Package 'krige'

May 1, 2022

Way 1, 2022
Type Package
Title Geospatial Kriging with Metropolis Sampling
Version 0.6.2
Date 2022-04-28
Author Jason S. Byers [aut, cre], Le Bao [aut], Jamie Carson [aut], Jeff Gill [aut]
Maintainer Jason S. Byers <jaybyers55@gmail.com></jaybyers55@gmail.com>
Description Estimates kriging models for geographical point-referenced data. Method is described in Gill (2020) <doi:10.1177 1532440020930197="">.</doi:10.1177>
License GPL (>= 2)
Depends R (>= 4.0)
Imports Rcpp, stats, graphics, coda
LinkingTo Rcpp
Encoding UTF-8
LazyData true
RoxygenNote 7.1.1
NeedsCompilation yes
Repository CRAN
Date/Publication 2022-05-01 14:20:02 UTC
R topics documented:
as.matrix.semivariance
as.mcmc.krige
burnin
congCombined 5 ContrivedData 7
exponential.semivariance
geweke
heidel.welch
krige

2 as.matrix.semivariance

	rrige.posterior	13
	owerCombined	
	ncmc.samples	17
	netropolis.krige	19
	NYcity_subset	23
	NY_subset	25
	oredict.krige	27
	semivariance	30
	semivariogram	32
	stateCombined	35
	summary.krige	37
	ıpdate.krige	38
	apperCombined	39
	WVwells	40
Index		44
as.m	rix.semivariance	

Convert semivariance to a matrix object

Description

Convert semivariance to a matrix object

Usage

```
## S3 method for class 'semivariance'
as.matrix(x, ...)
## S3 method for class 'semivariance'
as.data.frame(x, ...)
```

Arguments

- x An semivariance object created by semivariance or exponential.semivariance.
- ... Additional arguments passed to as.matrix and as.data.frame methods. Not supported for semivariance object.

Details

The defaults of semivariance methods give a list or numeric vector. These methods can convert the semivariance output list and vector to matrix or data. frame.

Value

A matrix containing the computed distance and semivariance.

as.mcmc.krige 3

Examples

```
## Not run:
# Summarize Data
summary(ContrivedData)
# Empirical semivariance for variable y
raw.var <- semivariance(x=ContrivedData$y,coords = cbind(ContrivedData$s.1,</pre>
  ContrivedData$s.2))
as.matrix(raw.var)
# Estimation using metropolis.krige()
#' # Set seed
set.seed(1241060320)
M <- 100
#M<-10000
contrived.run <- metropolis.krige(y \sim x.1 + x.2, coords = c("s.1", "s.2"),
   data = ContrivedData, n.iter = M, range.tol = 0.05)
# Parametric semivariance
parametric.var <- semivariance(contrived.run)</pre>
as.matrix(parametric.var)
as.data.frame(parametric.var)
## End(Not run)
```

as.mcmc.krige

Convert krige object to an mcmc object

Description

Convert MCMC matrix of posterior samples for use with the coda package

Usage

```
## S3 method for class 'krige'
as.mcmc(x, start = 1, end = x$n.iter, thin = 1, ...)
## S3 method for class 'summary.krige'
as.mcmc(x, start = 1, end = x$n.iter, thin = 1, ...)
```

Arguments

X	An krige or summary.krige object.
start	The iteration number of the first observation.
end	The iteration number of the last observation.

4 as.mcmc.krige

thin The thinning interval between consecutive observations.

... Additional arguments to be passed to mcmc() methods of coda package.

Details

The function converts a krige output object to a Markov Chain Monte Carlo (mcmc) object used in coda as well as a variety of MCMC packages. It extracts the MCMC matrix of posterior samples from the output of metropolis.krige for further use with other MCMC packages and functions.

Value

A mcmc object.

See Also

```
coda::as.mcmc()
```

```
## Not run:
# Summarize Data
summary(ContrivedData)
# Set seed
set.seed(1241060320)
#For simple illustration, we set to few iterations.
#In this case, a 10,000-iteration run converges to the true parameters.
#If you have considerable time and hardware, delete the # on the next line.
#10,000 iterations took 39 min. with 8 GB RAM & a 1.5 GHz Quad-Core processor.
M <- 100
#M<-10000
contrived.run <- metropolis.krige(y \sim x.1 + x.2, coords = c("s.1", "s.2"),
                                   data = ContrivedData, n.iter = M, n.burnin = 20,
                                   range.tol = 0.05)
# Convert to mcmc object
mcmc.contrived.run <- as.mcmc(contrived.run)</pre>
#mcmc.contrived.run <- as.mcmc(summary(contrived.run))</pre>
# Diagnostics using MCMC packages
coda::raftery.diag(mcmc.contrived.run)
# superdiag::superdiag(mcmc.contrived.run) #NOT WORKING YET
## End(Not run)
```

burnin 5

burnin

Discard Burn-in Period of Kriging Model

Description

Discard burn-in period of a estimated model from metropolis.krige

Usage

```
burnin(object, n.burnin)
## S3 method for class 'krige'
burnin(object, n.burnin = object$n.iter/2)
## S3 method for class 'matrix'
burnin(object, n.burnin = nrow(object)/2)
```

Arguments

object An krige object from the metropolis.krige function.

n.burnin The number of burnin iterations. Defaults to half of the iterations.

Details

The function discard the burn-in period from the results of metropolis.krige. It is generally used for discarding burn-in for krige object that keeps all the iterations.

congCombined

Congressional District Public Opinion Ideology in 2010

Description

These data present measures of ideology in 2010 for 434 districts for the U.S. House of Representatives, recorded as the variable krige.cong. Forecasts are based on a kriging model fitted over the 2008 Cooperative Congressional Election Survey (CCES), paired with predictive data from the 2010 Census. Each district's public ideology is paired with the DW-NOMINATE common space score of each of its representative in 2011 (update from McCarty, Poole and Rosenthal 1997). Eight districts have repeated observations in order to include the DW-NOMINATE score when a member was replaced mid-term.

6 congCombined

Format

The congCombined dataset has 442 observations and 12 variables. 4 34 out of 435 congressional districts are covered, with eight districts duplicated when a member was replaced mid-term.

stateCD Unique identifier for each congressional district by state. The first two digits are STATEA, and the second two are cd.

krige.cong The ideology of the average citizen in the congressional district.

krige.state.var The variance of ideology among the district's citizens.

cong The term of Congress studied–112 for this dataset.

idno Identification number for the House member–ICPSR numbers continued by Poole & Rosenthal.

state The ICPSR code for the state.

cd The congressional district number.

statenm The first seven letters of the state's name.

party Political party of the House member. 100=Democrat, 200=Republican.

name Last name of the House member, followed by first name if ambiguous.

dwnom1 First dimension DW-NOMINATE common space score for the House member. Higher values are usually interpreted as more right-wing, with lower values as more left-wing.

STATEA The FIPS code for the state.

Source

Ansolabehere, Stephen. 2011. "CCES, Common Content, 2008." Ver. 4.

McCarty, Nolan M., Keith T. Poole and Howard Rosenthal. 1997. *Income Redistribution and the Realignment of American Politics*. American Enterprise Institude Studies on Understanding Economic Inequality. Washington: AEI Press.

Minnesota Population Center. 2011. *National Historical Geographic Information System: Version* 2.0. Minneapolis, MN: University of Minnesota. 'https://www.nhgis.org'

References

Jeff Gill. 2020. Measuring Constituency Ideology Using Bayesian Universal Kriging. *State Politics & Policy Quarterly*. doi:10.1177/1532440020930197

```
# Descriptive Statistics
summary(congCombined)

# Correlate House Members' DW-NOMINATE Scores with Public Opinion Ideology
cor(congCombined$dwnom1,congCombined$krige.cong)

# Plot House Members' DW-NOMINATE Scores against Public Opinion Ideology
plot(y=congCombined$dwnom1,x=congCombined$krige.cong,
    xlab="District Ideology (Kriging)", ylab="Legislator Ideology (1st Dim., Common Space)",
```

ContrivedData 7

```
main="U.S. House of Representatives", type="n")
points(y=congCombined$dwnom1[congCombined$party==200],
    x=congCombined$krige.cong[congCombined$party==200],pch="R",col="red")
    points(y=congCombined$dwnom1[congCombined$party==100],
    x=congCombined$krige.cong[congCombined$party==100],pch="D",col="blue")
```

ContrivedData

Contrived Example Data

Description

These data are a simulated point-referenced geospatial data that serve to provide a clean example of a kriging model. There are 500 observations with coordinates located on a unit square.

Format

The ContrivedData dataset has 500 observations and 5 variables.

- y The outcome variable. Its true population functional form is $y_s = 0 + 1x_{1s} + 2x_{2s} + \omega_s + \epsilon_s$. The true variance of ω is $\sigma^2 = 0.5$ and of ϵ is $\tau^2 = 0.5$. The decay term that shapes spatial correlation levels is $\phi = 2.5$.
- x.1 A predictor with a standard uniform distribution.
- x.2 A predictor with a standard normal distribution.
- s.1 Coordinate in eastings for each observation, distributed standard uniform.
- s.2 Coordinate in northings for each observation, distributed standard uniform.

```
## Not run:
# Summarize example data
summary(ContrivedData)
# Initial OLS model
contrived.ols<-lm(y^x.1+x.2,data=ContrivedData)
# summary(contrived.ols)
# Set seed
set.seed(1241060320)
#For simple illustration, we set to few iterations.
#In this case, a 10,000-iteration run converges to the true parameters.
#If you have considerable time and hardware, delete the # on the next line.
#10,000 iterations took 39 min. with 8 GB RAM & a 1.5 GHz Quad-Core processor.
M <- 100
#M<-10000
contrived.run <- metropolis.krige(y \sim x.1 + x.2, coords = c("s.1", "s.2"),
  data = ContrivedData, n.iter = M, n.burnin=20, range.tol = 0.05)
```

```
# Alternatively, use burnin() after estimation
#contrived.run <- burnin(contrived.run, n.burnin=20)

# Summarize the results and examine results against true coefficients
summary(contrived.run)
(TRUTH<-c(0.5,2.5,0.5,0,1,2))

## End(Not run)</pre>
```

exponential.semivariance

Parametric Exponential Semivariance

Description

This function returns the value of a parametric powered exponential semivariogram given the values of the parameters and the distance between observations.

Usage

```
exponential.semivariance(...)
## S3 method for class 'krige'
exponential.semivariance(object, ...)
## Default S3 method:
exponential.semivariance(nugget, decay, partial.sill, distance, power = 2, ...)
```

Arguments

... Additional arguments

object A krige object of which the values of the estimates are used to calculate the

exponential semivariance.

nugget The value of the non-spatial variance, or nugget term.

decay The value of the decay term that sets the level of correlation given distance.

partial.sill The value of the spatial variance, or partial sill term.

distance The distance among observations for which the semivariance value is desired.

power The exponent specified in the powered exponential semivariogram. Defaults to

2, which corresponds to a Gaussian semivariance function.

Details

The models estimated by the krige package assume a powered exponential covariance structure. Each parametric covariance function for kriging models corresponds to a related semivariance function, given that highly correlated values will have a small variance in differences while uncorrelated values will vary widely. More specifically, semivariance is equal to half of the variance of

the difference in a variable's values at a given distance. That is, the semivariance is defined as: $\gamma(h) = 0.5 * E[X(s+h) - X(s)]^2$, where X is the variable of interest, s is a location, and h is the distance from s to another location.

The powered exponential covariance structure implies that the semivariance follows the specific functional form of $\gamma(d) = \tau^2 + \sigma^2(1 - \exp(-|\phi d|^p))$ (Banerjee, Carlin, and Gelfand 2015, 27). A perk of this structure is that the special case of $p{=}1$ implies the commonly-used exponential semivariogram, and the special case of $p{=}2$ implies the commonly-used Gaussian semivariogram. Upon estimating a model, it is advisable to graph the functional form of the implied parametric semivariance structure. By substituting estimated values of the nugget, decay, and partial.sill terms, as well as specifying the correct power argument, it is possible to compute the implied semivariance from the model. The distance argument easily can be a vector of observed distance values.

Value

A semivariance object. It will be a numeric vector with each bin's value of the semivariance.

References

Sudipto Banerjee, Bradley P. Carlin, and Alan E. Gelfand. 2015. *Hierarchical Modeling and Analysis for Spatial Data*. 2nd ed. Boca Raton, FL: CRC Press.

See Also

semivariogram, plot.semivariance, exponential.semivariance

```
## Not run:
# Summarize data
summary(ContrivedData)
# Set seed
set.seed(1241060320)
M <- 100
contrived.run <- metropolis.krige(y \sim x.1 + x.2, coords = c("s.1", "s.2"),
  data = ContrivedData, n.iter = M, range.tol = 0.05)
# Parametric powered exponential semivariogram
exponential.semivariance(contrived.run)
#OLS Model for Residuals
contrived.ols<-lm(y^x.1+x.2,data=ContrivedData)
# Residual semivariance
(resid.semivar <- semivariance(contrived.ols, coords = c("s.1", "s.2"), terms = "residual"))</pre>
# Parametric exponential semivariance
exponential.semivariance(nugget=0.5,decay=2.5,partial.sill=0.5,
```

10 geweke

```
distance=as.numeric(names(resid.semivar)))
```

geweke

End(Not run)

Geweke Diagnostic for MCMC

Description

Conducts a Geweke convergence diagnostic on MCMC iterations.

Usage

```
geweke(object, early.prop = 0.1, late.prop = 0.5, precision = 4)
## S3 method for class 'krige'
geweke(object, early.prop = 0.1, late.prop = 0.5, precision = 4)
## S3 method for class 'summary.krige'
geweke(object, early.prop = 0.1, late.prop = 0.5, precision = 4)
## Default S3 method:
geweke(object, early.prop = 0.1, late.prop = 0.5, precision = 4)
```

Arguments

object	An matrix or krige/summary.krige object for which a Geweke diagnostic is desired
early.prop	Proportion of iterations to use from the start of the chain.
late.prop	Proportion of iterations to use from the end of the chain.
precision	Number of digits of test statistics and p-values to print.

Details

This is a generic function currently works with matrix, krige, and summary.krige objects. It is a simplified version of the Geweke test for use with this package.

Geweke's (1992) test for nonconvergence of a MCMC chain is to conduct a difference-of-means test that compares the mean early in the chain to the mean late in the chain. If the means are significantly different from each other, then this is evidence that the chain has not converged. The difference-of-means test is a simple z-ratio, though the standard error is estimated using the spectral density at zero to account for autocorrelation in the chain.

heidel.welch

Value

A matrix in which the first row consists of z-scores for tests of equal means for the first and last parts of the chain. The second row consists of the corresponding p-values. Each column of the matrix represents another parameter. For each column, a significant result is evidence that the chain has not converged for that parameter. Thus, a non-significant result is desired.

References

John Geweke. 1992. "Evaluating the Accuracy of Sampling-Based Approaches to the Calculation of Posterior Moments." In *Bayesian Statistics 4*, ed. J.M. Bernardo, J.O. Berger, A.P. Dawid, and A.F.M. Smith. Oxford: Clarendon Press.

See Also

```
geweke.krige, geweke.summary.krige
```

Examples

```
## Not run:
# Load Data
data(ContrivedData)

# Set seed
set.seed(1241060320)

M <- 100

contrived.run <- metropolis.krige(y ~ x.1 + x.2, coords = c("s.1","s.2"),
    data = ContrivedData, n.iter = M, range.tol = 0.05)

geweke(contrived.run, early.prop=0.5)
geweke(summary(contrived.run), early.prop=0.5)
geweke(contrived.run$mcmc.mat, early.prop=0.5)
# Note that the default proportions in the geweke() is more typical for longer run.
## End(Not run)</pre>
```

heidel.welch

Heidelberger and Welch Diagnostic for MCMC

Description

Conducts a Heidelberger and Welch convergence diagnostic on MCMC iterations.

12 heidel.welch

Usage

```
heidel.welch(object, pvalue)

## S3 method for class 'krige'
heidel.welch(object, pvalue = 0.05)

## S3 method for class 'summary.krige'
heidel.welch(object, pvalue = 0.05)

## Default S3 method:
heidel.welch(object, pvalue = 0.05)
```

Arguments

object An matrix or krige/summary.krige object for which a Heidelberger and Welch

diagnostic is desired

pvalue Alpha level for significance tests. Defaults to 0.05.

Details

This is a generic function currently works with matrix, krige, and summary.krige objects. It is a simplified version of the Heidelberger and Welch test for use with this package.

This is an adaptation of a function in Plummer et al.'s coda package. Heidelberger and Welch's (1993) test for nonconvergence. This version of the diagnostic only reports a Cramer-von Mises test and its corresponding p-value to determine if the chain is weakly stationary with comparisons of early portions of the chain to the end of the chain.

Value

A matrix in which the first row consists of the values of the Cramer-von Mises test statistic for each parameter, and the second row consists of the corresponding p-values. Each column of the matrix represents another parameter of interest. A significant result serves as evidence of nonconvergence, so non-significant results are desired.

References

Philip Heidelberger and Peter D. Welch. 1993. "Simulation Run Length Control in the Presence of an Initial Transient." *Operations Research* 31:1109-1144.

Martyn Plummer, Nicky Best, Kate Cowles and Karen Vines. 2006. "CODA: Convergence Diagnosis and Output Analysis for MCMC." *R News* 6:7-11.

See Also

heidel.welch.krige, heidel.welch.summary.krige, geweke

krige 13

Examples

```
## Not run:
# Load Data
data(ContrivedData)

# Set seed
set.seed(1241060320)

M <- 100

contrived.run <- metropolis.krige(y ~ x.1 + x.2, coords = c("s.1","s.2"),
    data = ContrivedData, n.iter = M, n.burnin = 20, range.tol = 0.05)

heidel.welch(contrived.run)
heidel.welch(summary(contrived.run))
heidel.welch(contrived.run$mcmc.mat)

## End(Not run)</pre>
```

krige

krige: Geospatial Kriging with Metropolis Sampling

Description

Estimates kriging models for geographical point-referenced data. Method is described ' in Gill (2020) <doi:10.1177/1532440020930197>.

krige.posterior

Posterior Distribution for the Kriging Process

Description

This function finds the posterior density of a geospatial linear regression model given a point-referenced geospatial dataset and a set of parameter values. The function is useful for finding the optimum of or for sampling from the posterior distribution.

Usage

```
krige.posterior(
  tau2,
  phi,
  sigma2,
  beta,
  y,
  X,
```

14 krige.posterior

```
east,
north,
semivar.exp = 2,
p.spatial.share = 0.5,
p.range.share = 0.5,
p.range.tol = 0.05,
p.beta.var = 10,
tot.var = var(y),
local.Sigma = NULL,
max.distance = NULL
```

Arguments

tau2 Value of the nugget, or non-spatial error variance.

phi Value of the decay term, driving the level of spatial correlation. sigma2 Value of the partial sill, or maximum spatial error variance.

beta Coefficients from linear model.

y The outcome variable that is used in the kriging model.

X The matrix of explanatory variables used in the kriging model.

east Vector of eastings for all observations.

North Vector of northings for all observations.

semivar.exp This exponent, which must be greater than 0 and less than or equal to 2, specifies

a powered exponential correlation structure for the data. One widely used specification is setting this to 1, which yields an exponential correlation structure. Another common specification is setting this to 2 (the default), which yields a

Gaussian correlation structure.

p.spatial.share

Prior for proportion of unexplained variance that is spatial in nature. Must be

greater than 0 and less than 1. Defaults to an even split.

p.range.share Prior for the effective range term, as a proportion of the maximum distance in

the data. Users should choose the proportion of distance at which they think the spatial correlation will become negligible. Must be greater than 0. Values greater than 1 are permitted, but users should recognize that this implies that meaningful spatial correlation would persist outside of the convex hull of data.

Defaults to half the maximum distance.

p.range.tol Tolerance term for setting the effective range. At the distance where the spatial

correlation drops below this term, it is judged that the effective range has been met. Users are typically advised to leave this at its default value of 0.05 unless they have strong reasons to choose another level. Must be greater than 0 and

less than 1.

p.beta.var Prior for the variance on zero-meaned normal priors on the regression coeffi-

cients. Defaults to 10.

tot.var Combined variance between the nugget and partial sill. Defaults to the vari-

ance of y. The metropolis.krige function inserts the residual variance from a

standard linear model.

krige.posterior 15

local.Sigma	The user is advised to ignore this option, or leave it the value of NULL. This option is included to reduce the number of computations required when this function is called by metropolis.krige.
max.distance	The user is advised to ignore this option, or leave it the value of NULL. This option is included to reduce the number of computations required when this

function is called by metropolis.krige.

Details

This function finds the posterior density for a kriging model. It is designed to be an internal function but is exported in the hope of it can be useful to some users. The function utilizes information provided about the parameters tau2, phi, sigma2, and beta. It also utilizes the observed data y, X, east, and north. Given a set of parameter values as well as the observed data, the function returns the posterior density for the specified model.

Value

A single number that is the posterior density of the function, which is stored in object of class matrix.

References

Jeff Gill. 2020. Measuring Constituency Ideology Using Bayesian Universal Kriging. *State Politics & Policy Quarterly*. doi:10.1177/1532440020930197

```
# Summarize Data
summary(ContrivedData)

#Initial OLS Model
contrived.ols<-lm(y~x.1+x.2,data=ContrivedData);summary(contrived.ols)

#Define Covariate Matrix
covariates<-cbind(1,ContrivedData$x.1,ContrivedData$x.2)

# Find the posterior density for the Contrived Data if all parameters were 1:
s.test <- krige.posterior(tau2=1,phi=1,sigma2=1,beta=rep(1,ncol(covariates)),
    y=ContrivedData$y,X=covariates,east=ContrivedData$s.1,north=ContrivedData$s.2)

# Print posterior density
s.test</pre>
```

16 lowerCombined

lowerCombined	State Legislative District (Lower Chambers) Public Opinion Ideology in 2010

Description

These data present measures of ideology in 2010 for the districts for lower chambers of state legislatures, recorded as the variable krige.lower. 49 states' chambers are covered—the Nebraska Unicameral is omitted here to be included in the file upperCombined. Forecasts are based on a kriging model fitted over the 2008 Cooperative Congressional Election Survey (CCES), paired with predictive data from the 2010 Census. Each district's public ideology is paired with a measure of the ideology of the State House member (or members) from the district (update from Shor and McCarty 2011).

Format

The lowerCombined dataset has 5446 observations and 10 variables.

st Two-letter postal abbreviation for the state.

lower The state legislative district number (lower chamber).

STATEA The FIPS code for the state.

krige.lower The ideology of the average citizen in the district.

lowerKluge Combined index of STATEA followed by lower.

krige.lower.var The variance of ideology among the district's citizens.

name Last name of the state legislator, followed by first name and middle initial.

party Political party of the legislator. D=Democrat, R=Republican, X=Other.

st_id Temporary identifer variable. DO NOT USE.

np_score Ideology score for the state legislator (lower chamber). Higher values are usually interpreted as more right-wing, with lower values as more left-wing.

Source

Ansolabehere, Stephen. 2011. "CCES, Common Content, 2008." Ver. 4.

Minnesota Population Center. 2011. *National Historical Geographic Information System: Version* 2.0. Minneapolis, MN: University of Minnesota. 'https://www.nhgis.org'

Shor, Boris and Nolan M. McCarty. 2011. "The Ideological Mapping of American Legislatures." *American Political Science Review* 105(3):530-551.

References

Jeff Gill. 2020. Measuring Constituency Ideology Using Bayesian Universal Kriging. *State Politics & Policy Quarterly*. doi:10.1177/1532440020930197

mcmc.samples 17

Examples

mcmc.samples

Extract MCMC Samples

Description

Extract MCMC samples estimated by metropolis.krige()

Usage

```
mcmc.samples(object, as.matrix, as.data.frame, ...)
## S3 method for class 'krige'
mcmc.samples(object, as.matrix = !as.data.frame, as.data.frame = FALSE, ...)
## S3 method for class 'summary.krige'
mcmc.samples(object, as.matrix = !as.data.frame, as.data.frame = FALSE, ...)
## S3 method for class 'krige'
as.matrix(x, ...)
## S3 method for class 'summary.krige'
as.matrix(x, ...)
## S3 method for class 'krige'
as.data.frame(x, ...)
## S3 method for class 'summary.krige'
as.data.frame(x, ...)
```

18 mcmc.samples

Arguments

object	A krigeor summary.krige object from the metropolis.krige function.
as.matrix	Logical values indicating if the output format should be a matrix. Defaults to TRUE.
as.data.frame	Logical values indicating if the output format should be a data.frame. Defaults to FALSE.
	Additional arguments passed to as.matrix or as.data.frame methods.
X	A krige or summary.krige object for as.matrix and as.data.frame methods.

Details

The function extracts the MCMC samples from the a krigeor summary.krige object from the metropolis.krige function. Users can define the output by using as.matrix or as.data.frame.

Value

A summary.krige list object.

See Also

```
as.mcmc.krige
```

```
## Not run:
# Summarize Data
summary(ContrivedData)
# Initial OLS model
contrived.ols<-lm(y~x.1+x.2,data=ContrivedData)</pre>
# summary(contrived.ols)
# Set seed
set.seed(1241060320)
M <- 100
#M<-10000
contrived.run <- metropolis.krige(y \sim x.1 + x.2, coords = c("s.1", "s.2"),
   data = ContrivedData, n.iter = M, n.burnin = 20, range.tol = 0.05)
contrived.run.mat <- mcmc.samples(contrived.run)</pre>
### Alternatively, use generic methods
contrived.run.mat <- as.matrix(contrived.run)</pre>
contrived.run.df <- as.data.frame(contrived.run)</pre>
## End(Not run)
```

metropolis.krige

Sampling Technique Using Metropolis-Hastings

Description

This function performs Metropolis-Hastings sampling for a linear model specified over point-referenced geospatial data. It returns MCMC iterations, with which results of the geospatial linear model can be summarized.

Usage

```
metropolis.krige(
  formula,
  coords,
  data,
  n.iter = 100,
  powered.exp = 2,
  n.burnin = 0,
 у,
 Χ,
  east,
  north,
  na.action = "na.fail",
  spatial.share = 0.5,
  range.share = 0.5,
  beta.var = 10,
  range.tol = 0.05,
  b.tune = 1,
  nugget.tune = 10,
 psill.tune = 1,
  distance.matrix = FALSE,
 progress.bar = "message",
  accept.rate.warning = TRUE
)
```

Arguments

formula	An object of class formula (or one that can be coerced to that classes). A symbolic description of the model to be fitted. Alternatively, the model can be specified in y (a vector of the outcome variable) and X (a matrix of explanatory variables).
coords	A matrix of coordinates for all observations or a vector of variable names indicating the coordinates variables in the data. Alternatively, the coordinates can also be specified seperately using east and north.
data	An data frame containing the variables in the model.
n.iter	Number of MCMC iterations (defaults to 100).

powered.exp This exponent, which must be greater than 0 and less than or equal to 2, specifies a powered exponential correlation structure for the data. One widely used specification is setting this to 1, which yields an exponential correlation structure. Another common specification is setting this to 2 (the default), which yields a Gaussian correlation structure. n.burnin Number of iterations that will be discarded for burnin (warmup). The number of burnin should not be larger than n.iter and the default is 0. Alternative specification for the outcome variable that is used in the kriging У model. If formula is used, this argument will be suppressed. Χ Alternative specification for the matrix of explanatory variables used in the kriging model. Different forms of the variables such as transformations and interactions also need to be specified accordingly beforehand. Alternative specification for the vector of eastings for all observations. east Alternative specification for the vector of northing for all observations. north A function which indicates what should happen when the data contain NAs. The na.action default is "na.fail." Another possible value is "na.omit." spatial.share Prior for proportion of unexplained variance that is spatial in nature. Must be greater than 0 and less than 1. Defaults to an even split, valued at 0.5. Prior for the effective range term, as a proportion of the maximum distance in range.share the data. Users should choose the proportion of distance at which they think the spatial correlation will become negligible. Must be greater than 0. Values greater than 1 are permitted, but users should recognize that this implies that meaningful spatial correlation would persist outside of the convex hull of data. Defaults to half the maximum distance, valued at 0.5. Prior for the variance on zero-meaned normal priors on the regression coeffibeta.var cients. Must be greater than 0. Defaults to 10. range.tol Tolerance term for setting the effective range. At the distance where the spatial correlation drops below this term, it is judged that the effective range has been met. The default value is the commonly-used 0.05. Must be greater than 0 and less than 1. b.tune Tuning parameter for candidate generation of regression coefficients that must be greater than 0. A value of 1 means that draws will be based on the variancecovariance matrix of coefficients from OLS. Larger steps are taken for values greater than 1, and smaller steps are taken for values from 0 to 1. Defaults to 1.0. Tuning parameter for candidate generation of the nugget term (tau2) that must nugget.tune be greater than 0. A value of 1 means that draws will be based on the typical variance of an inverse gamma distribution. Smaller steps are taken for values greater than 1, and larger steps are taken for decimal values from 0 to 1. Defaults to 10.0. psill.tune Tuning parameter for candidate generation of the partial sill term (sigma2) that

must be greater than 0. A value of 1 means that draws will be based on the typical variance of an inverse gamma distribution. *Smaller* steps are taken for values *greater* than 1, and *larger* steps are taken for *decimal* values from 0 to 1.

Defaults to 1.0.

distance.matrix

Logical value indicates whether to save the distance matrix in the output object. Saving distance matrix can save time for furthur use such as in update() function but may results in larger file size. Defaults to FALSE.

progress.bar

Types of progress bar. The default is "message" and will report variance terms. Other possible values are "TRUE" (simple percentage) and "FALSE" (suppress the progress bar).

accept.rate.warning

Logical values indicating whether to show the warnings when the acceptance rates are too high or too low. Defaults to TRUE.

Details

Analysts should use this function if they want to estimate a linear regression model in which each observation can be located at points in geographic space. That is, each observation is observed for a set of coordinates in eastings & northings or longitude & latitude.

Researchers must specify their model in the following manner: formula should be a symbolic description of the model to be fitted; it is similar to R model syntax as used in lm(). In addition, a matrix of coordinates must be specified for the geospatial model in coords. coords should be a matrix with two columns that specify west-east and north-south coordinates, respectively (ideally eastings and northings but possibly longitude and latitude). It can also be a vector of strings indicating the variables names of the coordinates in the data. data should be a data frame containing the variables in the model including both the formula and coordinates (if only the names are provided). Alternatively, users can also specify the variables using y, X, east, and north for outcome, explanatory, west-east coordinates, and north-south coordinates variables, respectively. This alternative specification is compatible with the one used in the early version of this package.

n.iter is the number of iterations to sample from the posterior distribution using the Metropolis-Hastings algorithm. This defaults to 100 iterations, but many more iterations would normally be preferred. n.burnin is set to 0 by default to preserve all the iterations since the kriging model usually takes a relatively long time to run. Users can set a number for burnin or use burnin function afterwards to discard the burnin period. The output of the function prints the proportion of candidate values for the coefficients and for the variance terms accepted by the Metropolis-Hastings algorithm. Particularly low or high acceptance rates respectively may indicate slow mixing (requiring more iterations) or a transient state (leading to nonconvergence), so additional messages will print for extreme acceptance rates. Users may want to adjust the tuning parameters b.tune, nugget.tune, or psill.tune, or perhaps the tolerance parameter range.tol if the acceptance rate is too high or too low.

The function returns a "krige" list object including the output MCMC matrix of sampled values from the posterior distribution as well as the record of function arguments, model frame, acceptance rates, and standing parameters. Users can use the generic summary function to summarize the results or extract the elements of the object for further use.

Value

An object of class krige that includes the output MCMC matrix of sampled values from the posterior distribution as well as the record of function arguments, model frame, acceptance rates, and standing parameters.

References

Jeff Gill. 2020. Measuring Constituency Ideology Using Bayesian Universal Kriging. *State Politics & Policy Quarterly*. doi:10.1177/1532440020930197

```
## Not run:
# Summarize example data
summary(ContrivedData)
# Initial OLS model
contrived.ols<-lm(y^x.1+x.2,data=ContrivedData)
# summary(contrived.ols)
# Set seed
set.seed(1241060320)
#For simple illustration, we set to few iterations.
#In this case, a 10,000-iteration run converges to the true parameters.
#If you have considerable time and hardware, delete the # on the next line.
#10,000 iterations took 39 min. with 8 GB RAM & a 1.5 GHz Quad-Core processor.
M <- 100
#M<-10000
contrived.run <- metropolis.krige(y \sim x.1 + x.2, coords = c("s.1", "s.2"),
  data = ContrivedData, n.iter = M, n.burnin=20, range.tol = 0.05)
# Alternatively, use burnin() after estimation
#contrived.run <- burnin(contrived.run, n.burnin=20)</pre>
# Summarize the results and examine results against true coefficients
summary(contrived.run)
(TRUTH < -c(0.5, 2.5, 0.5, 0, 1, 2))
# Extract the MCMC matrix of the posterior distribution
contrived.run.mat <- mcmc.samples(contrived.run)</pre>
head(contrived.run.mat)
# Diagnostics
geweke(contrived.run, early.prop=0.5)
heidel.welch(contrived.run)
# Semivariogram
### Semivariance
semivariance(contrived.run)
### Plot semivariogram
semivariogram(contrived.run)
### Alternatively, use generic plot() on a krige object
plot(contrived.run)
## End(Not run)
```

NYcity_subset 23

NYcity_subset

New York City CCES Respondents in 2008

Description

These data are a subset of the 2008 Cooperative Congressional Election Survey (CCES) Common Content. Only 568 respondents from New York City are included, with predictors drawn from Gill's (2020) model of self-reported ideology. The CCES data are merged with predictors on geographic location based on ZIP codes (from ArcGIS & TomTom) and county ruralism (from the USDA).

Format

The NYcity_subset dataset has 568 observations and 26 variables.

state The state abbreviation of the respondent's residence.

zip The respondent's ZIP code.

age The age of the respondent in years.

female An indicator of whether the respondent is female.

ideology The respondent's self-reported ideology on a scale of 0 (liberal) to 100 (conservative).

educ The respondent's level of education. 0=No Highschool, 1=High School Graduate, 2=Some College, 3=2-year Degree, 4=4-year degree, 5=Post-Graduate.

race The respondent's race. 1=White, 2=African American, 3=Nonwhite & nonblack.

empstat The respondent's employment status. 1=employed, 2=unemployed, 3=not in workforce.

ownership Indicator for whether the respondent owns his or her own home.

inc14 The respondent's self reported income. 1=Less than \$10,000, 2=\$10,000-\$14,999, 3=\$15,000-\$19,000, 4=\$20,000-\$24,999, 5=\$25,000-\$29,999, 6=\$30,000-\$39,999, 7=\$40,000-\$49,999, 8=\$50,000-\$59,999, 9=\$60,000-\$69,999, 10=\$70,000-\$79,999, 11=\$80,000-\$89,999, 12=\$100,000-\$119,999, 13=\$120,000-\$149,999, 14=\$150,000 or more.

catholic Indicator for whether the respondent is Catholic.

mormon Indicator for whether the respondent is Mormon.

orthodox Indicator for whether the respondent is Orthodox Christian.

jewish Indicator for whether the respondent is Jewish.

islam Indicator for whether the respondent is Muslim.

mainline Indicator for whether the respondent is Mainline Christian.

evangelical Indicator for whether the respondent is Evangelical Christian.

FIPS_Code FIPS code of the repondent's state.

rural Nine-point USDA scale of the ruralism of each county, with 0 meaning the most urban and 8 meaning the most rural.

zipPop Indicates the population of the repondent's ZIP code.

zipLandKM Indicates the land area in square kilometers of the repondent's ZIP code.

weight Survey weights created by the CCES.

24 NYcity_subset

cd The congressional district the respondent resides in.

fipsCD Index that fuses the state FIPS code in the first two digits and the congressional district number in the last two digits.

northings Indicates the geographical location of the respondent in kilometer-based northings. eastings Indicates the geographical location of the respondent in kilometer-based eastings.

Source

```
Ansolabehere, Stephen. 2011. "CCES, Common Content, 2008." Ver. 4.

ArcGIS. 2012. "USA ZIP Code Areas." https://www.arcgis.com/home/item.html?id=8d2012a2016e484dafaac0451f9
United States Department of Agriculture. 2013. "2013 Rural-Urban Continuum Codes." https://www.ers.usda.gov/data-products/rural-urban-continuum-codes.aspx
```

References

Jeff Gill. 2020. Measuring Constituency Ideology Using Bayesian Universal Kriging. *State Politics & Policy Quarterly*. doi:10.1177/1532440020930197

```
## Not run:
nyc <- NYcity_subset</pre>
#data cleaning
nyc$cathOrth<-nyc$catholic+nyc$orthodox
nyc$consRelig<-nyc$mormon+nyc$evangelical
nyc$jewMus<-nyc$jewish+nyc$islam
# Explanatory Variable Matrix
psrm.data <-cbind(nyc$age, nyc$educ, I(nyc$age*nyc$educ), as.numeric(nyc$race==2),</pre>
       as.numeric(nyc$race==3), nyc$female, I(as.numeric(nyc$race==2)*nyc$female),
       I(as.numeric(nyc$race==3)*nyc$female), nyc$cathOrth, nyc$consRelig,
       nyc$jewMus, nyc$mainline, nyc$rural, nyc$ownership,
       as.numeric(nyc$empstat==2), as.numeric(nyc$empstat==3),nyc$inc14)
dimnames(psrm.data)[[2]] <- c("Age", "Education", "Age.education",</pre>
                              "African. American", "Nonwhite. nonblack", "Female",
                              "African.American.female", "Nonwhite.nonblack.female",
                              "Catholic.Orthodox", "Evang.Mormon", "Jewish.Muslim",
                              "Mainline", "Ruralism", "Homeowner", "Unemployed",
                              "Not.in.workforce", "Income")
# Outcome Variable
ideo <- matrix(nyc$ideology,ncol=1)</pre>
# WARNING: This example was tuned on Amazon Web Services (EC2) over many hours
# with 150,000 iterations--a strain in 2020 for most desktop machines.
# A test with few iterations allows illustration.
#M<-150000
```

NY_subset 25

```
M<-150
set.seed(1,kind="Mersenne-Twister")
# Estimate the Model
nyc.fit <- metropolis.krige(formula = ideo ~ psrm.data, coords = cbind(nyc$eastings, nyc$northings),</pre>
          powered.exp=1, n.iter=M, spatial.share=0.31,range.share=0.23,beta.var=10,
          range.tol=0.01, b.tune=0.1, nugget.tune=20, psill.tune=5)
# Discard first 20% of Iterations as Burn-In (User Discretion Advised).
nyc.fit <- burnin(nyc.fit, M/5)</pre>
# Summarize Results
summary(nyc.fit)
#Convergence Diagnostics: Geweke and Heidelberger-Welch
geweke(nyc.fit)
heidel.welch(nyc.fit)
# Draw Semivariogram
semivariogram(nyc.fit)
## End(Not run)
```

NY_subset

New York State CCES Respondents in 2008

Description

These data are a subset of the 2008 Cooperative Congressional Election Survey (CCES) Common Content. Only 1108 respondents from the state of New York are included, with predictors drawn from Gill's (2020) model of self-reported ideology. The CCES data are merged with predictors on geographic location based on ZIP codes (from ArcGIS & TomTom) and county ruralism (from the USDA).

Format

The NY_subset dataset has 1108 observations and 26 variables.

state The state abbreviation of the respondent's residence.

zip The respondent's ZIP code.

age The age of the respondent in years.

female An indicator of whether the respondent is female.

ideology The respondent's self-reported ideology on a scale of 0 (liberal) to 100 (conservative).

educ The respondent's level of education. 0=No Highschool, 1=High School Graduate, 2=Some College, 3=2-year Degree, 4=4-year degree, 5=Post-Graduate.

race The respondent's race. 1=White, 2=African American, 3=Nonwhite & nonblack.

empstat The respondent's employment status. 1=employed, 2=unemployed, 3=not in workforce.

26 NY_subset

ownership Indicator for whether the respondent owns his or her own home.

inc14 The respondent's self reported income. 1=Less than \$10,000, 2=\$10,000-\$14,999, 3=\$15,000-\$19,000, 4=\$20,000-\$24,999, 5=\$25,000-\$29,999, 6=\$30,000-\$39,999, 7=\$40,000-\$49,999, 8=\$50,000-\$59,999, 9=\$60,000-\$69,999, 10=\$70,000-\$79,999, 11=\$80,000-\$89,999, 12=\$100,000-\$119,999, 13=\$120,000-\$149,999, 14=\$150,000 or more.

catholic Indicator for whether the respondent is Catholic.

mormon Indicator for whether the respondent is Mormon.

orthodox Indicator for whether the respondent is Orthodox Christian.

jewish Indicator for whether the respondent is Jewish.

islam Indicator for whether the respondent is Muslim.

mainline Indicator for whether the respondent is Mainline Christian.

evangelical Indicator for whether the respondent is Evangelical Christian.

FIPS_Code FIPS code of the repondent's state.

rural Nine-point USDA scale of the ruralism of each county, with 0 meaning the most urban and 8 meaning the most rural.

zipPop Indicates the population of the repondent's ZIP code.

zipLandKM Indicates the land area in square kilometers of the repondent's ZIP code.

weight Survey weights created by the CCES.

cd The congressional district the respondent resides in.

fipsCD Index that fuses the state FIPS code in the first two digits and the congressional district number in the last two digits.

northings Indicates the geographical location of the respondent in kilometer-based northings.

eastings Indicates the geographical location of the respondent in kilometer-based eastings.

Source

```
Ansolabehere, Stephen. 2011. "CCES, Common Content, 2008." Ver. 4.

ArcGIS. 2012. "USA ZIP Code Areas." https://www.arcgis.com/home/item.html?id=8d2012a2016e484dafaac0451f9
United States Department of Agriculture. 2013. "2013 Rural-Urban Continuum Codes." https://www.ers.usda.gov/data-products/rural-urban-continuum-codes.aspx
```

References

Jeff Gill. 2020. Measuring Constituency Ideology Using Bayesian Universal Kriging. *State Politics & Policy Quarterly*. doi:10.1177/1532440020930197

```
## Not run:
ny <- NY_subset

#data cleaning
ny$cathOrth<-ny$catholic+ny$orthodox
ny$consRelig<-ny$mormon+ny$evangelical</pre>
```

predict.krige 27

```
ny$jewMus<-ny$jewish+ny$islam
# Explanatory Variable Matrix
psrm.data <-cbind(ny$age, ny$educ, I(ny$age*ny$educ), as.numeric(ny$race==2),</pre>
       as.numeric(ny$race==3), ny$female, I(as.numeric(ny$race==2)*ny$female),
       I(as.numeric(ny$race==3)*ny$female), ny$cathOrth, ny$consRelig,
       ny$jewMus, ny$mainline, ny$rural, ny$ownership,
       as.numeric(ny$empstat==2), as.numeric(ny$empstat==3),ny$inc14)
dimnames(psrm.data)[[2]] <- c("Age", "Education", "Age.education",</pre>
                               "African.American", "Nonwhite.nonblack", "Female",
                               "African.American.female", "Nonwhite.nonblack.female",
                               "Catholic.Orthodox", "Evang.Mormon", "Jewish.Muslim", "Mainline", "Ruralism", "Homeowner", "Unemployed",
                               "Not.in.workforce", "Income")
# Outcome Variable
ideo <- matrix(ny$ideology,ncol=1)</pre>
# Set Number of Iterations:
# WARNING: 20 iterations is intensive on many machines.
# This example was tuned on Amazon Web Services (EC2) over many hours
# with 20,000 iterations--unsuitable in 2020 for most desktop machines.
#M<-20000
M<-100
set.seed(1,kind="Mersenne-Twister")
# Estimate the Model
ny.fit <- metropolis.krige(formula = ideo ~ psrm.data, coords = cbind(ny$eastings, ny$northings),</pre>
          powered.exp=1, n.iter=M, spatial.share=0.31,range.share=0.23,beta.var=10,
          range.tol=0.01, b.tune=0.1, nugget.tune=20, psill.tune=5)
# Discard first 20% of Iterations as Burn-In (User Discretion Advised).
ny.fit <- burnin(ny.fit, M/5)</pre>
# Summarize Results
summary(ny.fit)
#Convergence Diagnostics: Geweke and Heidelberger-Welch
geweke(ny.fit)
heidel.welch(ny.fit)
# Draw Semivariogram
semivariogram(ny.fit)
## End(Not run)
```

28 predict.krige

Description

This function uses the results of a model estimated by metropolis.krige to make kriging-based predictions.

Usage

```
## S3 method for class 'krige'
predict(object, newdata, credible = FALSE, new.X, new.east, new.north, ...)
```

Arguments

object	An krige object estimated by metropolis.krige.
newdata	An optional data frame in which to look for variables with which to predict. If omitted, the fitted values are produced. Alternatively, the new data can be specified using new.X, new.east, and new.north.
credible	If a credible interval on predictions is desired, a user may specify a proportion between 0 and 1 to indicate the interval probability. For example, a value of 0.9 would create a 90% credible interval. If NULL, then no credible interval will be produced.
new.X	The matrix of independent variables for observations to be predicted.
new.east	Vector of eastings for observations to be predicted.
new.north	Vector of northings for observations to be predicted.
	Additional arguments passed to predict methods. Not supported for krige

Details

objects.

Analysts should use this function if they want to make kriged predictions for observations at new locations or predict fitted values at original locations. To do this, researchers first must estimate a model using the metropolis.krige function.

After estimating the model, a krige object can provide information from the model fitted with metropolis.krige, including the original imput data, coordinates, and the model results themselves. The prediction will also use the same powered.exp. new.data can be specified for predicting the observations at new location. Otherwise, the fitted values for the original data and locations will be produced.

By default, the function uses median values of parameters to make a single point prediction for every kriged data point. However, if the uses specifies a probability with the credible option, then the function will determine the predictions for all iterations of the MCMC sample. The point estimates will then be a median of these predictions, and a credible interval will be returned based on percentiles. Note that estimating a credible interval is substantially more intensive computationally, but has the benefit of reporting uncertainty in predictions.

predict.krige 29

Value

An object of class matrix with one prediction per row. By default the matrix has one column, as only point predictions are returned. If the credible option is specified, there are three columns respectively indicating a point estimate (median prediction from MCMC), lower bound of the credible interval, and upper bound of the credible interval.

References

Jeff Gill. 2020. Measuring Constituency Ideology Using Bayesian Universal Kriging. *State Politics & Policy Quarterly*. doi:10.1177/1532440020930197

```
## Not run:
# Summarize Data
summary(ContrivedData)
# Initial OLS model
contrived.ols<-lm(y^x.1+x.2, data=ContrivedData)
# summary(contrived.ols)
# Set seed
set.seed(1241060320)
M <- 100
#M<-10000
contrived.run <- metropolis.krige(y \sim x.1 + x.2, coords = c("s.1", "s.2"),
   data = ContrivedData, n.iter = M, range.tol = 0.05)
# Predict fitted values
predict(contrived.run)
# Predict new data
euler<-c(0.2, 0.7)
archimedes < -c(0.3, 0.1)
pythagoras < -c(0.1, 0.4)
mathematicians<-rbind(euler,archimedes,pythagoras)</pre>
basel<-c(0.1,0.8)
sicily < -c(0.4, 0.1)
samos < -c(0.1, 0.4)
new.locations<-rbind(basel, sicily, samos)</pre>
newDf <- as.data.frame(cbind(mathematicians, new.locations))</pre>
colnames(newDf) <- c("x.1", "x.2", "s.1", "s.2")</pre>
# Make predictions from median parameter values:
(median.pred <- predict(contrived.run, newdata = newDf))</pre>
# Make predictions with 90\
(cred.pred <- predict(contrived.run, newdata = newDf, credible=0.9))</pre>
## End(Not run)
```

30 semivariance

semivariance

Semivariance for Geospatial Data

Description

This function computes the empirical semivariance for a spatially-distributed variable. Based on the user's chosen level of coarsening, the semivariance is presented for various distances.

Usage

```
semivariance(object, ...)
## S3 method for class 'krige'
semivariance(object, bins = 13, terms = "all", plot = FALSE, ...)
## S3 method for class 'lm'
semivariance(
    object,
    bins = 13,
    coords,
    terms = c("raw", "residual"),
    east,
    north,
    plot = FALSE,
    ...
)

## Default S3 method:
semivariance(object, bins = 13, coords, data, east, north, plot = FALSE, ...)
```

Arguments

object	An object for which the semivariance is desired. The object can be a krige object, a lm object, or a vector of variables (or variable names in the data).
	Additional arguments passed to semivariance methods.
bins	Number of bins into which distances should be divided. The observed distances will be split at equal intervals, and the semivariance will be computed within each interval. Defaults to 13 intervals.
terms	A vector of strings specifies for which the semivariogram is created. Options are "raw" (the semivariogram for raw data), "residual" (the semivariogram for residuals from linear regression).
plot	Logical values indicates whether a graph of the empirical semivariogram should be presented with a run of the function. Default omits the plot and only returns semivariance values. See semivariogram for additional plotting functions.

semivariance 31

coords	A matrix of coordinates for all observations or a vector of variable names indi- cating the coordinates variables in the data. Alternatively, the coordinates can
	also be specified separately using east and north.
east	Alternative specification for the vector of eastings for all observations.
north	Alternative specification for the vector of northing for all observations.
data	If object is a variable name, a data frame must be provided.

Details

Semivariance is equal to half of the variance of the difference in a variable's values at a given distance. That is, the semivariance is defined as: $\gamma(h) = 0.5 * E[X(s+h) - X(s)]^2$, where X is the variable of interest, s is a location, and h is the distance from s to another location.

The function can be applied to a variable, a fitted linear model (1m object) before fitting a spatial model or to a krige object or semivariance object to assess the model fit. When applying to a variable, it will describes the raw data; for a 1m object, the default will present empirical semivariogram for both the raw data and linear residuals. Users can also specify which semivariance is needed in the terms argument if there are multiple kinds of semivariogram can be plotted. A semivariance object can also be used to create semivariogram afterwards using generic plot function with more options.

Value

A semivariance object. It will be a numeric vector with each bin's value of the semivariance if only one kind of semivariance is computed; a list including different kinds of semivariance if both raw and residual semivariance is computed.

References

Sudipto Banerjee, Bradley P. Carlin, and Alan E. Gelfand. 2015. *Hierarchical Modeling and Analysis for Spatial Data*. 2nd ed. Boca Raton, FL: CRC Press.

See Also

semivariogram, plot.semivariance, exponential.semivariance

```
## Not run:
# Summarize example data
summary(ContrivedData)

# Empirical semivariance for variable y
semivariance(ContrivedData$y,coords = cbind(ContrivedData$s.1, ContrivedData$s.2))

# Initial OLS Model
contrived.ols<-lm(y~x.1+x.2,data=ContrivedData); summary(contrived.ols)

# Empirical semivariance for ols fit
(sv.ols <- semivariance(contrived.ols, coords = c("s.1","s.2"), bins=13))</pre>
```

32 semivariogram

```
plot(sv.ols)

# Estimation using metropolis.krige()

# Set seed
set.seed(1241060320)

M <- 100

contrived.run <- metropolis.krige(y ~ x.1 + x.2, coords = c("s.1","s.2"),
    data = ContrivedData, n.iter = M, range.tol = 0.05)

# Parametric semivariance
(sv.krige <- semivariance(contrived.run, plot = TRUE))

# Convert to other format for further use
as.matrix(sv.krige)
as.data.frame(sv.krige)

## End(Not run)</pre>
```

semivariogram

Semivariogram for Geospatial Data

Description

This function creates semivariogram plots. It creates empirical semivariogram for raw data and 1m object or parametric exponential semivariogram based on the estimation from metropolis.krige. Based on the user's chosen level of coarsening, the semivariogram is presented for various distances.

Usage

semivariogram 33

```
type,
  legend,
  col,
  pch,
 lty
)
## Default S3 method:
semivariogram(
  х,
  . . . ,
  coords,
  data,
 bins = 13,
  east,
  north,
  type,
  pch,
  lty,
  col
)
## S3 method for class 'semivariance'
semivariogram(x, ..., type, pch, lty, legend, col)
## S3 method for class 'semivariance'
plot(x, ..., type, pch, lty, legend, col)
```

Arguments

bins

terms

type

pch

An object for which a semivariogram is desired. The object can be a krige object, a semivariance object, a lm object, or a vector of variables (or variable names in the data).

Additional arguments to be passed to semivariogram methods. Further arguments that can passed to plot() function can be specified here.

Number of bins into which distances should be divided. The observed distances will be split at equal intervals, and the semivariance will be computed within each interval. Defaults to 13 intervals.

A vector of strings specifies for which the semivariogram is created. Options are "raw" (the semivariogram for raw data), "residual" (the semivariogram for residuals from linear regression). "parametric" (the parametric powered exponential semivariogram based on the estimation from metropolis.krige). Defaults will create all the applicable plots.

A vector specify the type of plots for each term. Options are "l" (line plot) and "p" (scatter plot). Defaults to c(raw = "p", residual = "p", parametric = "l")

A vector specify the points symbols for scatter plot. Suppressed for line plot.

34 semivariogram

lty	A vector specify the line type for line plot. Suppressed for scatter plot.
legend	A logical argument for whether legend should be presented. Defaults to TRUE.
col	A vector specify the color for each term. Defaults to c(raw = "black", residual = "blue", parametric = "red")
coords	A matrix of coordinates for all observations or a vector of variable names indicating the coordinates variables in the data. Alternatively, the coordinates can also be specified separately using east and north.
east	Alternative specification for the vector of eastings for all observations.
north	Alternative specification for the vector of northing for all observations.
data	If object is a variable name, a data frame must be provided.

Details

The function creates semivariograms for diagnosing the spatial relationship that best describes the data and for diagnosing the degree to which the model fits the spatial relationship. With a view of the empirical semivariogram, a user can consult images of parametric semivariograms to determine whether an exponential, Gaussian, or other powered expoential function fit the data well, or if another style of semivariogram works better. Examining this also allows the user to develop priors such as the approximate split in variance between the nugget and partial sill as well as the approximate distance of the effective range. Semivariograms are explicitly tied to a corresponding spatial correlation function, so determining the former automatically implies the latter. See Banerjee, Carlin, and Gelfand for a fuller explanation, as well as a guidebook to semivariogram diagnosis (2015, 26-30).

The function can be applied to a variable, a fitted linear model (1m object) before fitting a spatial model or to a krige object or semivariance object to assess the model fit. When applying to a variable, it will describes the raw data; for a 1m object, the default will present empirical semivariogram for both the raw data and linear residuals; when applying to a krige object, the default will present empirical semivariogram for the raw data and the residuals from linear fit, and the parametric semivariogram given the estimates from the geospatial model fitted in metropolis.krige; for a semivariance object, it will present a plot(s) for whichever the semivariance is calculated. Users can also specify which semivariogram is needed in the terms argument if there are multiple kinds of semivariogram can be plotted. The plots are compatible to the arguments used in base R base graphics.

Value

An semivariogram plot. For krige object, it will return empirical semivariograms for raw data and residuals of linear regression as well as a parametric powered exponential semivariogram given the values of the estimates from metropolis.krige as default.

References

Sudipto Banerjee, Bradley P. Carlin, and Alan E. Gelfand. 2015. *Hierarchical Modeling and Analysis for Spatial Data*. 2nd ed. Boca Raton, FL: CRC Press.

See Also

semivariance, exponential.semivariance

stateCombined 35

Examples

```
## Not run:
# Summarize Data
summary(ContrivedData)
# Empirical semivariagram for variable y
semivariogram(x=ContrivedData$y, coords = cbind(ContrivedData$s.1, ContrivedData$s.2))
# Initial OLS Model
contrived.ols<-lm(y~x.1+x.2,data=ContrivedData)</pre>
# Empirical semivariagram for ols fit
semivariogram(contrived.ols, coords = c("s.1", "s.2"), bins=13)
# Set seed
set.seed(1241060320)
M <- 100
#M<-10000
contrived.run <- metropolis.krige(y \sim x.1 + x.2, coords = c("s.1", "s.2"),
  data = ContrivedData, n.iter = M, range.tol = 0.05)
# Parametric semivariagram
semivariogram(contrived.run, bins=13, terms = c("raw", "residual", "parametric"),
 type= c(raw = "p", residual = "p", parametric = "l"), legend = TRUE, col = c("black",
  "blue", "red"), pch = c(1,3,NA), lty = c(NA,NA,1))
# Alternatively, the generic function plot can also be applied to krige object
plot(contrived.run)
# Plot semivariance object
plot(semivariance(contrived.run, bins=13))
## End(Not run)
```

stateCombined

State Public Opinion Ideology in 2010

Description

These data present measures of ideology in 2010 for the 50 American states, recorded as the variable krige.state. Forecasts are based on a kriging model fitted over the 2008 Cooperative Congressional Election Survey (CCES), paired with predictive data from the 2010 Census. Each state is listed twice, as each state's public ideology is paired with the DW-NOMINATE common space score of each of its two senators in 2011 (update from McCarty, Poole and Rosenthal 1997).

36 stateCombined

Format

The stateCombined dataset has 100 observations (2 each for 50 states) and 13 variables.

STATEA The FIPS code for the state.

krige.state The ideology of the average citizen in the state.

krige.state.var The variance of ideology among the state's citizens.

cong The term of Congress studied-112 for this dataset.

idno Identification number for the senator-ICPSR numbers continued by Poole & Rosenthal.

state The ICPSR code for the state.

cd The congressional district number-0 for senators.

statenm The first seven letters of the state's name.

party Political party of the senator. 100=Democrat, 200=Republican, 328=Independent.

name Last name of the senator, followed by first name if ambiguous.

dwnom1 First dimension DW-NOMINATE common space score for the senator. Higher values are usually interpreted as more right-wing, with lower values as more left-wing.

stateCD Combined index of STATEA followed by cd.

obama Barack Obama's percentage of the two-party vote in the state in 2012.

Source

Ansolabehere, Stephen. 2011. "CCES, Common Content, 2008." Ver. 4.

McCarty, Nolan M., Keith T. Poole and Howard Rosenthal. 1997. *Income Redistribution and the Realignment of American Politics*. American Enterprise Institude Studies on Understanding Economic Inequality. Washington: AEI Press.

Minnesota Population Center. 2011. *National Historical Geographic Information System: Version* 2.0. Minneapolis, MN: University of Minnesota. 'https://www.nhgis.org'

References

Jeff Gill. 2020. Measuring Constituency Ideology Using Bayesian Universal Kriging. *State Politics & Policy Quarterly*. doi:10.1177/1532440020930197

summary.krige 37

summary.krige

Summarize Fitted Kriging Model

Description

Create a summary of a estimated model from metropolis.krige

Usage

```
## S3 method for class 'krige'
summary(object, ...)
```

Arguments

object An krige object from the metropolis.krige function.

... Additional arguments passed to summary methods. Not supported for krige

object.

Details

The function creates a summary of the model estimated by metropolis.krige. The output includes both the parameters and estimates of the model.

Value

A summary.krige list object.

See Also

```
as.mcmc.summary.krige
```

```
## Not run:
# Summarize data
summary(ContrivedData)

# Initial OLS model
contrived.ols<-lm(y~x.1+x.2,data=ContrivedData)
# summary(contrived.ols)

# Set seed
set.seed(1241060320)

#For simple illustration, we set to few iterations.
#In this case, a 10,000-iteration run converges to the true parameters.</pre>
```

38 update.krige

```
#If you have considerable time and hardware, delete the # on the next line.
#10,000 iterations took 39 min. with 8 GB RAM & a 1.5 GHz Quad-Core processor.
M <- 100
#M<-10000

contrived.run <- metropolis.krige(y ~ x.1 + x.2, coords = c("s.1","s.2"),
    data = ContrivedData, n.iter = M, range.tol = 0.05)

# Summary
summary(contrived.run)
## End(Not run)</pre>
```

update.krige

Update Model

Description

Update the Markov chain associated with the metropolis.krige model

Usage

```
## S3 method for class 'krige'
update(object, n.iter, n.burnin = 0, combine = FALSE, ...)
```

Arguments

object An krige object from the metropolis.krige function.

n.iter Number of iterations for the update run.

The number of burnin iterations. Defaults to 0.

Logical value indicate whether to combine the update run with original output.

Additional arguments passed to update methods. Not supported for krige objects.

Details

Since MCMC calculations typically need to run relatively long. This function can continue the MCMC calculations by metropolis.krige(). The parameters of the original model and the estimated results from the previous run are passed through the krige object.

As geospatial estimation can be computationally taxing, the users may want to preserve more iterations of the posterior samples. The combine argument can be used to indicate whether combine the updated run with previous results. This includes both the posterior samples and acceptance rates.

Value

An object of class krige that includes the output MCMC matrix of sampled values from the posterior distribution as well as the record of function arguments, model frame, acceptance rates, and standing parameters.

upperCombined 39

Examples

```
## Not run:
# Summarize Data
summary(ContrivedData)

# Set seed
set.seed(1241060320)

M <- 100
#M<-10000

contrived.run <- metropolis.krige(y ~ x.1 + x.2, coords = c("s.1","s.2"),
    data = ContrivedData, n.iter = M, range.tol = 0.05)
summary(contrived.run)

# Update run
contrived.run2 <- update(contrived.run, n.iter = M, combine = TRUE)
summary(contrived.run2)
#plot(contrived.run2)
## End(Not run)</pre>
```

upperCombined

State Legislative District (Upper Chambers) Public Opinion Ideology in 2010

Description

These data present measures of ideology in 2010 for the districts for upper chambers of state legislatures, recorded as the variable krige.upper. All 50 states' chambers are covered (including the Nebraska Unicameral). Forecasts are based on a kriging model fitted over the 2008 Cooperative Congressional Election Survey (CCES), paired with predictive data from the 2010 Census. Each district's public ideology is paired with a measure of the ideology of the State Senate member from the district (update from Shor and McCarty 2011).

Format

The upperCombined dataset has 1989 observations and 10 variables.

st Two-letter postal abbreviation for the state.

upper The state legislative district number (upper chamber).

STATEA The FIPS code for the state.

krige.upper The ideology of the average citizen in the district.

upperKluge Combined index of STATEA followed by upper.

krige.upper.var The variance of ideology among the district's citizens.

40 WVwells

name Last name of the state legislator, followed by first name and middle initial.

party Political party of the legislator. D=Democrat, R=Republican, X=Other.

st_id Temporary identifer variable. DO NOT USE.

np_score Ideology score for the state legislator (upper chamber). Higher values are usually interpreted as more right-wing, with lower values as more left-wing.

Source

Ansolabehere, Stephen. 2011. "CCES, Common Content, 2008." Ver. 4.

Minnesota Population Center. 2011. *National Historical Geographic Information System: Version* 2.0. Minneapolis, MN: University of Minnesota. 'https://www.nhgis.org'

Shor, Boris and Nolan M. McCarty. 2011. "The Ideological Mapping of American Legislatures." *American Political Science Review* 105(3):530-551.

References

Jeff Gill. 2020. Measuring Constituency Ideology Using Bayesian Universal Kriging. *State Politics & Policy Quarterly*. doi:10.1177/1532440020930197

Examples

WVwells

West Virginia Oil and Gas Production in 2012

Description

These data are a subset of the West Virginia Geological and Economic Survey of 2014. They contain information on the coordinates of wells that yielded at least some quantity of natural gas in 2012. In addition to coordinates, the data contain information on well ownership and operation, rock pressure at the well, elevation of the well, oil production, and gas production.

Format

The WVwells dataset has 1949 observations and 18 variables.

APINum A 10-digit number in the format assigned by the American Petroleum Institute (API), consisting of a 2-digit state code, a 3-digit county code with leading zeroes, and a 5-digit permit number with leading zeroes. Data Source: West Virginia Department of Environmental Protection, Office of Oil & Gas (WVDEP-OOG).

41

- CntyCode A 3-digit numeric code, assigned in numeric order by county name. Data Source: The county code for a well is assigned by WVDEP-OOG, based on the well location.
- CntyName The name of the county. Please see CntyCode (County Code) for a list of all West Virginia county names. Data Source: The county code for a well is assigned by WVDEP-OOG, based on the well location. The county name is a translation of the county code.
- Operator The name of the operator who owns the well at the time of reporting. Data Source: WVDEP-OOG plat; verified on the WR-35 completion record.
- SurfaceOwn The name of the owner of the surface property on which the well is located. Data Source: WVDEP-OOG plat; verified on the WR-35 completion record.
- MineralOwn Mineral Owner: The name of the owner of the mineral rights where the well is located. Data Source: WVDEP-OOG plat.
- CompanyNum The operator's serial number for the well. Data Source: WVDEP-OOG plat; verified on the WR-35 completion record.
- WellNum The operator's number for the well on the surface property (farm). Data Source: WVDEP-OOG plat; verified on the WR-35 completion record.
- UTMESrf Surface Location—Universal Transverse Mercator, Easting: The well location at the surface measured in meters to one decimal point, east of the central meridian in UTM Zone 17; datum: NAD83. Data Source: Taken directly from the plat if given as such. Otherwise, computed from the location reported on the plat. Suspect locations may be adjusted using various additional resources (e.g. topographic maps) if deemed necessary.
- UTMNSrf Surface Location—Universal Transverse Mercator, Northing: The well location at the surface measured in meters to one decimal point, north of the equator in UTM Zone 17; datum: NAD83. Data Source: Taken directly from the plat if given as such. Otherwise, computed from the location reported on the plat. Suspect locations may be adjusted using various additional resources (e.g. topographic maps) if deemed necessary.
- LonSrf Surface Location–Longitude: The well location at the surface measured to a precision of 6 decimal points, in degrees west of the Prime Meridian. Data Source: Taken directly from the plat if given as such. Otherwise, computed from the location reported on the plat. Suspect locations may be adjusted using various additional resources (e.g. topographic maps) if deemed necessary.
- LatSrf Surface Location–Latitude: The well location at the surface measured to a precision of 6 decimal points, in degrees north of the equator. Data Source: Taken directly from the plat if given as such. Otherwise, computed from the location reported on the plat. Suspect locations may be adjusted using various additional resources (e.g. topographic maps) if deemed necessary.
- Elevation Elevation: The height of the well in feet above mean sea level. Data Source: WVDEP-OOG plat; verified on the WR-35 completion record.

42 WVwells

RockPres Formation Rock Pressure at Surface: The pressure measured at the surface usually after stimulation, in pounds per square inch (psi). Data Source: WVDEP-OOG WR-35 comp#' letion record, submitted by the operator to WVDEP-OOG.

GProd2012 2012 Gas Production Reported: The total gas production for the well for 2012 in thousands of cubic feet (MCF); includes all pay zones. Data Source: Production data reported by the operator to the State regulatory authority for Oil and Gas (WVDEP-OOG); WVGES obtained the data from WVDEP-OOG.

OProd2012 2012 Oil Production Reported: The total oil production for the well for 2012 in barrels (Bbl); includes all pay zones. Production data reported by the operator to the State regulatory authority for Oil and Gas (WVDEP-OOG); WVGES obtained the data from WVDEP-OOG.

logElevation Logarithm of Elevation.

Source

West Virginia Geological and Economic Survey. 2014. "WVMarcellusWellsCompleted102014." Morgantown, WV. http://www.wvgs.wvnet.edu/www/datastat/devshales.htm Accessed via: FracTracker. 2019. "West Virginia Oil & Gas Activity." https://www.fractracker.org/map/us/west-virginia/

References

Jason S. Byers & Jeff Gill. N.D. "Applied Geospatial Data Modeling in the Big Data Era: Challenges and Solutions."

```
## Not run:
# Descriptive Statistics
summary(WVwells)
# Record means of predictors:
# These are used BOTH to eliminate the intercept and to recover predictions later.
mean.logGas<-mean(WVwells$logGProd2012);mean.logGas</pre>
mean.logElevation<-mean(WVwells$logElevation);mean.logElevation</pre>
mean.RockPres<-mean(WVwells$RockPres);mean.RockPres</pre>
# Outcome Variable, De-Meaned
WVwells$logGas <- WVwells$logGProd2012-mean.logGas
# Explanatory Variable: DE-MEANED PREDICTORS AND NO CONSTANT TERM
# Because we deducted the mean from all predictors and the outcome,
# it is valid to do regression through the origin.
WVwells$LogElevation <- WVwells$logElevation-mean.logElevation</pre>
WVwells$RockPressure <- WVwells$RockPres-mean.RockPres
# OLS Model
fracking.ols<-lm(logGas~LogElevation+RockPressure-1, data = WVwells)</pre>
summary(fracking.ols)
intercept.mod<-lm(logGProd2012~ logElevation+RockPres,data=WVwells)</pre>
```

WVwells 43

```
summary(intercept.mod)
# Set Number of Iterations:
# WARNING: 100 iterations is intensive on many machines.
# This example was tuned on Amazon Web Services (EC2) over many hours
# with 5,000 iterations--unsuitable in 2020 for most desktop machines.
#M<-5000
M<-20
set.seed(1000, kind="Mersenne-Twister")#SET SEED FOR CONSISTENCY
# Trial Run, Linear Model of Ideology with Geospatial Errors Using Metropolis-Hastings:
wv.fit <- metropolis.krige(logGas~LogElevation+RockPressure-1, coords = c("UTMESrf", "UTMNSrf"),</pre>
                           data = WVwells, n.iter=M, powered.exp=0.5, spatial.share=0.60,
                            range.share=0.31, beta.var=1000, range.tol=0.1, b.tune=1,
                           nugget.tune=1, psill.tune=30)
# Discard first 20% of Iterations as Burn-In (User Discretion Advised).
wv.fit <- burnin(wv.fit, M/5)</pre>
# Summarize Results
summary(wv.fit)
# Convergence Diagnostics
# geweke(wv.fit) Not applicable due to few iterations.
heidel.welch(wv.fit)
# Draw Semivariogram
semivariogram(wv.fit)
# Predictive Data for Two Wells Tapped in 2013
well.1<-c(log(1110)-mean.logElevation,1020-mean.RockPres)</pre>
well.2<-c(log(643)-mean.logElevation,630-mean.RockPres)</pre>
site.1<-c(557306.0, 4345265)
site.2<-c(434515.7, 4258449)
well.newdata <- as.data.frame(cbind(rbind(well.1,well.2),rbind(site.1,site.2)))</pre>
colnames(well.newdata)<-c("LogElevation", "RockPressure", "UTMESrf", "UTMNSrf")</pre>
# Make predictions from median parameter values:
(median.pred <- predict(wv.fit, newdata = well.newdata))</pre>
# Prediction in thousands of cubic feet (MCF):
round(exp(median.pred+mean.logGas))
# Make predictions with 90\
(cred.pred <- predict(wv.fit, newdata = well.newdata, credible = 0.9))</pre>
# Prediction in thousands of cubic feet (MCF) and the true yield in 2013:
Actual.Yield<-c(471171, 7211)
round(cbind(exp(cred.pred+mean.logGas),Actual.Yield))
## End(Not run)
```

Index

* data	krige, 13
congCombined, 5	krige.posterior, 13
ContrivedData, 7	
lowerCombined, 16	lowerCombined, 16
NY_subset, 25	
NYcity_subset, 23	mcmc.samples, 17
stateCombined, 35	metropolis.krige, 19
upperCombined, 39	NIV and and 05
WVwells, 40	NY_subset, 25
•	NYcity_subset, 23
as.data.frame.krige(mcmc.samples), 17	plot.krige(semivariogram), 32
as.data.frame.semivariance	plot.semivariance, 9, 31
(as.matrix.semivariance), 2	plot.semivariance(semivariogram), 32
as.data.frame.summary.krige	predict.krige, 27
(mcmc.samples), 17	predict. Krige, 27
as.matrix.krige (mcmc.samples), 17	semivariance, 30, 34
as.matrix.semivariance, 2	semivariogram, <i>9</i> , <i>30</i> , <i>31</i> , 32
as.matrix.summary.krige(mcmc.samples),	stateCombined, 35
17	summary.krige, 37
as.mcmc.krige, 3, <i>18</i>	3 7
as.mcmc.summary.krige, 37	update.krige,38
as.mcmc.summary.krige(as.mcmc.krige),3	upperCombined, 39
burnin, 5	WVwells, 40
coda::as.mcmc(), 4	
congCombined, 5	
ContrivedData,7	
exponential.semivariance, 8, 9, 31, 34	
formula, <i>19</i>	
geweke, 10, <i>12</i>	
geweke.krige, 11	
geweke.summary.krige, 11	
heidel.welch, 11	
heidel.welch.krige, 12	
heidel.welch.summary.krige, 12	