# Package 'logistf'

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      prior. Confidence intervals for regression coefficients can be computed by penalized profile like-
      lihood. Firth's method was proposed as ideal
      solution to the problem of separation in logistic regres-
      sion, see Heinze and Schemper (2002) <doi:10.1002/sim.1047>. If needed, the bias reduc-
      tion can be turned off such that ordinary
      maximum likelihood logistic regression is obtained. Two new modifica-
      tions of Firth's method, FLIC and FLAC, lead to unbiased predictions and are now available
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Firth's Bias-Reduced Logistic Regression

## **Description**

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Fits a binary logistic regression model using Firth's bias reduction method, and its modifications FLIC and FLAC, which both ensure that the sum of the predicted probabilities equals the number of events. If needed, the bias reduction can be turned off such that ordinary maximum likelihood logistic regression is obtained.

### Details

The package logistf provides a comprehensive tool to facilitate the application of Firth's correction for logistic regression analysis, including its modifications FLIC and FLAC.

The call of the main function of the library follows the structure of the standard functions as Im or glm, requiring a data.frame and a formula for the model specification. The resulting object belongs to the new class logistf, which includes penalized maximum likelihood (Firth-Logistic'- or FL'-type) logistic regression parameters, standard errors, confidence limits, p-values, the value of the maximized penalized log likelihood, the linear predictors, the number of iterations needed to arrive at the maximum and much more. Furthermore, specific methods for the resulting object are supplied. Additionally, a function to plot profiles of the penalized likelihood function and a function to perform penalized likelihood ratio tests have been included.

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In explaining the details of the estimation process we follow mainly the description in Heinze & Ploner (2003). In general, maximum likelihood estimates are often prone to small sample bias. To reduce this bias, Firth (1993) suggested to maximize the penalized log likelihood  $\log L(\beta)^* = \log L(\beta) + 1/2 \log |I(\beta)|$ , where  $I(\beta)$  is the Fisher information matrix, i. e. minus the second derivative of the log likelihood. Applying this idea to logistic regression, the score function  $U(\beta)$  is replaced by the modified score function  $U(\beta)^* = U(\beta) + a$ , where a has rth entry  $a_r = 0.5trI(\beta)^{-1}[dI(\beta)/d\beta_r], r = 1,...,k$ . Heinze and Schemper (2002) give the explicit formulae for  $I(\beta)$  and  $I(\beta)/d\beta_r$ .

In our programs estimation of  $\beta$  can be based on a Newton-Raphson algorithm or on iteratively reweighted least squares. Parameter values are initialized usually with 0, but in general the user can specify arbitrary starting values.

With a starting value of  $\beta^{(0)}$ , the penalized maximum likelihood estimate  $\beta$  is obtained iteratively via Newton-Raphson:

$$\beta^{(s+1)} = \beta^{(s)} + I(\beta^{(s)})^{-1}U(\beta^{(s)})^*$$

If the penalized log likelihood evaluated at  $\beta^{(s+1)}$  is less than that evaluated at  $\beta^{(s)}$ , then  $(\beta^{(s+1)})$  is recomputed by step-halving. For each entry r of  $\beta$  with r=1,...,k the absolute step size  $|\beta^{(s+1)}_r - \beta^s_r|$  is restricted to a maximal allowed value maxstep. These two means should avoid numerical problems during estimation. The iterative process is continued until the parameter estimates converge, i. e., until three criteria are met: the change in log likelihood is less than lconv, the maximum absolute element of the score vector is less than gconv, the maximum absolute change in beta is less than xconv. lconv, gconv, xconv can be controlled by control=logistf.control(lconv=..., gconv=...,xconv=...).

Computation of profile penalized likelihood confidence intervals for parameters (logistpl) follows the algorithm of Venzon and Moolgavkar (1988). For testing the hypothesis of  $\gamma = \gamma_0$ , let the likelihood ratio statistic

$$LR = 2[\log L(\gamma, \delta) - \log L(\gamma_0, \delta_{\gamma_0})^*]$$

where  $(\gamma, \delta)$  is the joint penalized maximum likelihood estimate of  $\beta = (\gamma, \delta)$ , and  $\delta_{\gamma_0}$  is the penalized maximum likelihood estimate of  $\delta$  when  $\gamma = \gamma_0$ . The profile penalized likelihood confidence interval is the continuous set of values  $\gamma_0$  for which LR does not exceed the  $(1-\alpha)100$ th percentile of the  $\chi^2_1$ -distribution. The confidence limits can therefore be found iteratively by approximating the penalized log likelihood function in a neighborhood of  $\beta$  by the quadratic function

$$l(\beta + \delta) = l(\beta) + \delta' U^* - 0.5\delta' I\delta$$

where 
$$U^* = U(\beta)^*$$
 and  $-I = -I(\beta)$ .

In some situations computation of profile penalized likelihood confidence intervals may be time consuming since the iterative procedure outlined above has to be repeated for the lower and for the upper confidence limits of each of the k parameters. In other problems one may not be interested in interval estimation, anyway. In such cases, the user can request computation of Wald confidence intervals and P-values, which are based on the normal approximation of the parameter estimates and do not need any iterative estimation process. Note that from version 1.24.1 on, the variance-covariance matrix is based on the second derivative of the likelihood of the augmented data rather than the original data, which proved to be a better approximation if the user chooses to set a higher value for  $\tau$ , the penalty strength.

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The adequacy of Wald confidence intervals for parameter estimates can be verified by plotting the profile penalized log likelihood (PPL) function. A symmetric shape of the PPL function allows use of Wald intervals, while an asymmetric shape demands profile penalized likelihood intervals (*Heinze & Schemper* (2002)). Further documentation can be found in *Heinze & Ploner* (2004).

The package includes functions to work with multiply imputed data sets, such as generated by the mice package. Results on individual fits can be pooled to obtain point and interval estimates, as well as profile likelihood confidence intervals and likelihood profiles in general (Heinze, Ploner and Beyea, 2013).

Moreover, in the package the modifications FLIC and FLAC have been implemented, which were described in Puhr et al (2017) as solutions to obtain accurate predicted probabilities.

#### Author(s)

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#### References

Firth D (1993). Bias reduction of maximum likelihood estimates. *Biometrika* 80, 27–38.

Heinze G, Schemper M (2002). A solution to the problem of separation in logistic regression. *Statistics in Medicine* 21: 2409-2419.

Heinze G, Ploner M (2003). Fixing the nonconvergence bug in logistic regression with SPLUS and SAS. *Computer Methods and Programs in Biomedicine* 71: 181-187.

Heinze G, Ploner M (2004). Technical Report 2/2004: A SAS-macro, S-PLUS library and R package to perform logistic regression without convergence problems. Section of Clinical Biometrics, Department of Medical Computer Sciences, Medical University of Vienna, Vienna, Austria. http://www.meduniwien.ac.at/user/georg.heinze/techreps/tr2\_2004.pdf

Heinze G (2006). A comparative investigation of methods for logistic regression with separated or nearly separated data. *Statistics in Medicine* 25: 4216-4226.

Heinze G, Ploner M, Beyea J (2013). Confidence intervals after multiple imputation: combining profile likelihood information from logistic regressions. *Statistics in Medicine* 32:5062-5076.

Puhr R, Heinze G, Nold M, Lusa L, Geroldinger A (2017). Firth's logistic regression with rare events: accurate effect estimates and predictions? *Statistics in Medicine* 36: 2302-2317.

Venzon DJ, Moolgavkar AH (1988). A method for computing profile-likelihood based confidence intervals. *Applied Statistics* 37:87-94.

add1.logistf

Add or Drop All Possible Single Terms to/from a logistf Model

## **Description**

Compute all the single terms in the scope argument that can be added to or dropped from the model, fit those models and compute a table of the changes in fit.

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### Usage

```
## S3 method for class 'logistf'
add1(object, scope, test = "PLR", ...)
```

## **Arguments**

object	A fitted logistf, flic or flac object
scope	The scope of variables considered for adding or dropping. Should be a vector of variable names. Can be left missing; the method will then use all variables in the object's data slot which are not identified as the response variable.
test	The type of test statistic. Currently, only the PLR test (penalized likelihood ratio test) is allowed for logistf fits.
	Further arguments passed to or from other methods.

### **Details**

drop1 and add1 generate a table where for each variable the penalized likelihood ratio chi-squared, the degrees of freedom, and the p-value for dropping/adding this variable are given.

## Value

A matrix with nvar rows and 3 columns (Chisquared, degrees of freedom, p-value).

## **Examples**

```
data(sex2)
fit<-logistf(data=sex2, case~1, pl=FALSE)
add1(fit, scope=c("dia", "age"))
fit2<-logistf(data=sex2, case~age+oc+dia+vic+vicl+vis)
drop1(fit2)</pre>
```

anova.logistf

Analysis of Penalized Deviance for logistf Models

## Description

This method compares hierarchical and non-hierarchical logistf models using penalized likelhood ratio tests. It replaces the function logistftest of former versions of logistf.

## Usage

```
## S3 method for class 'logistf'
anova(object, fit2, formula, method = "nested", ...)
```

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#### **Arguments**

object A fitted logistf model object

fit2 Another fitted logistf model object, to be compared with object

formula Alternatively to fit2, a formula which specifies terms to omit from the object

model fit.

method One of c("nested", "PLR"). nested is the default for hierarchically nested mod-

els, and will compare the penalized likelihood ratio statistics (minus twice the difference between maximized penalized log likelihood and null penalized log likelihood), where the null penalized log likelihood is computed from the same, hierarchically superior model. Note that unlike in maximum likelihood analysis, the null penalized likelihood depends on the penalty (Jeffreys prior) which itself depends on the scope of variables of the hierarchically superior model. PLR compares the difference in penalized likelihood ratio between the two models, where for each model the null penalized likelihood is computed within the scope of variables in that model. For PLR, the models need not be hierarchically

nested.

... Further arguments passed to the method.

#### **Details**

Comparing models fitted by penalized methods, one must consider that the penalized likelihoods are not directly comparable, since a penalty is involved. Or in other words, inserting zero for some regression coefficients will not lead to the same penalized likelihood as if the corresponding variables are simply "unknown" to a model. The anova method takes care that the same penalty is used for two hierarchically nested models, and if the models are not hierarchically nested, it will first relate each penalized likelihood to its null penalized likelihood, and only compare the resulting penalized likelihod ratio statistics. The chi-squared approximation for this latter method (PLR) is considered less accurate than that of the nested method. Nevertheless, it is the only way to go for comparison of non-nested models.

#### Value

An object of class anova.logistf with items

chisq the chisquared statistic for the model comparison

df The degrees of freedom

pval The p-value

call The function call

method The method of comparison (input)

model1 The first model

model 2 The second model which was compared to the first model

PLR1 The PLR statistic of the first model

PLR2 the PLR statistic of the second model; for the nested method, this will be the

drop in chi-squared due to setting the coefficients to zero

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## **Examples**

```
data(sex2)
fit<-logistf(data=sex2, case~age+oc+dia+vic+vicl+vis)
#simultaneous test of variables vic, vicl, vis:
anova(fit, formula=~vic+vicl+vis)

#test versus a simpler model
fit2<-logistf(data=sex2, case~age+oc+dia)
# or: fit2<-update(fit, case~age+oc+dia)
anova(fit,fit2)

# comparison of non-nested models (with different df):
fit3<-logistf(data=sex2, case~age+vic+vicl+vis)
anova(fit2,fit3, method="PLR")</pre>
```

backward

Backward Elimination/Forward Selection of Model Terms in logistf Models

## **Description**

These functions provide simple backward elimination/forward selection procedures for logistf models.

## Usage

```
backward(object, ...)
## S3 method for class 'logistf'
backward(
 object,
  scope,
  steps = 1000,
  slstay = 0.05,
  trace = TRUE,
  printwork = FALSE,
  full.penalty = FALSE,
)
## S3 method for class 'flic'
backward(
  object,
  scope,
  steps = 1000,
```

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```
slstay = 0.05,
 trace = TRUE,
 printwork = FALSE,
  full.penalty = FALSE,
)
forward(object, ...)
## S3 method for class 'logistf'
forward(
 object,
  scope,
  steps = 1000,
  slentry = 0.05,
  trace = TRUE,
 printwork = FALSE,
 pl = TRUE,
)
```

### **Arguments**

object	A fitted logistf model object. To start with an empty model, create a model fit with a formula= y~1, pl=FALSE. (Replace y by your response variable.)
	Further arguments to be passed to methods.
scope	The scope of variables to add/drop from the model. Can be missing for backward, backward will use the terms of the object fit. Alternatively, an arbitrary vector of variable names can be given, to allow that only some of the variables will be competitively selected or dropped. Has to be provided for forward.
steps	The number of forward selection/backward elimination steps.
slstay	For backward, the significance level to stay in the model.
trace	If TRUE, protocols selection steps.
printwork	If TRUE, prints each working model that is visited by the selection procedure.
full.penalty	If TRUE penalty is not taken from current model but from start model.
slentry	For forward, the significance level to enter the model.
pl	For forward, computes profile likelihood confidence intervals for the final model if TRUE.

## **Details**

The variable selection is simply performed by repeatedly calling add1 or drop1 methods for logistf, and is based on penalized likelihood ratio test. It can also properly handle variables that were defined as factors in the original data set.

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#### Value

An updated logistf, flic or flac fit with the finally selected model.

#### **Functions**

forward: Forward Selection

## **Examples**

```
data(sex2)
fit<-logistf(data=sex2, case~1, pl=FALSE)
fitf<-forward(fit, scope = c("dia", "age"))
fit2<-logistf(data=sex2, case~age+oc+vic+vicl+vis+dia)
fitb<-backward(fit2)</pre>
```

CLIP.confint

Confidence Intervals after Multiple Imputation: Combination of Likelihood Profiles

## **Description**

This function implements the new combination of likelihood profiles (CLIP) method described in Heinze, Ploner and Beyea (2013). This method is useful for computing confidence intervals for parameters after multiple imputation of data sets, if the normality assumption on parameter estimates and consequently the validity of applying Rubin's rules (pooling of variances) is in doubt. It consists of combining the profile likelihoods into a posterior. The function CLIP.confint searches for those values of a regression coefficient, at which the cumulative distribution function of the posterior is equal to the values specified in the argument ci.level (usually 0.025 and 0.975). The search is performed using R's optimize function.

## Usage

```
CLIP.confint(
  obj = NULL,
  variable = NULL,
  data,
  firth = TRUE,
  weightvar = NULL,
  control = logistf.control(),
  ci.level = c(0.025, 0.975),
  pvalue = TRUE,
  offset = NULL,
  bound.lo = NULL,
  bound.up = NULL,
  legacy = FALSE
)
```

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## Arguments

obj Either a list of logistf fits (on multiple imputed data sets), or the result of analysis

of a mice (multiply imputed) object using with.mids

variable The variable of interest, for which confidence intervals should be computed. If

missing, confidence intervals for all variables will be computed.

data A list of data set corresponding to the model fits. Can be left blank if obj was

obtained with the dataout=TRUE option or if obj was obtained by mice

firth If TRUE, applies the Firth correction. Should correspond to the entry in obj.

weightvar An optional weighting variable for each observation.

control Control parameters for logistf, usually obtained by logistf.control()

ci.level The two confidence levels for each tail of the posterior distribution.

pvalue If TRUE, will also compute a P-value from the posterior.

offset An optional offset variable

bound.lo Bounds (vector of length 2) for the lower limit. Can be left blank. Use only if

problems are encountered.

bound up Bounds (vector of length 2) for the upper limit. Can be left blank. Use only if

problems are encountered.

legacy If TRUE, will use pure R code for all model fitting. Can be slow. Not recom-

mended.

#### Details

For each confidence limit, this function performs a binary search to evaluate the combined posterior, which is obtained by first transforming the imputed-data likelihood profiles into cumulative distribution functions (CDFs), and then averaging the CDFs to obtain the CDF of the posterior. Usually, the binary search manages to find the confidence intervals very quickly. The number of iterations (mean and maximum) will be supplied in the output object. Further details on the method can be found in Heinze, Ploner and Beyea (2013).

## Value

An object of class CLIP. confint, with items:

variable The variable(s) which were analyzed

estimate The pooled estimate (average over imputations)

ci The confidence interval(s)

pvalue The p-value(s)

imputations The number of imputed datasets ci.level The confidence level (input)

bound.lo The bounds used for finding the lower confidence limit; usually not of interest.

May be useful for error-tracing.

bound.up The bounds used for finding the upper confidence limit iter The number of iterations (for each variable and each tail)

call The call object

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### Author(s)

Georg Heinze and Meinhard Ploner

#### References

Heinze G, Ploner M, Beyea J (2013). Confidence intervals after multiple imputation: combining profile likelihood information from logistic regressions. Statistics in Medicine, to appear.

#### See Also

logistf() for Firth's bias-Reduced penalized-likelihood logistic regression.

## **Examples**

```
#generate data set with NAs
freq=c(5,2,2,7,5,4)
y<-c(rep(1,freq[1]+freq[2]), rep(0,freq[3]+freq[4]), rep(1,freq[5]), rep(0,freq[6]))
x<-c(rep(1,freq[1]), rep(0,freq[2]), rep(1,freq[3]), rep(0,freq[4]),</pre>
rep(NA, freq[5]), rep(NA, freq[6]))
toy<-data.frame(x=x,y=y)</pre>
# impute data set 5 times
set.seed(169)
toymi<-list(0)
for(i in 1:5){
  toymi[[i]]<-toy</pre>
  y1<-toymi[[i]]$y==1 & is.na(toymi[[i]]$x)</pre>
  y0<-toymi[[i]]$y==0 & is.na(toymi[[i]]$x)</pre>
  xnew1<-rbinom(sum(y1),1,freq[1]/(freq[1]+freq[2]))</pre>
  xnew0 < -rbinom(sum(y0), 1, freq[3]/(freq[3]+freq[4]))
  toymi[[i]]$x[y1==TRUE]<-xnew1</pre>
  toymi[[i]]$x[y0==TRUE]<-xnew0</pre>
 # logistf analyses of each imputed data set
 fit.list<-lapply(1:5, function(X) logistf(data=toymi[[X]], y~x, pl=TRUE))</pre>
 # CLIP confidence limits
 CLIP.confint(obj=fit.list, data = toymi)
```

CLIP.profile

Combine Profile Likelihoods from Imputed-Data Model Fits

## **Description**

This function uses CLIP (combination of likelihood profiles) to compute the pooled profile of the posterior after multiple imputation.

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## Usage

```
CLIP.profile(
  obj = NULL,
  variable,
  data,
  which,
  firth = TRUE,
  weightvar,
  control = logistf.control(),
  offset = NULL,
  from = NULL,
  to = NULL,
  steps = 101,
  legacy = FALSE,
  keep = FALSE
)
```

## **Arguments**

obj	Either a list of logistf fits (on multiple imputed data sets), or the result of analysis of a mice (multiply imputed) object using with.mids.
variable	The variable of interest, for which confidence intervals should be computed. If missing, confidence intervals for all variables will be computed.
data	A list of data set corresponding to the model fits. Can be left blank if obj was obtained with the dataout=TRUE option or if obj was obtained by mice.
which	Alternatively to variable, the argument which allows to specify the variable to compute the profile for as righthand formula, e.g. which=~X.
firth	If TRUE, applies the Firth correction. Should correspond to the entry in obj.
weightvar	An optional weighting variable for each observation
control	control parameters for logistf, usually obtained by logistf.control()
offset	An optional offset variable
from	Lowest value for the sequence of values for the regression coefficients for which the profile will be computed. Can be left blank.
to	Highest value for the sequence of values for the regression coefficients for which the profile will be computed. Can be left blank
steps	Number of steps for the sequence of values for the regression coefficients for which the profile will be computed
legacy	If TRUE, only R code will be used. Should be avoided.
keep	If TRUE, keeps the profiles for each imputed data sets in the output object.

## **Details**

While CLIP.confint iterates to find those values at which the CDF of the pooled posterior equals the confidence levels, CLIP.profile will evaluate the whole profile, which enables plotting and evaluating the skewness of the combined and the completed-data profiles. The combined and completed-data profiles are available as cumulative distribution function (CDF) or in the scaling of relative

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profile likelihood (minus twice the likelihood ratio statistic compared to the maximum). Using a plot method, the pooled posterior can also be displayed as a density.

#### Value

An object of class CLIP.profile with items:

beta The values of the regression coefficient

cdf The cumulative distribution function of the posterior

profile The profile of the posterior

cdf.matrix An imputations x steps matrix with the values of the completed-data CDFs for

each beta

profile.matrix An imputations x steps matrix with the values of the completed-data profiles for

each beta

call The function call

### Author(s)

Georg Heinze und Meinhard Plonar

#### References

Heinze G, Ploner M, Beyea J (2013). Confidence intervals after multiple imputation: combining profile likelihood information from logistic regressions. Statistics in Medicine, to appear.

### **Examples**

```
#generate data set with NAs
freq=c(5,2,2,7,5,4)
y<-c(rep(1,freq[1]+freq[2]), rep(0,freq[3]+freq[4]), rep(1,freq[5]), rep(0,freq[6]))
x<-c(rep(1,freq[1]), rep(0,freq[2]), rep(1,freq[3]), rep(0,freq[4]), rep(NA,freq[5]),
rep(NA, freq[6]))
toy<-data.frame(x=x,y=y)
# impute data set 5 times
set.seed(169)
toymi<-list(0)
for(i in 1:5){
 toymi[[i]]<-toy
 y1<-toymi[[i]]$y==1 & is.na(toymi[[i]]$x)</pre>
 y0<-toymi[[i]]$y==0 & is.na(toymi[[i]]$x)</pre>
 xnew1<-rbinom(sum(y1),1,freq[1]/(freq[1]+freq[2]))</pre>
 xnew0 < -rbinom(sum(y0), 1, freq[3]/(freq[3]+freq[4]))
  toymi[[i]]$x[y1==TRUE]<-xnew1</pre>
  toymi[[i]]x[y0==TRUE]<-xnew0
}
# logistf analyses of each imputed data set
fit.list<-lapply(1:5, function(X) logistf(data=toymi[[X]], y~x, pl=TRUE))</pre>
```

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```
# CLIP profile
xprof<-CLIP.profile(obj=fit.list, variable="x",data =toymi, keep=TRUE)
plot(xprof)

#plot as CDF
plot(xprof, "cdf")

#plot as density
plot(xprof, "density")</pre>
```

flac

FLAC - Firth's logistic regression with added covariate

## **Description**

flac implements Firth's bias-reduced penalized-likelihood logistic regression with added covariate.

## Usage

```
flac(...)
## Default S3 method:
flac(
  formula,
  data,
  model = TRUE,
  control,
  modcontrol,
  weights,
  offset,
  na.action,
  ...
)
## S3 method for class 'logistf'
flac(lfobject, data, model = TRUE, ...)
```

## **Arguments**

	Further arguments p	bassed to the method	d or logistf-call.
--	---------------------	----------------------	--------------------

formula A formula object, with the response on the left of the operator, and the model

terms on the right. The response must be a vector with 0 and 1 or FALSE and

TRUE for the outcome, where the higher value (1 or TRUE) is modeled.

data A data frame containing the variables in the model.

model If TRUE the corresponding components of the fit are returned.

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control Controls iteration parameter. Taken from logistf-object when specified. Oth-

erwise default is control=logistf.control().

modcontrol Controls additional parameter for fitting. Taken from logistf-object when

specified. Otherwise default is logistf.mod.control().

weights specifies case weights. Each line of the input data set is multiplied by the corre-

sponding element of weights

offset a priori known component to be included in the linear predictor

na.action a function which indicates what should happen when the data contain NAs

lfobject A fitted logistf object.

#### **Details**

FLAC is a simple modification of Firth's logistic regression which provides average predicted probabilities equal to the observed proportion of events, while preserving the ability to deal with separation. It has been described by Puhr et al (2017).

The modified score equations to estimate coefficients for Firth's logistic regression can be interpreted as score equations for ML estimates for an augmented data set. This data set can be created by complementing each original observation i with two pseudo-observations weighted by  $h_i/2$  with unchanged covariate values and with response values set to y=0 and y=1 respectively. The basic idea of FLAC is to discriminate between original and pseudo-observations in the alternative formulation of Firth's estimation as an iterative data augmentation procedure. The following generic methods are available for 'flac's output object: print, summary, coef, confint, anova, extractAIC, add1, drop1, profil Furthermore, forward and backward functions perform convenient variable selection. Note that anova, extractAIC, add1, drop1, forward and backward are based on penalized likelihood ratio tests.

## Value

A flac object with components:

coefficients The coefficients of the parameter in the fitted model.

predict A vector with the predicted probability of each observation

linear.predictors

A vector with the linear predictor of each observation.

prob The p-values of the specific parameters

ci.lower The lower confidence limits of the parameter.
ci.upper The upper confidence limits of the parameter.

call The call object.

alpha The significance level: 0.95

var The variance-covariance-matrix of the parameters.

loglik A vector of the (penalized) log-likelihood of the restricted and the full models.

n The number of observations.

formula The formula object.

augmented.data The augmented dataset used

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df The number of degrees of freedom in the model.

method depending on the fitting method 'Penalized ML' or Standard ML'. \\text{item{method.ci}{the method in cal-

culating the confidence intervals, i.e. profile likelihood' or 'Wald', depending on

the argument pl and plconf.

control a copy of the control parameters.

modcontrol a copy of the modcontrol parameters.

terms the model terms (column names of design matrix).

model if requested (the default), the model frame used.

## Methods (by class)

default: With formula and datalogistf: With logistf object

#### References

Puhr R, Heinze G, Nold M, Lusa L, Geroldinger A (2017). Firth's logistic regression with rare events: accurate effect estimates and predictions? Statistics in Medicine 36: 2302-2317.

#### See Also

logistf() for Firth's bias-Reduced penalized-likelihood logistic regression.

## **Examples**

```
#With formula and data:
data(sex2)
flac(case ~ age + oc + vic + vicl + vis + dia, sex2)

#With a logistf object:
lf <- logistf(formula = case ~ age + oc + vic + vicl + vis + dia, data = sex2)
flac(lf, data=sex2)</pre>
```

flic

FLIC - Firth's logistic regression with intercept correction

### **Description**

flic implements Firth's bias-reduced penalized-likelihood logistic regression with intercept correction.

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## Usage

```
flic(...)
## Default S3 method:
flic(
  formula,
  data,
  model = TRUE,
  control,
  modcontrol,
  weights,
  offset,
  na.action,
  ...
)
## S3 method for class 'logistf'
flic(lfobject, model = TRUE, ...)
```

## **Arguments**

	Further arguments passed to the method or logistf-call.
formula	A formula object, with the response on the left of the operator, and the model terms on the right. The response must be a vector with 0 and 1 or FALSE and TRUE for the outcome, where the higher value (1 or TRUE) is modeled.
data	If using with formula, a data frame containing the variables in the model.
model	If TRUE the corresponding components of the fit are returned.
control	Controls iteration parameter. Taken from logistf-object when specified. Otherwise default is control=logistf.control().
modcontrol	Controls additional parameter for fitting. Taken from logistf-object when specified. Otherwise default is logistf.mod.control().
weights	specifies case weights. Each line of the input data set is multiplied by the corresponding element of weights
offset	a priori known component to be included in the linear predictor
na.action	a function which indicates what should happen when the data contain NAs
lfobject	A fitted logistf object.

## **Details**

FLIC is a simple modification of Firth's logistic regression which provides average predicted probabilities equal to the observed proportion of events, while preserving the ability to deal with separation.

In general the average predicted probability in Firth's logistic regression is not equal to the observed proportion of events. Because the determinant of the Fisher-Information matrix is maximized for  $\pi_i=\frac{1}{2}$  it is concluded that Firth's penalization tends to push the predicted probabilities

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towards one-half compared with ML-estimation. FLIC first applies Firth's logistic regression and then corrects the intercept such that the predicted probabilities become unbiased while keeping all other coefficients constant. The following generic methods are available for flic's output object: print, summary, coef, confint, anova, extractAIC, add1, drop1, profile, terms, nobs, predict. Furthermore, forward and backward functions perform convenient variable selection. Note that anova, extractAIC, add1, drop1, forward and backward are based on penalized likelihood ratio tests.

#### Value

A flic object with components:

coefficients The coefficients of the parameter in the fitted model.

predict A vector with the predicted probability of each observation.

linear.predictors

A vector with the linear predictor of each observation.

var The variance-covariance-matrix of the parameters.

prob The p-values of the specific parameters.

ci.lower The lower confidence limits of the parameter.
ci.upper The upper confidence limits of the parameter.

call The call object.

alpha The significance level: 0.95.

method depending on the fitting method 'Penalized ML' or Standard ML'. \tem{method.ci}{the method in cal-

culating the confidence intervals, i.e. profile likelihood' or 'Wald', depending on

the argument pl and plconf.

df The number of degrees of freedom in the model.

loglik A vector of the (penalized) log-likelihood of the restricted and the full models.

n The number of observations.

formula The formula object.

control a copy of the control parameters.

modcontrol a copy of the modcontrol parameters.

terms the model terms (column names of design matrix).

model if requested (the default), the model frame used.

## Methods (by class)

default: With formula and datalogistf: With logistf object

## References

Puhr R, Heinze G, Nold M, Lusa L, Geroldinger A (2017). Firth's logistic regression with rare events: accurate effect estimates and predictions? Statistics in Medicine 36: 2302-2317.

### See Also

logistf for Firth's bias-Reduced penalized-likelihood logistic regression.

## **Examples**

```
#With formula and data:
data(sex2)
flic(case ~ age + oc + vic + vicl + vis + dia, sex2)

#With a logistf object:
lf <- logistf(formula = case ~ age + oc + vic + vicl + vis + dia, data = sex2)
flic(lf)</pre>
```

logistf

Firth's Bias-Reduced Logistic Regression

## **Description**

Implements Firth's bias-Reduced penalized-likelihood logistic regression.

## Usage

```
logistf(
  formula,
  data,
 pl = TRUE,
  alpha = 0.05,
  control,
  plcontrol,
 modcontrol,
  firth = TRUE,
  init,
 weights,
 na.action,
 offset,
 plconf = NULL,
 flic = FALSE,
 model = TRUE,
)
```

## Arguments

formula

A formula object, with the response on the left of the operator, and the model terms on the right. The response must be a vector with 0 and 1 or FALSE and TRUE for the outcome, where the higher value (1 or TRUE) is modeled. It is possible to include contrasts, interactions, nested effects, cubic or polynomial splines and all S features as well, e.g.  $Y \sim X1*X2 + ns(X3, df=4)$ .

data	A data frame where the variables named in the formula can be found, i. e. the variables containing the binary response and the covariates.
pl	Specifies if confidence intervals and tests should be based on the profile penalized log likelihood (p1=TRUE, the default) or on the Wald method (p1=FALSE).
alpha	The significance level (1- $\alpha$ the confidence level, 0.05 as default).
control	Controls iteration parameter. Default is control=logistf.control()
plcontrol	Controls Newton-Raphson iteration for the estimation of the profile likelihood confidence intervals. Default is plcontrol= logistpl.control()
modcontrol	Controls additional parameter for fitting. Default is logistf.mod.control()
firth	Use of Firth's penalized maximum likelihood (firth=TRUE, default) or the standard maximum likelihood method (firth=FALSE) for the logistic regression. Note that by specifying pl=TRUE and firth=FALSE (and probably a lower number of iterations) one obtains profile likelihood confidence intervals for maximum likelihood logistic regression parameters.
init	Specifies the initial values of the coefficients for the fitting algorithm
weights	specifies case weights. Each line of the input data set is multiplied by the corresponding element of weights
na.action	a function which indicates what should happen when the data contain NAs
offset	a priori known component to be included in the linear predictor
plconf	specifies the variables (as vector of their indices) for which profile likelihood confidence intervals should be computed. Default is to compute for all variables.
flic	If TRUE, intercept is altered such that the predicted probabilities become unbiased while keeping all other coefficients constant (see Puhr et al, 2017)
model	If TRUE the corresponding components of the fit are returned.
	Further arguments to be passed to logistf

## **Details**

logistf is the main function of the package. It fits a logistic regression model applying Firth's correction to the likelihood. The following generic methods are available for logistf's output object: print, summary, coef, vcov, confint, anova, extractAIC, add1, drop1, profile, terms, nobs, predict. Furthermore, forward and backward functions perform convenient variable selection. Note that anova, extractAIC, add1, drop1, forward and backward are based on penalized likelihood ratios.

### Value

The object returned is of the class logistf and has the following attributes:

coefficients the coefficients of the parameter in the fitted model.

alpha the significance level (1- the confidence level) as specified in the input.

terms the column names of the design matrix

var the variance-covariance-matrix of the parameters.

df the number of degrees of freedom in the model.

a vector of the (penalized) log-likelihood of the restricted and the full models. loglik

A vector of the number of iterations needed in the fitting process for the null and iter

full model.

the number of observations. n

the response-vector, i. e. 1 for successes (events) and 0 for failures.

formula the formula object. the call object.

the model terms (column names of design matrix). terms

linear.predictors

call

a vector with the linear predictor of each observation.

predict a vector with the predicted probability of each observation.

hat.diag a vector with the diagonal elements of the Hat Matrix.

the convergence status at last iteration: a vector of length 3 with elements: last conv

change in log likelihood, max(abs(score vector)), max change in beta at last

iteration.

method depending on the fitting method 'Penalized ML' or Standard ML'. \\ten{method.ci}{the method in cal-

culating the confidence intervals, i.e. profile likelihood' or 'Wald', depending on

the argument pl and plconf.

ci.lower the lower confidence limits of the parameter.

ci.upper the upper confidence limits of the parameter.

prob the p-values of the specific parameters.

only if pl==TRUE: the number of iterations needed for each confidence limit. pl.iter

betahist only if pl==TRUE: the complete history of beta estimates for each confidence

limit.

only if pl==TRUE: the convergence status (deviation of log likelihood from tarpl.conv

get value, last maximum change in beta) for each confidence limit.

control a copy of the control parameters.

modcontrol a copy of the modcontrol parameters.

flic logical, is TRUE if intercept was altered such that the predicted probabilities

become unbiased while keeping all other coefficients constant. According to

input of logistf.

mode1 if requested (the default), the model frame used.

information returned by model.frame on the special handling of NAs na.action

#### Author(s)

Georg Heinze and Meinhard Ploner

#### References

Firth D (1993). Bias reduction of maximum likelihood estimates. Biometrika 80, 27-38. Heinze G, Schemper M (2002). A solution to the problem of separation in logistic regression. Statistics in Medicine 21: 2409-2419.

Heinze G, Ploner M (2003). Fixing the nonconvergence bug in logistic regression with SPLUS and SAS. Computer Methods and Programs in Biomedicine 71: 181-187.

Heinze G, Ploner M (2004). Technical Report 2/2004: A SAS-macro, S-PLUS library and R package to perform logistic regression without convergence problems. Section of Clinical Biometrics, Department of Medical Computer Sciences, Medical University of Vienna, Vienna, Austria. http://www.meduniwien.ac.at/user/georg.heinze/techreps/tr2\_2004.pdf

Heinze G (2006). A comparative investigation of methods for logistic regression with separated or nearly separated data. Statistics in Medicine 25: 4216-4226.

Puhr R, Heinze G, Nold M, Lusa L, Geroldinger A (2017). Firth's logistic regression with rare events: accurate effect estimates and predictions? Statistics in Medicine 36: 2302-2317.

Venzon DJ, Moolgavkar AH (1988). A method for computing profile-likelihood based confidence intervals. Applied Statistics 37:87-94.

#### See Also

```
add1.logistf(), anova.logistf()
```

### **Examples**

```
fit<-logistf(case ~ age+oc+vic+vicl+vis+dia, data=sex2)</pre>
summary(fit)
nobs(fit)
drop1(fit)
plot(profile(fit,variable="dia"))
extractAIC(fit)
fit1<-update(fit, case ~ age+oc+vic+vicl+vis)</pre>
extractAIC(fit1)
anova(fit,fit1)
data(sexagg)
fit2<-logistf(case ~ age+oc+vic+vicl+vis+dia, data=sexagg, weights=COUNT)</pre>
summary(fit2)
# simulated SNP example
set.seed(72341)
snpdata<-rbind(</pre>
  matrix(rbinom(2000,2,runif(2000)*0.3),100,20),
  matrix(rbinom(2000,2,runif(2000)*0.5),100,20))
colnames(snpdata)<-paste("SNP",1:20,"_",sep="")</pre>
snpdata<-as.data.frame(snpdata)</pre>
for(i in 1:20) snpdata[,i]<-as.factor(snpdata[,i])</pre>
snpdata$case<-c(rep(0,100),rep(1,100))
```

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```
fitsnp<-logistf(data=snpdata, formula=case~1, pl=FALSE)
add1(fitsnp, scope=paste("SNP",1:20,"_",sep=""))
fitf<-forward(fitsnp, scope = paste("SNP",1:20,"_",sep=""))
fitf</pre>
```

logistf.control

Control Parameters for logistf

## Description

Sets parameters for iterations in Firth's penalized-likelihood logistic regression.

## Usage

```
logistf.control(
  maxit = 25,
  maxhs = 0,
  maxstep = 5,
  lconv = 1e-05,
  gconv = 1e-05,
  xconv = 1e-05,
  collapse = TRUE,
  fit = "NR"
)
```

## **Arguments**

maxit	The maximum number of iterations
maxhs	The maximum number of step-halvings in one iteration. The increment of the beta vector within one iteration is divided by 2 if the new beta leads to a decrease in log likelihood.
maxstep	Specifies the maximum step size in the beta vector within one iteration. Set to -1 for infinite stepsize.
lconv	Specifies the convergence criterion for the log likelihood.
gconv	Specifies the convergence criterion for the first derivative of the log likelihood (the score vector).
xconv	Specifies the convergence criterion for the parameter estimates.
collapse	If TRUE, evaluates all unique combinations of x and y and collapses data set.
fit	Fitting method used. One of Newton-Raphson: "NR" or Iteratively reweighted least squares: "IRLS"

## **Details**

logistf.control() is used by logistf and logistftest to set control parameters to default values. Different values can be specified, e. g., by logistf(...,control= logistf.control(maxstep=1)).

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#### Value

maxit The maximum number of iterations

maxhs The maximum number of step-halvings in one iteration. The increment of the

beta vector within one iteration is divided by 2 if the new beta leads to a decrease

in log likelihood.

maxstep Specifies the maximum step size in the beta vector within one iteration.

1conv Specifies the convergence criterion for the log likelihood.

gconv Specifies the convergence criterion for the first derivative of the log likelihood

(the score vector).

xconv Specifies the convergence criterion for the parameter estimates.

collapse If TRUE, evaluates all unique combinations of x and y and collapses data set.

fit Fitting method used. One of Newton-Raphson: "NR" or Iteratively reweighted

least squares: "IRLS"

call The function call.

## **Examples**

```
data(sexagg)
fit2<-logistf(case ~ age+oc+vic+vicl+vis+dia, data=sexagg, weights=COUNT,
control=logistf.control(maxstep=1))
summary(fit2)</pre>
```

logistf.mod.control

Controls additional parameters for logistf

#### **Description**

Sets parameters for logistf calls.

### Usage

```
logistf.mod.control(tau = 0.5, terms.fit = NULL)
```

## **Arguments**

tau Penalization parameter (default = 0.5)

terms.fit A numeric vector of terms to fit. Intercept has to be included if needed.

#### Value

tau Penalization parameter (default = 0.5)

terms.fit A numeric vector of terms to fit. Intercept has to be included if needed.

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## **Examples**

```
data(sexagg)
fit2<-logistf(case ~ age+oc+vic+vicl+vis+dia, data=sexagg, weights=COUNT,
modcontrol=logistf.mod.control(terms.fit=c(1,2)))
summary(fit2)</pre>
```

logistftest

Penalized likelihood ratio test

## **Description**

This function performs a penalized likelihood ratio test on some (or all) selected factors. The resulting object is of the class logistftest and includes the information printed by the proper print method.

## Usage

```
logistftest(
  object,
  test,
  values,
  firth = TRUE,
  beta0,
  weights,
  control,
  modcontrol,
  ...
)
```

## **Arguments**

beta0

object	A fitted logistf object
test	righthand formula of parameters to test (e.g. $\sim$ B + D - 1). As default all parameter apart from the intercept are tested. If the formula includes -1, the intercept is omitted from testing. As alternative to the formula one can give the indexes of the ordered effects to test (a vector of integers). To test only the intercept specify test = $\sim$ or test = 1.
values	Null hypothesis values, default values are 0. For testing the specific hypothesis B1=1, B4=2, B5=0 we specify test= $\sim$ B1+B4+B5-1 and values=c(1, 2,0).
firth	Use of Firth's (1993) penalized maximum likelihood (firth=TRUE, default) or the standard maximum likelihood method (firth=FALSE) for the logistic regression. Note that by specifying pl=TRUE and firth=FALSE (and probably lower number of iterations) one obtains profile likelihood confidence intervals for maximum likelihood logistic regression parameters.

Specifies the initial values of the coefficients for the fitting algorithm

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weights Case weights

control Controls parameters for iterative fitting

modcontrol Controls additional parameter for fitting. Default is modcontrol of object.

... further arguments passed to logistf.fit

#### **Details**

This function performs a penalized likelihood ratio test on some (or all) selected factors. The resulting object is of the class logistftest and includes the information printed by the proper print method. Further documentation can be found in Heinze & Ploner (2004). In most cases, the functionality of the logistftest function is replaced by anova.logistf, which is a more standard way to perform likelihood ratio tests. However, as shown in the example below, logistftest provides some specials such as testing against non-zero values. (By the way, anova.logistf calls logistftest.

#### Value

The object returned is of the class logistf and has the following attributes:

testcov A vector of the fixed values of each covariate; NA stands for a parameter which

is not tested.

loglik A vector of the (penalized) log-likelihood of the full and the restricted models.

If the argument beta0 not missing, the full model isn't evaluated

df The number of degrees of freedom in the model

prob The p-value of the test

call The call object

method Depending on the fitting method 'Penalized ML' or 'Standard ML'

beta The coefficients of the restricted solution

## Author(s)

Georg Heinze

### References

Firth D (1993). Bias reduction of maximum likelihood estimates. Biometrika 80, 27-38.

Heinze G, Ploner M (2004). Technical Report 2/2004: A SAS-macro, S-PLUS library and R package to perform logistic regression without convergence problems. Section of Clinical Biometrics, Department of Medical Computer Sciences, Medical University of Vienna, Vienna, Austria. http://www.meduniwien.ac.at/user/georg.heinze/techreps/tr2\_2004.pdf

Heinze G (2006). A comparative investigation of methods for logistic regression with separated or nearly separated data. Statistics in Medicine 25: 4216-4226

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## **Examples**

```
data(sex2)
fit<-logistf(case ~ age+oc+vic+vicl+vis+dia, data=sex2)
logistftest(fit, test = ~ vic + vicl - 1, values = c(2, 0))</pre>
```

logistpl.control

Control Parameters for logistf Profile Likelihood Confidence Interval Estimation

### **Description**

Sets parameters for modified Newton-Raphson iteration for finding profile likelihood confidence intervals in Firth's penalized likelihood logistic regression

## Usage

```
logistpl.control(
  maxit = 100,
  maxhs = 0,
  maxstep = 5,
  lconv = 1e-05,
  xconv = 1e-05,
  ortho = FALSE,
  pr = FALSE
)
```

## **Arguments**

maxit	The maximum number of iterations
maxhs	The maximum number of step-halvings in one iteration. The increment of the beta vector within one iteration is divided by 2 if the new beta leads to a decrease in log likelihood.
maxstep	Specifies the maximum step size in the beta vector within one iteration. Set to -1 for infinite stepsize.
lconv	Specifies the convergence criterion for the log likelihood.
xconv	Specifies the convergence criterion for the parameter estimates.
ortho	Requests orthogonalization of variable for which confidence intervals are computed with respect to other covariates
pr	Request rotation of the matrix spanned by the covariates

## **Details**

logistpl.control() is used by logistf to set control parameters to default values when computing profile likelihood confidence intervals. Different values can be specified, e. g., by logistf(..., control=logistf.control(maxstep=1)).

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## Value

maxit	The maximum number of iterations
maxhs	The maximum number of step-halvings in one iteration. The increment of the beta vector within one iteration is divided by 2 if the new beta leads to a decrease in log likelihood.
maxstep	Specifies the maximum step size in the beta vector within one iteration.
lconv	Specifies the convergence criterion for the log likelihood.
xconv	Specifies the convergence criterion for the parameter estimates.
ortho	specifies if orthogonalization is requested.
pr	specifies if rotation is requested

## Author(s)

Georg Heinze

## **Examples**

```
data(sexagg)
fit2<-logistf(case ~ age+oc+vic+vicl+vis+dia, data=sexagg, weights=COUNT,
    plcontrol=logistpl.control(maxstep=1))
summary(fit2)</pre>
```

```
\verb|plot.logistf.profile| & \verb|plot| \textit{Method for } \verb|logistf| \textit{Likelihood Profiles}
```

## **Description**

Provides the plot method for objects created by profile.logistf or CLIP.profile

## Usage

```
## S3 method for class 'logistf.profile'
plot(
    x,
    type = "profile",
    max1 = TRUE,
    colmain = "black",
    colimp = "gray",
    plotmain = T,
    ylim = NULL,
    ...
)
```

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## Arguments

X	A profile.logistf object
type	Type of plot: one of c("profile", "cdf", "density")
max1	If type="density", normalizes density to maximum 1
colmain	Color for main profile line
colimp	color for completed-data profile lines (for logistf.profile objects that also carry the CLIP.profile class attribute)
plotmain	if FALSE, suppresses the main profile line (for logistf.profile objects that also carry the CLIP.profile class attribute)
ylim	Limits for the y-axis
	Further arguments to be passed to plot().

#### **Details**

The plot method provides three types of plots (profile, CDF, and density representation of a profile likelihood). For objects generated by CLIP.profile, it also allows to show the completed-data profiles along with the pooled profile.

#### Value

The function is called for its side effects

### Author(s)

Georg Heinze und Meinhard Ploner

## References

Heinze G, Ploner M, Beyea J (2013). Confidence intervals after multiple imputation: combining profile likelihood information from logistic regressions. Statistics in Medicine, to appear.

## **Examples**

```
data(sex2)
fit<-logistf(case ~ age+oc+vic+vicl+vis+dia, data=sex2)
plot(profile(fit,variable="dia"))
plot(profile(fit,variable="dia"), "cdf")
plot(profile(fit,variable="dia"), "density")

#generate data set with NAs
freq=c(5,2,2,7,5,4)
y<-c(rep(1,freq[1]+freq[2]), rep(0,freq[3]+freq[4]), rep(1,freq[5]), rep(0,freq[6]))
x<-c(rep(1,freq[1]), rep(0,freq[2]), rep(1,freq[3]), rep(0,freq[4]), rep(NA,freq[5]),
    rep(NA,freq[6]))
toy<-data.frame(x=x,y=y)

# impute data set 5 times</pre>
```

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```
set.seed(169)
toymi<-list(0)</pre>
for(i in 1:5){
   toymi[[i]]<-toy</pre>
   y1<-toymi[[i]]$y==1 & is.na(toymi[[i]]$x)</pre>
   y0<-toymi[[i]]$y==0 & is.na(toymi[[i]]$x)</pre>
   xnew1<-rbinom(sum(y1),1,freq[1]/(freq[1]+freq[2]))</pre>
   xnew0<-rbinom(sum(y0),1,freq[3]/(freq[3]+freq[4]))
   toymi[[i]]$x[y1==TRUE]<-xnew1</pre>
   toymi[[i]]$x[y0==TRUE]<-xnew0</pre>
}
# logistf analyses of each imputed data set
fit.list<-lapply(1:5, function(X) logistf(data=toymi[[X]], y~x, pl=TRUE))</pre>
# CLIP profile
xprof<-CLIP.profile(obj=fit.list, variable="x", data=toymi, keep=TRUE)</pre>
plot(xprof)
#plot as CDF
plot(xprof, "cdf")
#plot as density
plot(xprof, "density")
```

predict.flac

Predict Method for flac Fits

## Description

Obtains predictions from a fitted flac object.

#### **Usage**

```
## S3 method for class 'flac'
predict(
  object,
  newdata,
  type = c("link", "response", "terms"),
  se.fit = FALSE,
  ...
)
```

## **Arguments**

object A fitted object of class flac.

newdata Optionally, a data frame in which to look for variables with which to predict. If

omitted, the fitted linear predictors are used.

predict.flic 31

type	The type of prediction required. The default is on the scale of the linear predictors. The alternative response gives the predicted probabilities. Type terms returns a matrix with the fitted values of each term in the formula on the linear predictor scale.
se.fit	If TRUE(default = FALSE) standard errors are computed.
• • •	further arguments passed to or from other methods.

## **Details**

If newdata is omitted the predictions are based on the data used for the fit.

## Value

A vector or matrix of predictions.

predict.flic

Predict Method for flic Fits

## Description

Obtains predictions from a fitted flic object.

## Usage

```
## $3 method for class 'flic'
predict(
  object,
  newdata,
  type = c("link", "response", "terms"),
  se.fit = FALSE,
  ...
)
```

## Arguments

object	A fitted object of class flic.
newdata	Optionally, a data frame in which to look for variables with which to predict. If omitted, the fitted linear predictors are used.
type	The type of prediction required. The default is on the scale of the linear predictors. The alternative response gives the predicted probabilities. Type terms returns a matrix with the fitted values of each term in the formula on the linear predictor scale.
se.fit	If TRUE(default = FALSE) standard errors are computed.
	further arguments passed to or from other methods.

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## **Details**

If newdata is omitted the predictions are based on the data used for the fit.

## Value

A vector or matrix of predictions

predict.logistf

Predict Method for logistf Fits

## Description

Obtains predictions from a fitted logistf object.

## Usage

```
## S3 method for class 'logistf'
predict(
  object,
  newdata,
  type = c("link", "response", "terms"),
  flic = FALSE,
  se.fit = FALSE,
  reference,
  na.action = na.pass,
  ...
)
```

## **Arguments**

object	A fitted object of class logistf.
newdata	Optionally, a data frame in which to look for variables with which to predict. If omitted, the fitted linear predictors are used.
type	The type of prediction required. The default is on the scale of the linear predictors. The alternative response gives the predicted probabilities. Type terms returns a matrix with the fitted values of each term in the formula on the linear predictor scale.
flic	If TRUE(default = FALSE), predictions are computed with intercept correction.
se.fit	If TRUE(default = FALSE) standard errors are computed.
reference	A named vector of reference values for each variable for type="terms".
na.action	Function determining what should be done with missing values in newdata. The default is to predict NA.
	further arguments passed to or from other methods.

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## **Details**

If newdata is omitted the predictions are based on the data used for the fit.

## Value

A vector or matrix of predictions.

profile.logistf

Compute Profile Penalized Likelihood

## Description

Evaluates the profile penalized likelihood of a variable based on a logistf model fit

## Usage

```
## S3 method for class 'logistf'
profile(
   fitted,
   which,
   variable,
   steps = 100,
   pitch = 0.05,
   limits,
   alpha = 0.05,
   firth = TRUE,
   legends = TRUE,
   control,
   plcontrol,
   ...
)
```

## Arguments

fitted	An object fitted by logistf
which	A righthand formula to specify the variable for which the profile should be evaluated, e.g., which= $\sim$ X).
variable	Alternatively to which, a variable name can be given, e.g., variable="X"
steps	Number of steps in evaluating the profile likelihood
pitch	Alternatively to steps, one may specify the step width in multiples of standard errors
limits	Lower and upper limits of parameter values at which profile likelihood is to be evaluated
alpha	The significance level (1- $\alpha$ the confidence level, 0.05 as default).

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firth	Use of Firth's penalized maximum likelihood (firth=TRUE, default) or the standard maximum likelihood method (firth=FALSE) for the logistic regression.
legends	legends to be included in the optional plot
control	Controls Newton-Raphson iteration. Default is control=logistf.control(maxstep,maxit,maxhs,logistf.control(maxstep,maxit,maxhs,logistf.control)
plcontrol	Controls Newton-Raphson iteration for the estimation of the profile likelihood confidence intervals. Default is plcontrol=logistpl.control(maxstep,maxit,maxhs,lconv,xconv
	Further arguments to be passed.

#### Value

An object of class logistf.profile with the following items:

beta	Parameter values at which likelihood was evaluated
stdbeta	Parameter values divided by standard error
profile	profile likelihood, standardized to 0 at maximum of likelihood. The values in profile are given as minus $\chi^2$
loglik	Unstandardized profile likelihood
signed.root	signed root (z) of $\chi^2$ values (negative for values below the maximum likelihood estimate, positive for values above the maximum likelihood estimate)
cdf	profile likelihood expressed as cumulative distribution function, obtained as $\Phi(z)$ , where $\Phi$ denotes the standard normal distribution function.

## References

Heinze G, Ploner M, Beyea J (2013). Confidence intervals after multiple imputation: combining profile likelihood information from logistic regressions. Statistics in Medicine, to appear.

## Examples

```
data(sex2)
fit<-logistf(case ~ age+oc+vic+vicl+vis+dia, data=sex2)
plot(profile(fit,variable="dia"))
plot(profile(fit,variable="dia"), "cdf")
plot(profile(fit,variable="dia"), "density")</pre>
```

PVR.confint	Pseudo Variance Modification of Rubin's Rule

## **Description**

The pseudo-variance modification proposed by Heinze, Ploner and Beyea (2013) provides a quick way to adapt Rubin's rules to situations of a non-normal distribution of a regression coefficient. However, the approxiation is less accurate than that of the CLIP method.

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### Usage

```
PVR.confint(obj, variable, skewbeta = FALSE)
```

#### **Arguments**

obj A fitted logisf object

variable The variable(s) to compute the PVR confidence intervals, either provided as

names or as numbers

skewbeta If TRUE, incorporates information on the skewness of the parameter estimates

across the imputed data sets.

#### **Details**

The pseudo-variance modification computes a lower and an upper pseudo-variance, which are based on the distance between profile likelihood limits and the parameter estimates. These are then plugged into the usual Rubin's rules method of variance combination

#### Value

An object of class PVR. confint with items:

estimate the pooled parameter estimate(s) (the average across completed-data estimates)

ci the confidence intervals based on the PVR method

lower.var the lower pseudo-variance(s) upper.var the upper pseudo-variance(s)

conflev the confidence level: this is determined by the confidence level (1-alpha) used

in the input fit objects

call the function call

variable the variable(s) for which confidence intervals were computed

## Author(s)

Georg Heinze

#### References

Heinze G, Ploner M, Beyea J (2013). Confidence intervals after multiple imputation: combining profile likelihood information from logistic regressions. Statistics in Medicine, to appear.

### **Examples**

```
#generate data set with NAs
freq=c(5,2,2,7,5,4)
y<-c(rep(1,freq[1]+freq[2]), rep(0,freq[3]+freq[4]), rep(1,freq[5]), rep(0,freq[6]))
x<-c(rep(1,freq[1]), rep(0,freq[2]), rep(1,freq[3]), rep(0,freq[4]), rep(NA,freq[5]),
    rep(NA,freq[6]))
toy<-data.frame(x=x,y=y)</pre>
```

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```
# impute data set 5 times
set.seed(169)
toymi<-list(0)
for(i in 1:5){
    toymi[[i]]<-toy
    y1<-toymi[[i]]$y==1 & is.na(toymi[[i]]$x)
    y0<-toymi[[i]]$y==0 & is.na(toymi[[i]]$x)
    xnew1<-rbinom(sum(y1),1,freq[1]/(freq[1]+freq[2]))
    xnew0<-rbinom(sum(y0),1,freq[3]/(freq[3]+freq[4]))
    toymi[[i]]$x[y1==TRUE]<-xnew1
    toymi[[i]]$x[y0==TRUE]<-xnew0
}

# logistf analyses of each imputed data set
fit.list<-lapply(1:5, function(X) logistf(data=toymi[[X]], y~x, pl=TRUE))
# CLIP confidence limits
PVR.confint(obj=fit.list)</pre>
```

sex2

Urinary Tract Infection in American College Students

## Description

This data set deals with urinary tract infection in sexually active college women, along with covariate information on age an contraceptive use. The variables are all binary and coded in 1 (condition is present) and 0 (condition is absent).

## Usage

sex2

### **Format**

```
sex2: a data.frame containing 239 observations

case urinary tract infection, the study outcome variable

age >= 24 years

dia use of diaphragm

oc use of oral contraceptive

vic use of condom

vicl use of lubricated condom

vis use of spermicide
```

## Source

```
https://www.cytel.com/
```

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### References

Cytel Inc., (2010) LogXact 9 user manual, Cambridge, MA:Cytel Inc

sexagg

Urinary Tract Infection in American College Students

## **Description**

This data set deals with urinary tract infection in sexually active college women, along with covariate information on age an contraceptive use. The variables are all binary and coded in 1 (condition is present) and 0 (condition is absent): case (urinary tract infection, the study outcome variable), age (>= 24 years), dia (use of diaphragm), oc (use of oral contraceptive), vic (use of condom), vicl (use of lubricated condom), and vis (use of spermicide).

## Usage

sexagg

#### **Format**

sexagg: an aggregated data.frame containing 31 observations with case weights (COUNT).

case urinary tract infection, the study outcome variable

age >= 24 years

dia use of diaphragm

oc use of oral contraceptive

vic use of condom

vicl use of lubricated condom

vis use of spermicide

## **Source**

```
https://www.cytel.com/
```

## References

Cytel Inc., (2010) LogXact 9 user manual, Cambridge, MA:Cytel Inc

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