
sub.caption common title - above figures if there are multiple; used as sub (s.title) otherwise. If NULL, as by default, a possible shortened version of deparse ( \(x \$ c a l l\) ) is used.
main title to each plot - in addition to the above caption.
ask logical; if TRUE, the user is asked before each plot, see par (ask = .).
... other parameters to be passed through to plotting functions.
\begin{tabular}{ll} 
id.n & number of points to be labelled in each plot starting with the most extreme. \\
labels.id & \begin{tabular}{l} 
vector of labels, from which the labels for extreme points will be chosen. NULL \\
uses observation numbers.
\end{tabular} \\
cex.id & \begin{tabular}{l} 
magnification of point labels.
\end{tabular} \\
qqline & \begin{tabular}{l} 
logical indicating if a qqline() should be added to the normal Q-Q plot. \\
cook.levels \\
add.smooth
\end{tabular} \\
\begin{tabular}{l} 
levels of Cook's distance at which to draw contours. \\
logical indicating if a smoother should be added to most plots; see also panel \\
above.
\end{tabular} \\
label.pos & \begin{tabular}{l} 
positioning of labels, for the left half and right half of the graph respectively, for \\
plots 1-3. \\
cex.caption
\end{tabular} \\
controls the size of 'caption'.
\end{tabular}

\section*{Details}
sub.caption - by default the function call - is shown as a subtitle (under the x -axis title) on each plot when plots are on separate pages, or as a subtitle in the outer margin (if any) when there are multiple plots per page.
The "Scale-Location" plot, also called "Spread-Location" or "S-L" plot, takes the square root of the absolute residuals in order to diminish skewness \((\sqrt{|E|}\) is much less skewed than \(|E|\) for Gaussian zero-mean \(E\) ).

The S-L, the Q-Q, and the Residual-Leverage plot, use standardized residuals which have identical
 entries of the hat matrix, influence()\$hat, see also hat.
The Residual-Leverage plot shows contours of equal Cook's distance, for values of cook. levels (by default 0.5 and 1 ) and omits cases with leverage one. If the leverages are constant, as typically in a balanced aov situation, the plot uses factor level combinations instead of the leverages for the x -axis.

\section*{Author(s)}

Modification of plot. lm by the R Core Team. Adapted for "gnm" objects by Heather Turner.

\section*{See Also}
```

gnm, plot.lm

```

\section*{Examples}
```

set.seed(1)

## Fit an association model with homogeneous row-column effects

RChomog <- gnm(Freq ~ origin + destination + Diag(origin, destination) +
MultHomog(origin, destination), family = poisson,
data = occupationalStatus)

## Plot model diagnostics

plot(RChomog)

```
```


## Put 4 plots on 1 page; allow room for printing model formula in outer margin:

par(mfrow = c(2, 2), oma = c(0, 0, 3, 0))
title <- paste(deparse(RChomog\$formula, width.cutoff = 50), collapse = "\n")
plot(RChomog, sub.caption = title)

## Fit smoother curves

plot(RChomog, sub.caption = title, panel = panel.smooth)
plot(RChomog, sub.caption = title, panel = function(x,y) panel.smooth(x, y, span = 1))

```
predict.gnm Predict Method for Generalized Nonlinear Models

\section*{Description}

Obtains predictions and optionally estimates standard errors of those predictions from a fitted generalized nonlinear model object.

\section*{Usage}
\#\# S3 method for class 'gnm'
predict(object, newdata \(=\) NULL,
type = c("link", "response", "terms"), se.fit = FALSE, dispersion =
NULL, terms = NULL, na.action = na.exclude, ...)

\section*{Arguments}
\(\left.\begin{array}{ll}\text { object } & \text { a fitted object of class inheriting from "gnm". } \\ \text { newdata } \\ \text { optionally, a data frame in which to look for variables with which to predict. If } \\ \text { omitted, the fitted predictors are used. } \\ \text { the type of prediction required. The default is on the scale of the predictors; } \\ \text { the alternative "response" is on the scale of the response variable. Thus for } \\ \text { a default binomial model the default predictions are of log-odds (probabilities } \\ \text { on logit scale) and type = "response" gives the predicted probabilities. The } \\ \text { "terms" option returns a matrix giving the fitted values of each term in the } \\ \text { model formula on the predictor scale. }\end{array}\right]\) The value of this argument can be abbreviated.

\section*{Details}

If newdata is omitted the predictions are based on the data used for the fit. In that case how cases with missing values in the original fit is determined by the na.action argument of that fit. If na. action \(=\) na.omit omitted cases will not appear in the residuals, whereas if na. action \(=\) na.exclude they will appear (in predictions and standard errors), with residual value NA. See also napredict.

Value
If se = FALSE, a vector or matrix of predictions. If se \(=\) TRUE, a list with components
```

fit predictions.
se.fit estimated standard errors.
residual.scale
a scalar giving the square root of the dispersion used in computing the standard errors.

```

Note
Variables are first looked for in 'newdata' and then searched for in the usual way (which will include the environment of the formula used in the fit). A warning will be given if the variables found are not of the same length as those in 'newdata' if it was supplied.

\section*{Author(s)}

Heather Turner

\section*{References}

Chambers, J. M. and Hastie, T. J. (1992) Statistical Models in \(S\)

\section*{See Also}
gnm

\section*{Examples}
```

set.seed(1)

## Fit an association model with homogeneous row-column effects

RChomog <- gnm(Freq ~ origin + destination + Diag(origin, destination) +
MultHomog(origin, destination), family = poisson,
data = occupationalStatus)

## Fitted values (expected counts)

predict(RChomog, type = "response", se.fit = TRUE)

## Fitted values on log scale

predict(RChomog, type = "link", se.fit = TRUE)

```

\section*{Description}

For one or more parameters in a generalized nonlinear model, profile the deviance over a range of values about the fitted estimate.

\section*{Usage}
```

    ## S3 method for class 'gnm'
    ```
    profile(fitted, which \(=\) ofInterest(fitted), alpha \(=0.05\), maxsteps \(=10\),
            stepsize \(=\) NULL, trace \(=\) FALSE,.. )

\section*{Arguments}
fitted an object of class "gnm".
which (optional) either a numeric vector of indices or a character vector of names, specifying the parameters over which the deviance is to be profiled. If NULL, the deviance is profiled over all parameters.
alpha the significance level of the z statistic, indicating the range that the profile must cover (see details).
maxsteps the maximum number of steps to take either side of the fitted parameter.
stepsize (optional) a numeric vector of length two, specifying the size of steps to take when profiling down and up respectively, or a single number specifying the step size in both directions. If NULL, the step sizes will be determined automatically.
trace logical, indicating whether profiling should be traced.
... further arguments.

\section*{Details}

This is a method for the generic function profile in the base package.
For a given parameter, the deviance is profiled by constraining that parameter to certain values either side of its estimate in the fitted model and refitting the model.

For each updated model, the following " z statistic" is computed
\[
z(\theta)=(\theta-\hat{\theta}) * \sqrt{\frac{D_{\text {theta }}-D_{\text {thêta }}}{\delta}}
\]
where \(\theta\) is the constrained value of the parameter; \(\hat{\theta}\) is the original fitted value; \(D_{\theta}\) is the deviance when the parameter is equal to \(\theta\), and \(\delta\) is the dispersion parameter.
When the deviance is quadratic in \(\theta\), z will be linear in \(\theta\). Therefore departures from quadratic behaviour can easily be identified by plotting z against \(\theta\) using plot. profile.gnm.
confint.profile.gnm estimates confidence intervals for the parameters by interpolating the deviance profiles and identifying the parameter values at which \(z\) is equal to the relevant percentage
points of the normal distribution. The alpha argument to profile.gnm specifies the significance level of z which must be covered by the profile. In particular, the profiling in a given direction will stop when maxsteps is reached or two steps have been taken in which
\[
z(\theta)>(\theta-\hat{\theta}) * z_{(1-\alpha) / 2}
\]

By default, the stepsize is
\[
z_{(1-\alpha) / 2} * s_{\hat{\theta}}
\]
where \(s_{\hat{\theta}}\) is the standard error of \(\hat{\theta}\). Strong asymmetry is detected and the stepsize is adjusted accordingly, to try to ensure that the range determined by alpha is adequately covered. profile.gnm will also attempt to detect if the deviance is asymptotic such that the desired significance level cannot be reached. Each profile has an attribute "asymptote", a two-length logical vector specifying whether an asymptote has been detected in either direction.
For unidentified parameters the profile will be NA, as such parameters cannot be profiled.

\section*{Value}

A list of profiles, with one named component for each parameter profiled. Each profile is a data.frame: the first column, " \(z\) ", contains the \(z\) statistics and the second column "par.vals" contains a matrix of parameter values, with one column for each parameter in the model.
The list has two attributes: "original.fit" containing fitted and "summary" containing summary (fitted).

\section*{Author(s)}

Modification of profile.glm from the MASS package. Originally D. M. Bates and W. N. Venables, ported to R by B. D. Ripley, adapted for "gnm" objects by Heather Turner.

\section*{References}

Chambers, J. M. and Hastie, T. J. (1992) Statistical Models in S

\section*{See Also}
confint.gnm, gnm, profile.glm, ofInterest

\section*{Examples}
```

set.seed(1)

### Example in which deviance is near quadratic

count <- with(voting, percentage/100 * total)
yvar <- cbind(count, voting\$total - count)
classMobility <- gnm(yvar ~ -1 + Dref(origin, destination),
constrain = "delta1", family = binomial,
data = voting)
prof <- profile(classMobility, trace = TRUE)
plot(prof)

## confint similar to MLE +/- 1.96*s.e.

confint(prof, trace = TRUE)

```
```

coefData <- se(classMobility)
cbind(coefData[1] - 1.96 * coefData[2], coefData[1] + 1.96 * coefData[2])

## Not run:

### These examples take longer to run

### Another near quadratic example

RChomog <- gnm(Freq ~ origin + destination + Diag(origin, destination) +
MultHomog(origin, destination),
ofInterest = "MultHomog", constrain = "MultHomog.*1",
family = poisson, data = occupationalStatus)
prof <- profile(RChomog, trace = TRUE)
plot(prof)

## confint similar to MLE +/- 1.96*s.e.

confint(prof)
coefData <- se(RChomog)
cbind(coefData[1] - 1.96 * coefData[2], coefData[1] + 1.96 * coefData[2])

## Another near quadratic example, with more complex constraints

count <- with(voting, percentage/100 * total)
yvar <- cbind(count, voting\$total - count)
classMobility <- gnm(yvar ~ -1 + Dref(origin, destination),
family = binomial, data = voting)
wts <- prop.table(exp(coef(classMobility))[1:2])
classMobility <- update(classMobility, constrain = "delta1",
constrainTo = log(wts[1]))
sum(exp(parameters(classMobility))[1:2]) \#=1
prof <- profile(classMobility, trace = TRUE)
plot(prof)

## confint similar to MLE +/- 1.96*s.e.

confint(prof, trace = TRUE)
coefData <- se(classMobility)
cbind(coefData[1] - 1.96 * coefData[2], coefData[1] + 1.96 * coefData[2])

### An example showing asymptotic deviance

unidiff <- gnm(Freq ~ educ*orig + educ*dest +
Mult(Exp(educ), orig:dest),
ofInterest = "[.]educ", constrain = "[.]educ1",
family = poisson, data = yaish, subset = (dest != 7))
prof <- profile(unidiff, trace = TRUE)
plot(prof)

## clearly not quadratic for Mult1.Factor1.educ4 or Mult1.Factor1.educ5!

confint(prof)

## 2.5 % 97.5 %

## Mult(Exp(.), orig:dest).educ1 NA NA

## Mult(Exp(.), orig:dest).educ2 -0.5978901 0.1022447

## Mult(Exp(.), orig:dest).educ3 -1.4836854 -0.2362378

## Mult(Exp(.), orig:dest).educ4 -2.5792398 -0.2953420

## Mult(Exp(.), orig:dest).educ5 -Inf -0.7006889

coefData <- se(unidiff)
cbind(coefData[1] - 1.96 * coefData[2], coefData[1] + 1.96 * coefData[2])

### A far from quadratic example, also with eliminated parameters

backPainLong <- expandCategorical(backPain, "pain")

```
```

    oneDimensional <- gnm(count ~ pain + Mult(pain, x1 + x2 + x3),
        eliminate = id, family = "poisson",
        constrain = "[.](painworse|x1)", constrainTo = c(0, 1),
        data = backPainLong)
    prof <- profile(oneDimensional, trace = TRUE)
plot(prof)

## not quadratic for any non-eliminated parameter

confint(prof)
coefData <- se(oneDimensional)
cbind(coefData[1] - 1.96 * coefData[2], coefData[1] + 1.96 * coefData[2])

## End(Not run)

```
residSVD Multiplicative Approximation of Model Residuals

\section*{Description}

This function uses the first d components of the singular value decomposition in order to approximate a vector of model residuals by a sum of d multiplicative terms, with the multiplicative structure determined by two specified factors. It applies to models of class lm, glm or gnm.

\section*{Usage}
residSVD(model, fac1, fac2, \(d=1\) )

\section*{Arguments}
\begin{tabular}{ll} 
model & an object of class gnm, glm or lm \\
fac1 & a factor \\
fac2 & a factor \\
d & integer, the number of multiplicative terms to use in the approximation
\end{tabular}

\section*{Details}

This function operates on the matrix of mean residuals, with rows indexed by fac 1 and columns indexed by fac2. For glm and glm models, the matrix entries are weighted working residuals. The primary use of residSVD is to generate good starting values for the parameters in Mult terms in models to be fitted using gnm.

\section*{Value}

If \(d=1\), a numeric vector; otherwise a numeric matrix with \(d\) columns.

\section*{Author(s)}

David Firth and Heather Turner

\section*{See Also}
gnm, Mult

\section*{Examples}
```

set.seed(1)

## Goodman RC1 association model fits well (deviance 3.57, df 8)

mentalHealth$MHS <- C(mentalHealth$MHS, treatment)
mentalHealth$SES <- C(mentalHealth$SES, treatment)

## independence model

indep <- gnm(count ~ SES + MHS, family = poisson, data = mentalHealth)
mult1 <- residSVD(indep, SES, MHS)

## Now use mult1 as starting values for the RC1 association parameters

RC1model <- update(indep, . ~ . + Mult(SES, MHS),
start = c(coef(indep), mult1), trace = TRUE)

## Similarly for the RC2 model:

mult2 <- residSVD(indep, SES, MHS, d = 2)
RC2model <- update(indep, . ~ . + instances(Mult(SES, MHS), 2),
start = c(coef(indep), mult2), trace = TRUE)

## 

## See also example(House2001), where good starting values matter much more!

## 

```
se.gnm
Standard Errors of Linear Parameter Combinations in gnm Models

\section*{Description}

Computes approximate standard errors for (a selection of) individual parameters or one or more linear combinations of the parameters in a gnm (generalized nonlinear model) object. By default, a check is made first on the estimability of each specified combination.

\section*{Usage}
```


## S3 method for class 'gnm'

se(object, estimate = NULL, checkEstimability = TRUE,
Vcov = NULL, dispersion = NULL, ...)

```

\section*{Arguments}
object a model object of class "gnm".
estimate (optional) specifies parameters or linear combinations of parameters for which to find standard errors. In the first case either a character vector of names, a numeric vector of indices or "[?]" to select from a Tk dialog. In the second case coefficients given as a vector or the rows of a matrix, such that NROW (estimate) is equal to length (coef (object)). If NULL, standard errors are returned for all (non-eliminated) parameters in the model.
```

checkEstimability
logical: should the estimability of all specified combinations be checked?
Vcov either NULL, or a matrix
dispersion either NULL, or a positive number
... possible further arguments for checkEstimable.

```

\section*{Value}

A data frame with two columns:
Estimate The estimated parameter combinations
Std. Error Their estimated standard errors
If available, the column names of coefMatrix will be used to name the rows.

\section*{Note}

In the case where estimate is a numeric vector, se will assume that indices have been specified if all the values of estimate are in seq(length(coef(object)).
Where both Vcov and dispersion are supplied, the variance-covariance matrix of estimated model coefficients is taken to be Vcov * dispersion.

\section*{Author(s)}

David Firth and Heather Turner

\section*{See Also}
gnm, getContrasts, checkEstimable, ofInterest

\section*{Examples}
```

set.seed(1)

## Fit the "UNIDIFF" mobility model across education levels

unidiff <- gnm(Freq ~ educ*orig + educ*dest +
Mult(Exp(educ), orig:dest),
ofInterest = "[.]educ", family = poisson,
data = yaish, subset = (dest != 7))

## Deviance is 200.3

## Get estimate and se for the contrast between educ4 and educ5 in the

## UNIDIFF multiplier

mycontrast <- numeric(length(coef(unidiff)))
mycontrast[ofInterest(unidiff)[4:5]] <- c(1, -1)
se(unidiff, mycontrast)

## Get all of the contrasts with educ5 in the UNIDIFF multipliers

getContrasts(unidiff, rev(ofInterest(unidiff)))

```

\section*{Description}
summary method for objects of class "gnm"

\section*{Usage}
```

    ## S3 method for class 'gnm'
    summary(object, dispersion = NULL, correlation = FALSE,
                        symbolic.cor = FALSE, with.eliminate = FALSE, ...)
    ## S3 method for class 'summary.gnm'
    print(x, digits = max(3, getOption("digits") - 3),
        signif.stars = getOption("show.signif.stars"),
        symbolic.cor = x$symbolic.cor, ...)
    ```

\section*{Arguments}
object an object of class "gnm".
\(x \quad\) an object of class "summary.gnm".
dispersion the dispersion parameter for the fitting family. By default it is obtained from object.
correlation logical: if TRUE, the correlation matrix of the estimated parameters is returned.
digits the number of significant digits to use when printing.
symbolic.cor logical: if TRUE, the correlations are printed in a symbolic form rather than numbers (see symnum).
signif.stars logical. If TRUE, "significance stars" are printed for each coefficient.
with.eliminate Logical. If TRUE, any eliminated coefficients are included in the summary.
... further arguments passed to or from other methods.

\section*{Details}
print. summary.gnm prints the original call to gnm; a summary of the deviance residuals from the model fit; the coefficients of the model; the residual deviance; the Akaike's Information Criterion value, and the number of main iterations performed.
Standard errors, z-values and p-values are printed alongside the coefficients, with "significance stars" if signif. stars is TRUE.
When the "summary.gnm" object has a "correlation" component, the lower triangle of this matrix is also printed, to two decimal places (or symbolically); to see the full matrix of correlations print summary (object, correlation = TRUE) \$correlation directly.
The standard errors returned by summary.gnm are scaled by sqrt(dispersion). If the dispersion is not specified, it is taken as 1 for the binomial and Poisson families, and otherwise estimated by the residual Chi-squared statistic divided by the residual degrees of freedom. For coefficients that have been constrained or are not estimable, the standard error is returned as NA.

\section*{Value}
summary.gnm returns an object of class "summary.gnm", which is a list with components
\begin{tabular}{|c|c|}
\hline call & the "call" component from object. \\
\hline of Interest & the "ofInterest" component from object. \\
\hline family & the "family" component from object. \\
\hline deviance & the "deviance" component from object. \\
\hline aic & the "aic" component from object. \\
\hline df.residual & the "df.residual" component from object. \\
\hline iter & the "iter" component from object. \\
\hline \multicolumn{2}{|l|}{deviance. resid} \\
\hline & the deviance residuals, see residuals.glm. \\
\hline coefficients & the matrix of coefficients, standard errors, z -values and p-values. \\
\hline elim.coefs & if with.eliminate \(=\) TRUE a matrix of eliminated coefficients, standard errors, \(z\)-values and \(p\)-values. \\
\hline dispersion & either the supplied argument or the estimated dispersion if the latter is NULL. \\
\hline df & a 3-vector of the rank of the model; the number of residual degrees of freedom, and number of unconstrained coefficients. \\
\hline cov.scaled & the estimated covariance matrix scaled by dispersion (see vcov.gnm for more details). \\
\hline correlation & (only if correlation is TRUE) the estimated correlations of the estimated coefficients. \\
\hline symbolic.cor & (only if correlation is TRUE) the value of the argument symbolic.cor. \\
\hline
\end{tabular}

\section*{Note}

The gnm class includes generalized linear models, and it should be noted that summary. gnm differs from summary.glm in that it does not omit coefficients which are NA from the objects it returns. (Such coefficients are NA since they have been fixed at 0 either by use of the constrain argument to gnm or by a convention to handle linear aliasing).

\section*{Author(s)}

Modification of summary.glm by the R Core Team. Adapted for "gnm" objects by Heather Turner.

\section*{See Also}
gnm, summary

\section*{Examples}
```


### First example from ?Dref

set.seed(1)

## reconstruct counts voting Labour/non-Labour

count <- with(voting, percentage/100 * total)
yvar <- cbind(count, voting\$total - count)

## fit diagonal reference model with constant weights

classMobility <- gnm(yvar ~ -1 + Dref(origin, destination),
family = binomial, data = voting)

## summarize results - note diagonal weights are over-parameterised

summary(classMobility)

## refit setting first weight to zero (as DrefWeights() does)

classMobility <- gnm(yvar ~ -1 + Dref(origin, destination),
family = binomial, data = voting,
constrain = "delta1")
summary(classMobility)

```
Symm
Symmetric Interaction of Factors

\section*{Description}

Symm codes the symmetric interaction of factors having the same set of levels, for use in regression models of symmetry or quasi-symmetry.

\section*{Usage}

Symm(..., separator = ":")

\section*{Arguments}
... one or more factors.
separator a character string of length 1 or more, to be used in naming the levels of the resulting interaction factor.

\section*{Value}

A factor whose levels index the symmetric interaction of all factors supplied as input.

\section*{Author(s)}

David Firth and Heather Turner

\section*{See Also}

Diag

\section*{Examples}
```

    # square table
    rowfac <- gl(4, 4, 16)
    colfac <- gl(4, 1, 16)
    symm4by4 <- Symm(rowfac, colfac)
    matrix(symm4by4, 4, 4)
    # 3 x 3 x 3 table
    ind <- expand.grid(A = 1:3, B = 1:3, C = 1:3)
    symm3cubed <- with(ind, Symm(A, B, C))
    array(symm3cubed, c(3, 3, 3))
    ```
    termPredictors Extract Term Contributions to Predictor

\section*{Description}
termPredictors is a generic function which extracts the contribution of each term to the predictor from a fitted model object.

\section*{Usage}
termPredictors(object, ...)

\section*{Arguments}
\(\begin{array}{ll}\text { object } & \text { a fitted model object. } \\ \ldots & \text { additional arguments for method functions. }\end{array}\)

\section*{Details}

The default method assumes that the predictor is linear and calculates the contribution of each term from the model matrix and fitted coefficients. A method is also available for gnm objects.

\section*{Value}

A matrix with the additive components of the predictor in labelled columns.

\section*{Author(s)}

Heather Turner

\section*{See Also}
gnm

\section*{Examples}
```

    ## Linear model
    G <- gl(4, 6)
    x <- 1:24
    y <- rnorm(24, 0, 1)
    lmGx <- lm(y ~ G + x)
    contrib <- termPredictors(lmGx)
    contrib
    all.equal(as.numeric(rowSums(contrib)), as.numeric(lmGx$fitted)) #TRUE
    ## Generalized linear model
    y <- cbind(rbinom(24, 10, 0.5), rep(10, 24))
    glmGx <- glm(y ~ G + x, family = binomial)
    contrib <- termPredictors(glmGx)
    contrib
    all.equal(as.numeric(rowSums(contrib)),
        as.numeric(glmGx$linear.predictors)) #TRUE
    ## Generalized nonlinear model
    A <- gl(4, 6)
    B <- gl(6, 1, 24)
    y <- cbind(rbinom(24, 10, 0.5), rep(10, 24))
    set.seed(1)
    gnmAB <- gnm(y ~ A + B + Mult(A, B), family = binomial)
    contrib <- termPredictors(gnmAB)
    contrib
    all.equal(as.numeric(rowSums(contrib)),
        as.numeric(gnmAB$predictors)) #TRUE
    ```
    Topo Topological Interaction of Factors

\section*{Description}

Given two or more factors Topo creates an interaction factor as specified by an array of levels, which may be arbitrarily structured.

\section*{Usage}

Topo(..., spec \(=\) NULL)

\section*{Arguments}
.. two or more factors
spec an array of levels, with dimensions corresponding to the number of levels of each factor in the interaction

\section*{Value}

A factor of levels extracted from the levels array given in spec, using the given factors as index variables.

\section*{Author(s)}

David Firth

\section*{References}

Erikson, R., Goldthorpe, J. H. and Portocarero, L. (1982) Social Fluidity in Industrial Nations: England, France and Sweden. Brit. J. Sociol. 33(1), 1-34.
Xie, Y. (1992) The Log-multiplicative Layer Effect Model for Comparing Mobility Tables. Am. Sociol. Rev. 57(3), 380-395.

\section*{See Also}

Symm and Diag for special cases

\section*{Examples}
```

set.seed(1)

### Collapse to 7 by 7 table as in Erikson (1982)

erikson <- as.data.frame(erikson)
lvl <- levels(erikson$origin)
levels(erikson$origin) <- levels(erikson\$destination) <-
c(rep(paste(lvl[1:2], collapse = " + "), 2), lvl[3],
rep(paste(lvl[4:5], collapse = " + "), 2), lvl[6:9])
erikson <- xtabs(Freq ~ origin + destination + country, data = erikson)

### Create array of interaction levels as in Table 2 of Xie (1992)

levelMatrix <- matrix(c(2, 3, 4, 6, 5, 6, 6,
3, 3, 4, 6, 4, 5, 6,
4, 4, 2, 5, 5, 5, 5,
6, 6, 5, 1, 6, 5, 2,
4, 4, 5, 6, 3, 4, 5,
5, 4, 5, 5, 3, 3, 5,
6, 6, 5, 3, 5, 4, 1), 7, 7, byrow = TRUE)

```
\#\#\# Fit the levels models given in Table 3 of Xie (1992)
\#\# Null association between origin and destination
nullModel <- gnm(Freq ~ country:origin + country:destination, family = poisson, data = erikson)
\#\# Interaction specified by levelMatrix, common to all countries
commonTopo <- update(nullModel, ~ . +
Topo(origin, destination, spec = levelMatrix))
```


## Interaction specified by levelMatrix, different multiplier for

## each country

multTopo <- update(nullModel, ~ . +
Mult(Exp(country),
Topo(origin, destination, spec = levelMatrix)))

## Interaction specified by levelMatrix, different effects for

## each country

separateTopo <- update(nullModel, ~ . +
country:Topo(origin, destination,
spec = levelMatrix))

```
vcov.gnm

Variance-covariance Matrix for Parameters in a Generalized Nonlinear Model

\section*{Description}

This method extracts or computes a variance-covariance matrix for use in approximate inference on estimable parameter combinations in a generalized nonlinear model.

\section*{Usage}
\#\# S3 method for class 'gnm'
vcov(object, dispersion \(=\) NULL, with.eliminate \(=\) FALSE, ...)

\section*{Arguments}
object a model object of class gnm.
dispersion the dispersion parameter for the fitting family. By default it is obtained from object.
with. eliminate logical; should parts of the variance-covariance matrix corresponding to eliminated coefficients be computed?
.. as for vcov.

\section*{Details}

The resultant matrix does not itself necessarily contain variances and covariances, since gnm typically works with over-parameterized model representations in which parameters are not all identified. Rather, the resultant matrix is to be used as the kernel of quadratic forms which are the variances or covariances for estimable parameter combinations.

The matrix values are scaled by dispersion. If the dispersion is not specified, it is taken as 1 for the binomial and Poisson families, and otherwise estimated by the residual Chi-squared statistic divided by the residual degrees of freedom. The dispersion used is returned as an attribute of the matrix.

The dimensions of the matrix correspond to the non-eliminated coefficients of the "gnm" object. If use. eliminate = TRUE then setting can sometimes give appreciable speed gains; see gnm for details of the eliminate mechanism. The use.eliminate argument is currently ignored if the model has full rank.

\section*{Value}

A matrix with number of rows/columns equal to length(coef(object)). If there are eliminated coefficients and use.eliminate \(=\) TRUE, the matrix will have the following attributes:
covElim a matrix of covariances between the eliminated and non-eliminated parameters.
varElim a vector of variances corresponding to the eliminated parameters.

\section*{Note}

The gnm class includes generalized linear models, and it should be noted that the behaviour of vcov.gnm differs from that of vcov.glm whenever any (is.na(coef(object))) is TRUE. Whereas vcov.glm drops all rows and columns which correspond to NA values in coef (object), vcov.gnm keeps those columns (which are full of zeros, since the NA represents a parameter which is fixed either by use of the constrain argument to gnm or by a convention to handle linear aliasing).

\section*{Author(s)}

David Firth

\section*{References}

Turner, H and Firth, D (2005). Generalized nonlinear models in R: An overview of the gnm package. At https://cran.r-project.org

\section*{See Also}
```

getContrasts, se.gnm

```

\section*{Examples}
```

set.seed(1)

## Fit the "UNIDIFF" mobility model across education levels

unidiff <- gnm(Freq ~ educ*orig + educ*dest +
Mult(Exp(educ), orig:dest), family = poisson,
data = yaish, subset = (dest != 7))

## Examine the education multipliers (differences on the log scale):

ind <- pickCoef(unidiff, "[.]educ")
educMultipliers <- getContrasts(unidiff, rev(ind))

## Now get the same standard errors using a suitable set of

## quadratic forms, by calling vcov() directly:

cmat <- contr.sum(ind)
sterrs <- sqrt(diag(t(cmat)
%*% vcov(unidiff)[ind, ind]
%*% cmat))
all(sterrs == (educMultipliers\$SE)[-1]) \#\# TRUE

```

\section*{Description}

Voting data from the 1987 British general election, cross-classified by the class of the head of household and the class of their father.

\section*{Usage}
voting

\section*{Format}

A data frame with 25 observations on the following 4 variables.
percentage the percentage of the cell voting Labour.
total the cell count.
origin a factor describing the father's class with levels 1:5.
destination a factor describing the head of household's class with levels 1:5.

\section*{Source}

Clifford, P. and Heath, A. F. (1993) The Political Consequences of Social Mobility. J. Roy. Stat. Soc. A, 156(1), 51-61.

\section*{Examples}
```


### Examples from Clifford and Heath paper

### (Results differ slightly - possible transcription error in

### published data?)

set.seed(1)

## reconstruct counts voting Labour/non-Labour

count <- with(voting, percentage/100 * total)
yvar <- cbind(count, voting\$total - count)

## fit diagonal reference model with constant weights

classMobility <- gnm(yvar ~ -1 + Dref(origin, destination),
family = binomial, data = voting)
DrefWeights(classMobility)

## create factors indicating movement in and out of salariat (class 1)

upward <- with(voting, origin != 1 \& destination == 1)
downward <- with(voting, origin == 1 \& destination != 1)

## fit separate weights for the "socially mobile" groups

socialMobility <- gnm(yvar ~ -1 + Dref(origin, destination,

```
```

                            delta = ~ 1 + downward + upward),
    family = binomial, data = voting)
    DrefWeights(socialMobility)
    ## fit separate weights for downwardly mobile groups only
    downwardMobility <- gnm(yvar ~ -1 + Dref(origin, destination,
                        delta = ~ 1 + downward),
    family = binomial, data = voting)
    DrefWeights(downwardMobility)

```
wedderburn Wedderburn Quasi-likelihood Family

\section*{Description}

Creates a family object for use with glm, gnm, etc., for the variance function \([\mu(1-\mu)]^{2}\) introduced by Wedderburn (1974) for response values in [0,1].

\section*{Usage}
wedderburn(link = "logit")

\section*{Arguments}
link The name of a link function. Allowed are "logit", "probit" and "cloglog".

\section*{Value}

An object of class family.

\section*{Note}

The reported deviance involves an arbitrary constant (see McCullagh and Nelder, 1989, p330); for estimating dispersion, use the Pearson chi-squared statistic instead.

\section*{Author(s)}

Modification of binomial by the R Core Team. Adapted for the Wedderburn quasi-likelihood family by David Firth.

\section*{References}

Gabriel, K R (1998). Generalised bilinear regression. Biometrika 85, 689-700.
McCullagh, P and Nelder, J A (1989). Generalized Linear Models (2nd ed). Chapman and Hall.
Wedderburn, R W M (1974). Quasilikelihood functions, generalized linear models and the GaussNewton method. Biometrika 61, 439-47.

\section*{See Also}
```

glm, gnm, family

```

\section*{Examples}
```

set.seed(1)

### Use data from Wedderburn (1974), see ?barley

### Fit Wedderburn's logit model with variance proportional to the

### square of mu(1-mu)

logitModel <- glm(y ~ site + variety, family = wedderburn, data = barley)
fit <- fitted(logitModel)
print(sum((barley\$y - fit)^2 / (fit * (1-fit))^2))

## Agrees with the chi-squared value reported in McCullagh and Nelder

## (1989, p331), which differs slightly from Wedderburn's reported value.

### Fit the biplot model as in Gabriel (1998, p694)

biplotModel <- gnm(y ~ -1 + instances(Mult(site, variety), 2),
family = wedderburn, data = barley)
barleySVD <- svd(matrix(biplotModel$predictors, 10, 9))
A <- sweep(barleySVD$v, 2, sqrt(barleySVD$d), "*")[, 1:2]
B <- sweep(barleySVD$u, 2, sqrt(barleySVD\$d), "*")[, 1:2]

## These are essentially A and B as in Gabriel (1998, p694), from which

## the biplot is made by

plot(rbind(A, B), pch = c(LETTERS[1:9], as.character(1:9), "X"))

### Fit the double-additive model as in Gabriel (1998, p697)

variety.binary <- factor(match(barley\$variety, c(2,3,6), nomatch = 0) > 0,
labels = c("Rest", "2,3,6"))
doubleAdditive <- gnm(y ~ variety + Mult(site, variety.binary),
family = wedderburn, data = barley)

```
    wheat Wheat Yields from Mexican Field Trials

\section*{Description}

Data from a 10-year experiment at the CIMMYT experimental station located in the Yaqui Valley near Ciudad Obregon, Sonora, Mexico - factorial design using 24 treatments in all. In each of the 10 years the experiment was arranged in a randomized complete block design with three replicates.

\section*{Usage}
wheat

\section*{Format}

A data frame with 240 observations on the following 33 variables.
yield numeric, mean yield in \(\mathrm{kg} / \mathrm{ha}\) for 3 replicates
year a factor with levels 1988:1997
tillage a factor with levels \(\mathrm{T} t\)
summerCrop a factor with levels S s
manure a factor with levels Mm
\(\mathbf{N}\) a factor with levels 0 N n
MTD numeric, mean max temp sheltered \((\operatorname{deg} C)\) in December
MTJ same for January
MTF same for February
MTM same for March
MTA same for April
mTD numeric, mean min temp sheltered \((\operatorname{deg} C)\) in December
mTJ same for January
mTF same for February
mTM same for March
mTA same for April
mTUD numeric, mean min temp unsheltered (deg C)in December
mTUJ same for January
mTUF same for February
mTUM same for March
mTUA same for April
PRD numeric, total precipitation (mm) in December
PRJ same for January
PRF same for February
PRM same for March
SHD numeric, mean sun hours in December
SHJ same for January
SHF same for February
EVD numeric, total evaporation (mm) in December
EVJ same for January
EVF same for February
EVM same for March
EVA same for April

\section*{Source}

Tables A1 and A3 of Vargas, M, Crossa, J, van Eeuwijk, F, Sayre, K D and Reynolds, M P (2001). Interpreting treatment by environment interaction in agronomy trials. Agronomy Journal 93, 949960.

\section*{Examples}
```

set.seed(1)

## Scale yields to reproduce analyses reported in Vargas et al (2001)

yield.scaled <- wheat\$yield * sqrt(3/1000)

## Reproduce (up to error caused by rounding) Table 1 of Vargas et al (2001)

aov(yield.scaled ~ year*tillage*summerCrop*manure*N, data = wheat)
treatment <- interaction(wheat$tillage, wheat$summerCrop, wheat$manure,
    wheat$N, sep = "")
mainEffects <- lm(yield.scaled ~ year + treatment, data = wheat)
svdStart <- residSVD(mainEffects, year, treatment, 3)
bilinear1 <- update(asGnm(mainEffects), . ~ . +
Mult(year, treatment),
start = c(coef(mainEffects), svdStart[,1]))
bilinear2 <- update(bilinear1, . ~ . +
Mult(year, treatment, inst = 2),
start = c(coef(bilinear1), svdStart[,2]))
bilinear3 <- update(bilinear2, . ~ . +
Mult(year, treatment, inst = 3),
start = c(coef(bilinear2), svdStart[,3]))
anova(mainEffects, bilinear1, bilinear2, bilinear3)

## Examine the extent to which, say, mTF explains the first bilinear term

bilinear1mTF <- gnm(yield.scaled ~ year + treatment + Mult(1 + mTF, treatment),
family = gaussian, data = wheat)
anova(mainEffects, bilinear1mTF, bilinear1)
How to get the standard SVD representation of an AMMI-n model

## 

## We'll work with the AMMI-2 model, which here is called "bilinear2"

## 

## First, extract the contributions of the 5 terms in the model:

## 

wheat.terms <- termPredictors(bilinear2)

## 

## That's a matrix, whose 4th and 5th columns are the interaction terms

## 

## Combine those two interaction terms, to get the total estimated

## interaction effect:

## 

wheat.interaction <- wheat.terms[, 4] + wheat.terms[, 5]

## 

## That's a vector, so we need to re-shape it as a 24 by 10 matrix

## ready for calculating the SVD:

## 

```
```

wheat.interaction <- matrix(wheat.interaction, 24, 10)

## 

## Now we can compute the SVD:

## 

wheat.interaction.SVD <- svd(wheat.interaction)

## 

## Only the first two singular values are nonzero, as expected

## (since this is an AMMI-2 model, the interaction has rank 2)

## 

## So the result object can be simplified by re-calculating the SVD with

## just two dimensions:

## 

wheat.interaction.SVD <- svd(wheat.interaction, nu = 2, nv = 2)

```
yaish

Class Mobility by Level of Education in Israel

\section*{Description}

A 3-way contingency table of father/son pairs, classified by father's social class (orig), son's social class (dest) and son's education level (educ).

\section*{Usage}
yaish

\section*{Format}

A table of counts, with classifying factors educ (levels 1:5), orig (levels 1:7) and dest (levels 1:7).

\section*{Author(s)}

David Firth

\section*{Source}

Originally in Yaish (1998), see also Yaish (2004, p316).

\section*{References}

Yaish, M (1998). Opportunities, Little Change. Class Mobility in Israeli Society: 1974-1991. D.Phil. Thesis, Nuffield College, University of Oxford.

Yaish, M (2004). Class Mobility Trends in Israeli Society, 1974-1991. Lewiston: Edwin Mellen Press.

\section*{Examples}
```

set.seed(1)

## Fit the "UNIDIFF" mobility model across education levels, leaving out

## the uninformative subtable for dest == 7:

## 

unidiff <- gnm(Freq ~ educ*orig + educ*dest +
Mult(Exp(educ), orig:dest), family = poisson,
data = yaish, subset = (dest != 7))

## Deviance should be 200.3, 116 d.f.

## 

## Look at the multipliers of the orig:dest association:

ofInterest(unidiff) <- pickCoef(unidiff, "[.]educ")
coef(unidiff)

## 

## Coefficients of interest:

## Mult(Exp(.), orig:dest).educ1 Mult(Exp(.), orig:dest).educ2

## -0.5513258 -0.7766976

## Mult(Exp(.), orig:dest).educ3 Mult(Exp(.), orig:dest).educ4

## 

                -1.2947494
                            -1.5902644
    
## Mult(Exp(.), orig:dest).educ5

## -2.8008285

## 

## Get standard errors for the contrasts with educ1:

## 

getContrasts(unidiff, ofInterest(unidiff))

## estimate SE quasiSE

## Mult(Exp(.), orig:dest).educ1 0.0000000 0.0000000 0.09757438

## Mult(Exp(.), orig:dest).educ2 -0.2253718 0.1611874 0.12885847

## Mult(Exp(.), orig:dest).educ3 -0.7434236 0.2335083 0.21182123

## Mult(Exp(.), orig:dest).educ4 -1.0389386 0.3434256 0.32609380

## Mult(Exp(.), orig:dest).educ5 -2.2495026 0.9453764 0.93560643

## 

                                    quasivar
    
## Mult(Exp(.), orig:dest).educ1 0.00952076

## Mult(Exp(.), orig:dest).educ2 0.01660450

## Mult(Exp(.), orig:dest).educ3 0.04486823

## Mult(Exp(.), orig:dest).educ4 0.10633716

## Mult(Exp(.), orig:dest).educ5 0.87535940

## 

## Table of model residuals:

## 

residuals(unidiff)

```

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```

