Package 'logspline'

April 25, 2022

Version 2.1.17 **Date** 2022-04-24

Maintainer Charles Kooperberg <clk@fredhutch.org></clk@fredhutch.org>	
Title Routines for Logspline Density Estimation	
Description Contains routines for logspline density estimation. The function oldlogspline() uses the same algorithm as the logspline package version 1.0.x; i.e. the Kooperberg and Stone (1992) algorithm (with an improved interface). The recommended routine logspline() uses an algorithm from Stone et al (1997) <doi:10.1214 1031594728="" aos="">.</doi:10.1214>	
Imports stats, graphics	
License Apache License 2.0	
NeedsCompilation yes	
Author Charles Kooperberg [aut, cre], Cleve Moler [ctb] (LINPACK routines in src), Jack Dongarra [ctb] (LINPACK routines in src)	
Repository CRAN	
Date/Publication 2022-04-25 07:30:02 UTC	
R topics documented:	
dlogspline doldlogspline logspline oldlogspline oldlogspline plot.logspline plot.oldlogspline summary.logspline summary.oldlogspline unstrip	3 4 7 9 10 12 13 14
Index	17

2 dlogspline

dlogspline

Logspline Density Estimation

Description

Density (dlogspline), cumulative probability (plogspline), quantiles (qlogspline), and random samples (rlogspline) from a logspline density that was fitted using the 1997 knot addition and deletion algorithm (logspline). The 1992 algorithm is available using the oldlogspline function.

Usage

```
dlogspline(q, fit)
plogspline(q, fit)
qlogspline(p, fit)
rlogspline(n, fit)
```

Arguments

q	vector of quantiles. Missing values (NAs) are allowed.
p	vector of probabilities. Missing values (NAs) are allowed.
n	sample size. If $length(n)$ is larger than 1, then $length(n)$ random values are returned.
fit	logspline object, typically the result of logspline.

Details

Elements of q or p that are missing will cause the corresponding elements of the result to be missing.

Value

Densities (dlogspline), probabilities (plogspline), quantiles (qlogspline), or a random sample (rlogspline) from a logspline density that was fitted using knot addition and deletion.

Author(s)

Charles Kooperberg <clk@fredhutch.org>.

References

Charles Kooperberg and Charles J. Stone. Logspline density estimation for censored data (1992). *Journal of Computational and Graphical Statistics*, **1**, 301–328.

Charles J. Stone, Mark Hansen, Charles Kooperberg, and Young K. Truong. The use of polynomial splines and their tensor products in extended linear modeling (with discussion) (1997). *Annals of Statistics*, **25**, 1371–1470.

doldlogspline 3

See Also

logspline, plot.logspline, summary.logspline, oldlogspline.

Examples

```
x <- rnorm(100)
fit <- logspline(x)
qq <- qlogspline((1:99)/100, fit)
plot(qnorm((1:99)/100), qq)  # qq plot of the fitted density
pp <- plogspline((-250:250)/100, fit)
plot((-250:250)/100, pp, type = "l")
lines((-250:250)/100, pnorm((-250:250)/100))  # asses the fit of the distribution
dd <- dlogspline((-250:250)/100, fit)
plot((-250:250)/100, dd, type = "l")
lines((-250:250)/100, dnorm((-250:250)/100))  # asses the fit of the density
rr <- rlogspline(100, fit)  # random sample from fit</pre>
```

doldlogspline

Logspline Density Estimation - 1992 version

Description

Probability density function (doldlogspline), distribution function (poldlogspline), quantiles (qoldlogspline), and random samples (roldlogspline) from a logspline density that was fitted using the 1992 knot deletion algorithm (oldlogspline). The 1997 algorithm using knot deletion and addition is available using the logspline function.

Usage

```
doldlogspline(q, fit)
poldlogspline(q, fit)
qoldlogspline(p, fit)
roldlogspline(n, fit)
```

Arguments

```
    vector of quantiles. Missing values (NAs) are allowed.
    vector of probabilities. Missing values (NAs) are allowed.
    sample size. If length(n) is larger than 1, then length(n) random values are returned.
    oldlogspline object, typically the result of oldlogspline.
```

Details

Elements of q or p that are missing will cause the corresponding elements of the result to be missing.

4 logspline

Value

Densities (doldlogspline), probabilities (poldlogspline), quantiles (qoldlogspline), or a random sample (roldlogspline) from an oldlogspline density that was fitted using knot deletion.

Author(s)

Charles Kooperberg <clk@fredhutch.org>.

References

Charles Kooperberg and Charles J. Stone. Logspline density estimation for censored data (1992). *Journal of Computational and Graphical Statistics*, **1**, 301–328.

Charles J. Stone, Mark Hansen, Charles Kooperberg, and Young K. Truong. The use of polynomial splines and their tensor products in extended linear modeling (with discussion) (1997). *Annals of Statistics*, **25**, 1371–1470.

See Also

logspline, oldlogspline, plot.oldlogspline, summary.oldlogspline

Examples

```
x <- rnorm(100)
fit <- oldlogspline(x)
qq <- qoldlogspline((1:99)/100, fit)
plot(qnorm((1:99)/100), qq)  # qq plot of the fitted density
pp <- poldlogspline((-250:250)/100, fit)
plot((-250:250)/100, pp, type = "l")
lines((-250:250)/100, pnorm((-250:250)/100)) # asses the fit of the distribution
dd <- doldlogspline((-250:250)/100, fit)
plot((-250:250)/100, dd, type = "l")
lines((-250:250)/100, dnorm((-250:250)/100)) # asses the fit of the density
rr <- roldlogspline(100, fit) # random sample from fit</pre>
```

logspline

Logspline Density Estimation

Description

Fits a logspline density using splines to approximate the log-density using the 1997 knot addition and deletion algorithm (logspline). The 1992 algorithm is available using the oldlogspline function.

Usage

```
logspline(x, lbound, ubound, maxknots = 0, knots, nknots = 0, penalty, silent = TRUE, mind = -1, error.action = 2)
```

5 logspline

Arguments

data vector. The data needs to be uncensored. oldlogspline can deal with Х

right- left- and interval-censored data.

lbound, ubound lower/upper bound for the support of the density. For example, if there is a priori

> knowledge that the density equals zero to the left of 0, and has a discontinuity at 0, the user could specify 1bound = 0. However, if the density is essentially zero

near 0, one does not need to specify 1bound.

maxknots the maximum number of knots. The routine stops adding knots when this num-

ber of knots is reached. The method has an automatic rule for selecting max-

knots if this parameter is not specified.

knots ordered vector of values (that should cover the complete range of the observa-

tions), which forces the method to start with these knots. Overrules knots. If

knots is not specified, a default knot-placement rule is employed.

nknots forces the method to start with nknots knots. The method has an automatic rule

for selecting nknots if this parameter is not specified.

penalty the parameter to be used in the AIC criterion. The method chooses the number

> of knots that minimizes -2 * loglikelihood + penalty * (number of knots -1). The default is to use a penalty parameter of penalty = log(samplesize) as in BIC. The effect of this parameter is summarized in summary. logspline.

silent should diagnostic output be printed?

mind minimum distance, in order statistics, between knots.

error.action how should logspline deal with non-convergence problems? Very-very rarely

in some extreme situations logspline has convergence problems. The only two situations that I am aware of are when there is effectively a sharp bound, but this bound was not specified, or when the data is severly rounded. logspline can deal with this in three ways. If error action is 2, the same data is rerun with the slightly more stable, but less flexible oldlogspline. The object is translated in a logspline object using oldlogspline. to.logspline, so this is almost invisible to the user. It is particularly useful when you run simulation studies, as he code can seemlessly continue. Only the 1bound and ubound options are passed on to oldlogspline, other options revert to the default. If error.action is 1, a warning is printed, and logspline returns nothing (but does not crash). This is useful if you run a simulation, but do not like to revert to oldlogspline. If error. action is 0, the code crashes using the stop function.

Value

Object of the class logspline, that is intended as input for plot.logspline (summary plots), summary, logspline (fitting summary), dlogspline (densities), plogspline (probabilities), qlogspline (quantiles), rlogspline (random numbers from the fitted distribution).

The object has the following members:

call the command that was executed.

nknots the number of knots in the model that was selected. 6 logspline

coef.pol	coefficients of the polynomial part of the spline. The first coefficient is the constant term and the second is the linear term.	
coef.kts	coefficients of the knots part of the spline. The k-th element is the coefficient of $(x-t(k))^3_+$ (where x^3_+ means the positive part of the third power of x , and $t(k)$ means knot k).	
knots	vector of the locations of the knots in the logspline model.	
maxknots	the largest number of knots minus one considered during fitting (i.e. with maxknots = 6 the maximum number of knots is 5).	
penalty	the penalty that was used.	
bound	first element: 0 - 1bound was $-\inf 1$ it was something else; second element: 1bound, if specified; third element: 0 - ubound was \inf , 1 it was something else; fourth element: ubound, if specified.	
samples	the sample size.	
logl	matrix with 3 columns. Column one: number of knots; column two: model fitted during addition (1) or deletion (2); column 3: log-likelihood.	
range	range of the input data.	
mind	minimum distance in order statistics between knots required during fitting (the actual minimum distance may be much larger).	

Author(s)

Charles Kooperberg <clk@fredhutch.org>.

References

Charles Kooperberg and Charles J. Stone. Logspline density estimation for censored data (1992). *Journal of Computational and Graphical Statistics*, **1**, 301–328.

Charles J. Stone, Mark Hansen, Charles Kooperberg, and Young K. Truong. The use of polynomial splines and their tensor products in extended linear modeling (with discussion) (1997). *Annals of Statistics*, **25**, 1371–1470.

See Also

```
plot.logspline, summary.logspline, dlogspline, plogspline, qlogspline, rlogspline, oldlogspline, oldlogspline.to.logspline.
```

Examples

```
y <- rnorm(100)
fit <- logspline(y)
plot(fit)
#
# as (4 == length(-2, -1, 0, 1, 2) -1), this forces these initial knots,
# and does no knot selection
fit <- logspline(y, knots = c(-2, -1, 0, 1, 2), maxknots = 4, penalty = 0)
#
# the following example give one of the rare examples where logspline</pre>
```

oldlogspline 7

```
# crashes, and this shows the use of error.action = 2.
#
set.seed(118)
zz <- rnorm(300)
zz[151:300] <- zz[151:300]+5
zz <- round(zz)
fit <- logspline(zz)
#
# you could rerun this with
# fit <- logspline(zz, error.action=0)
# or
# fit <- logspline(zz, error.action=1)</pre>
```

oldlogspline

Logspline Density Estimation - 1992 version

Description

Fits a logspline density using splines to approximate the log-density using the 1992 knot deletion algorithm (oldlogspline). The 1997 algorithm using knot deletion and addition is available using the logspline function.

Usage

```
oldlogspline(uncensored, right, left, interval, lbound,
ubound, nknots, knots, penalty, delete = TRUE)
```

and the default for ubound is inf.

Arguments

uncensored	vector of uncensored observations from the distribution whose density is to be estimated. If there are no uncensored observations, this argument can be omitted. However, either uncensored or interval must be specified.
right	vector of right censored observations from the distribution whose density is to be estimated. If there are no right censored observations, this argument can be omitted.
left	vector of left censored observations from the distribution whose density is to be estimated. If there are no left censored observations, this argument can be omitted.
interval	two column matrix of lower and upper bounds of observations that are interval censored from the distribution whose density is to be estimated. If there are no interval censored observations, this argument can be omitted.
lbound, ubound	lower/upper bound for the support of the density. For example, if there is a priori knowledge that the density equals zero to the left of 0, and has a discontinuity at 0, the user could specify 1bound = 0. However, if the density is essentially zero near 0, one does not need to specify 1bound. The default for 1bound is -inf

8 oldlogspline

nknots forces the method to start with nknots knots (delete = TRUE) or to fit a den-

sity with nknots knots (delete = FALSE). The method has an automatic rule for

selecting nknots if this parameter is not specified.

knots ordered vector of values (that should cover the complete range of the observa-

tions), which forces the method to start with these knots (delete = TRUE) or to fit a density with these knots delete = FALSE). Overrules nknots. If knots is

not specified, a default knot-placement rule is employed.

penalty the parameter to be used in the AIC criterion. The method chooses the number

of knots that minimizes -2 * loglikelihood + penalty * (number of knots -1). The default is to use a penalty parameter of penalty = log(samplesize) as in BIC. The effect of this parameter is summarized in summary.oldlogspline.

delete should stepwise knot deletion be employed?

Value

Object of the class oldlogspline, that is intended as input for plot.oldlogspline, summary.oldlogspline, doldlogspline (densities), poldlogspline (probabilities), qoldlogspline (quantiles), roldlogspline (random numbers from the fitted distribution). The function oldlogspline.to.logspline can translate an object of the class oldlogspline to an object of the class logspline.

The object has the following members:

call the command that was executed.

knots vector of the locations of the knots in the oldlogspline model. old

coef coefficients of the spline. The first coefficient is the constant term, the second

is the linear term and the k-th (k > 2) is the coefficient of $(x - t(k - 2))_+^3$ (where x_+^3 means the positive part of the third power of x, and t(k - 2) means knot k - 2). If a coefficient is zero the corresponding knot was deleted from the

model.

bound first element: 0 - 1bound was $-\inf 1$ it was something else; second element:

1bound, if specified; third element: 0 - ubound was inf, 1 it was something else;

fourth element: ubound, if specified.

log1 the k-th element is the log-likelihood of the fit with k+2 knots.

penalty the penalty that was used.
sample the sample size that was used.

delete was stepwise knot deletion employed?

Author(s)

Charles Kooperberg <clk@fredhutch.org>.

References

Charles Kooperberg and Charles J. Stone. Logspline density estimation for censored data (1992). *Journal of Computational and Graphical Statistics*, **1**, 301–328.

Charles J. Stone, Mark Hansen, Charles Kooperberg, and Young K. Truong. The use of polynomial splines and their tensor products in extended linear modeling (with discussion) (1997). *Annals of Statistics*, **25**, 1371–1470.

See Also

logspline, oldlogspline, plot.oldlogspline, summary.oldlogspline, doldlogspline, poldlogspline, qoldlogspline, roldlogspline, oldlogspline.to.logspline.

Examples

```
# A simple example
y <- rnorm(100)
fit <- oldlogspline(y)
plot(fit)
# An example involving censoring and a lower bound
y <- rlnorm(1000)
censoring <- rexp(1000) * 4
delta <- 1 * (y <= censoring)
y[delta == 0] <- censoring[delta == 0]
fit <- oldlogspline(y[delta == 1], y[delta == 0], lbound = 0)</pre>
```

oldlogspline.to.logspline

Logspline Density Estimation - 1992 to 1997 version

Description

Translates an oldlogspline object in an logspline object. This routine is mostly used in logspline, as it allows the routine to use oldlogspline for some situations where logspline crashes. The other use is when you have censored data, and thus have to use oldlogspline to fit, but wish to use the auxiliary routines from logspline.

Usage

```
oldlogspline.to.logspline(obj, data)
```

Arguments

obj object of class logspline

data the original data. Used to compute the range component of the new object. if

data is not available, the 1/(n+1) and n/(n+1) quantiles of the fitted distribution

are used for range.

Value

object of the class logspline. The call component of the new object is not useful. The delete component of the old object is ignored.

10 plot.logspline

Author(s)

Charles Kooperberg <clk@fredhutch.org>.

References

Charles Kooperberg and Charles J. Stone. Logspline density estimation for censored data (1992). *Journal of Computational and Graphical Statistics*, **1**, 301–328.

Charles J. Stone, Mark Hansen, Charles Kooperberg, and Young K. Truong. The use of polynomial splines and their tensor products in extended linear modeling (with discussion) (1997). *Annals of Statistics*, **25**, 1371–1470.

See Also

```
logspline, oldlogspline.
```

Examples

```
x <- rnorm(100)
fit.old <- oldlogspline(x)
fit.translate <- oldlogspline.to.logspline(fit.old,x)
fit.new <- logspline(x)
plot(fit.new)
plot(fit.old,add=TRUE,col=2)
#
# should look almost the same, the differences are the
# different fitting routines
#</pre>
```

plot.logspline

Logspline Density Estimation

Description

Plots a logspline density, distribution function, hazard function or survival function from a logspline density that was fitted using the 1997 knot addition and deletion algorithm (logspline). The 1992 algorithm is available using the oldlogspline function.

Usage

```
## S3 method for class 'logspline'
plot(x, n = 100, what = "d", add = FALSE, xlim, xlab = "",
ylab = "", type = "l", ...)
```

plot.logspline 11

Arguments

Х	logspline object, typically the result of logspline.
n	the number of equally spaced points at which to plot the density.
what	what should be plotted: "d" (density), "p" (distribution function), "s" (survival function) or "h" (hazard function).
add	should the plot be added to an existing plot.
xlim	range of data on which to plot. Default is from the 1th to the 99th percentile of the density, extended by 10% on each end.
xlab,ylab	labels plotted on the axes.
type	type of plot.
	other plotting options, as desired

Details

This function produces a plot of a logspline fit at n equally spaced points roughly covering the support of the density. (Use xlim = c(from, to) to change the range of these points.)

Author(s)

Charles Kooperberg <clk@fredhutch.org>.

References

Charles Kooperberg and Charles J. Stone. Logspline density estimation for censored data (1992). *Journal of Computational and Graphical Statistics*, **1**, 301–328.

Charles J. Stone, Mark Hansen, Charles Kooperberg, and Young K. Truong. The use of polynomial splines and their tensor products in extended linear modeling (with discussion) (1997). *Annals of Statistics*, **25**, 1371–1470.

See Also

```
logspline, summary.logspline, dlogspline, plogspline, qlogspline, rlogspline, oldlogspline.
```

Examples

```
y <- rnorm(100)
fit <- logspline(y)
plot(fit)</pre>
```

12 plot.oldlogspline

plot.oldlogspline Logspline Density Estimation - 1992 version	plot.oldlogspline	Logspline Density Estimation - 1992 version	
---	-------------------	---	--

Description

Plots an oldlogspline density, distribution function, hazard function or survival function from a logspline density that was fitted using the 1992 knot deletion algorithm. The 1997 algorithm using knot deletion and addition is available using the logspline function.

Usage

```
## S3 method for class 'oldlogspline'
plot(x, n = 100, what = "d", xlim, xlab = "", ylab = "",
type = "l", add = FALSE, ...)
```

Arguments

X	logspline object, typically the result of logspline.
n	the number of equally spaced points at which to plot the density.
what	what should be plotted: "d" (density), "p" (distribution function), "s" (survival function) or "h" (hazard function).
xlim	range of data on which to plot. Default is from the 1th to the 99th percentile of the density, extended by 10% on each end.
xlab,ylab	labels plotted on the axes.
type	type of plot.
add	should the plot be added to an existing plot.
	other plotting options, as desired

Details

This function produces a plot of a oldlogspline fit at n equally spaced points roughly covering the support of the density. (Use xlim=c(from, to) to change the range of these points.)

Author(s)

Charles Kooperberg <clk@fredhutch.org>.

References

Charles Kooperberg and Charles J. Stone. Logspline density estimation for censored data (1992). *Journal of Computational and Graphical Statistics*, **1**, 301–328.

Charles J. Stone, Mark Hansen, Charles Kooperberg, and Young K. Truong. The use of polynomial splines and their tensor products in extended linear modeling (with discussion) (1997). *Annals of Statistics*, **25**, 1371–1470.

summary.logspline 13

See Also

logspline, oldlogspline, summary.oldlogspline, doldlogspline, poldlogspline, qoldlogspline, roldlogspline.

Examples

```
y <- rnorm(100)
fit <- oldlogspline(y)
plot(fit)</pre>
```

summary.logspline

Logspline Density Estimation

Description

This function summarizes both the stepwise selection process of the model fitting by logspline, as well as the final model that was selected using AIC/BIC. A logspline object was fit using the 1997 knot addition and deletion algorithm. The 1992 algorithm is available using the oldlogspline function.

Usage

```
## S3 method for class 'logspline'
summary(object, ...)
## S3 method for class 'logspline'
print(x, ...)
```

Arguments

```
object, x logspline object, typically the result of logspline ... other arguments are ignored.
```

Details

These function produce identical printed output. The main body is a table with five columns: the first column is a possible number of knots for the fitted model;

the second column is the log-likelihood for the fit;

the third column is -2 * loglikelihood + penalty * (number of knots -1), which is the AIC criterion; logspline selected the model with the smallest value of AIC;

the fourth and fifth columns give the endpoints of the interval of values of penalty that would yield the model with the indicated number of knots. (NAs imply that the model is not optimal for any choice of penalty.) At the bottom of the table the number of knots corresponding to the selected model is reported, as is the value of penalty that was used.

Author(s)

Charles Kooperberg <clk@fredhutch.org>.

References

Charles Kooperberg and Charles J. Stone. Logspline density estimation for censored data (1992). *Journal of Computational and Graphical Statistics*, **1**, 301–328.

Charles J. Stone, Mark Hansen, Charles Kooperberg, and Young K. Truong. The use of polynomial splines and their tensor products in extended linear modeling (with discussion) (1997). *Annals of Statistics*, **25**, 1371–1470.

See Also

```
logspline, plot.logspline, dlogspline, plogspline, qlogspline, rlogspline, oldlogspline.
```

Examples

```
y <- rnorm(100)
fit <- logspline(y)
summary(fit)</pre>
```

summary.oldlogspline

Logspline Density Estimation - 1992 version

Description

This function summarizes both the stepwise selection process of the model fitting by oldlogspline, as well as the final model that was selected using AIC/BIC. A logspline object was fit using the 1992 knot deletion algorithm (oldlogspline). The 1997 algorithm using knot deletion and addition is available using the logspline function.

Usage

```
## S3 method for class 'oldlogspline'
summary(object, ...)
## S3 method for class 'oldlogspline'
print(x, ...)
```

Arguments

```
object, x oldlogspline object, typically the result of oldlogspline ... other arguments are ignored.
```

Details

These function produces the same printed output. The main body is a table with five columns: the first column is a possible number of knots for the fitted model;

the second column is the log-likelihood for the fit;

unstrip 15

the third column is -2 * loglikelihood + penalty * (number of knots -1), which is the AIC criterion; logspline selected the model with the smallest value of AIC;

the fourth and fifth columns give the endpoints of the interval of values of penalty that would yield the model with the indicated number of knots. (NAs imply that the model is not optimal for any choice of penalty.) At the bottom of the table the number of knots corresponding to the selected model is reported, as is the value of penalty that was used.

Author(s)

Charles Kooperberg <clk@fredhutch.org>.

References

Charles Kooperberg and Charles J. Stone. Logspline density estimation for censored data (1992). *Journal of Computational and Graphical Statistics*, **1**, 301–328.

Charles J. Stone, Mark Hansen, Charles Kooperberg, and Young K. Truong. The use of polynomial splines and their tensor products in extended linear modeling (with discussion) (1997). *Annals of Statistics*, **25**, 1371–1470.

See Also

logspline, oldlogspline, plot.oldlogspline, doldlogspline, poldlogspline, qoldlogspline, roldlogspline.

Examples

```
y <- rnorm(100)
fit <- oldlogspline(y)
summary(fit)</pre>
```

unstrip

Reformat data as vector or matrix

Description

This function tries to convert a date.frame or a matrix to a no-frills matrix without labels, and a vector or time-series to a no-frills vector without labels.

Usage

```
unstrip(x)
```

Arguments

Χ

one- or two-dimensional object.

16 unstrip

Details

Many of the functions for logspline, oldlogspline, were written in the "before data.frame" era; unstrip attempts to keep all these functions useful with more advanced input objects. In particular, many of these functions call unstrip before doing anything else.

Value

If x is two-dimensional a matrix without names, if x is one-dimensional a numerical vector

Author(s)

Charles Kooperberg <clk@fredhutch.org>.

Examples

data(co2)
unstrip(co2)
data(iris)
unstrip(iris)

Index

```
* classes
                                                  print.oldlogspline
    unstrip, 15
                                                           (summary.oldlogspline), 14
* distribution
                                                  qlogspline, 5, 6, 11, 14
    dlogspline, 2
                                                  qlogspline (dlogspline), 2
    doldlogspline, 3
                                                  qoldlogspline, 8, 9, 13, 15
    logspline, 4
                                                  qoldlogspline (doldlogspline), 3
    oldlogspline, 7
    oldlogspline.to.logspline,9
                                                  rlogspline, 5, 6, 11, 14
    plot.logspline, 10
                                                  rlogspline (dlogspline), 2
    plot.oldlogspline, 12
                                                  roldlogspline, 8, 9, 13, 15
    summary.logspline, 13
                                                  roldlogspline (doldlogspline), 3
    summary.oldlogspline, 14
* smooth
                                                  summary.logspline, 3, 5, 6, 11, 13
    dlogspline, 2
                                                  summary.oldlogspline, 4, 8, 9, 13, 14
    doldlogspline, 3
    logspline, 4
                                                  unstrip, 15
    oldlogspline, 7
    oldlogspline.to.logspline,9
    plot.logspline, 10
    plot.oldlogspline, 12
    summary.logspline, 13
    summary.oldlogspline, 14
* utilities
    unstrip, 15
dlogspline, 2, 5, 6, 11, 14
doldlogspline, 3, 8, 9, 13, 15
logspline, 2-4, 4, 7, 9-16
oldlogspline, 2-7, 7, 9-16
oldlogspline.to.logspline, 6, 8, 9, 9
plogspline, 5, 6, 11, 14
plogspline (dlogspline), 2
plot.logspline, 3, 5, 6, 10, 14
plot.oldlogspline, 4, 8, 9, 12, 15
poldlogspline, 8, 9, 13, 15
poldlogspline (doldlogspline), 3
print.logspline (summary.logspline), 13
```