# Package 'modEvA'

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**Description** Analyses species distribution models and evaluates their performance. It includes functions for performing variation partitioning, calculating several measures of model discrimination and calibration, optimizing prediction thresholds based on a number of criteria, performing multivariate environmental similarity surface (MESS) analysis, and displaying various analytical plots.

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modEvA-package

Model Evaluation and Analysis

## Description

The modEvA package can analyse species distribution models and evaluate their performance. It includes functions for performing variation partitioning; calculating several measures of model discrimination, classification, explanatory power, and calibration; optimizing prediction thresholds based on a number of criteria; performing multivariate environmental similarity surface (MESS) analysis; and displaying various analytical plots.

modEvA
Package
3.5
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GPL-3

## Author(s)

Barbosa A.M., Brown J.A., Jimenez-Valverde A., Real R.

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#### References

Barbosa A.M., Real R., Munoz A.R. & Brown J.A. (2013) New measures for assessing model equilibrium and prediction mismatch in species distribution models. Diversity and Distributions 19: 1333-1338 (DOI: 10.1111/ddi.12100)

#### See Also

#### PresenceAbsence, ROCR, verification

## Examples

```
# load sample models:
data(rotif.mods)
# choose a particular model to play with:
mod <- rotif.mods$models[[1]]</pre>
# plot this model:
plotGLM(model = mod)
# calculate the area under the ROC curve for the model:
AUC(model = mod)
# calculate some threshold-based measures for this model:
threshMeasures(model = mod, thresh = 0.5)
threshMeasures(model = mod, thresh = "preval")
# calculate optimal thresholds based on several criteria:
optiThresh(model = mod, measures = c("CCR", "Sensitivity", "kappa", "TSS"),
ylim = c(0, 1))
# calculate the optimal threshold balancing two evaluation measures:
optiPair(model = mod, measures = c("Sensitivity", "Specificity"))
```

```
# calculate the Boyce index, explained deviance, Hosmer-Lemeshow goodness-of-fit,
# Miller's calibration stats, and (pseudo) R-squared values for the model:
Boyce(model = mod)
Dsquared(model = mod)
HLfit(model = mod, bin.method = "quantiles")
MillerCalib(model = mod)
RsqGLM(model = mod)
# calculate a bunch of evaluation measures for a set of models:
multModEv(models = rotif.mods$models[1:4], thresh = "preval",
bin.method = "quantiles")
```

applyThreshold Apply a threshold to model predictions

## Description

This function applies a threshold value to the continuous predictions of a model, converting them to binary predictions -1 for values above the threshold, and 0 for values below it.

#### Usage

```
applyThreshold(model = NULL, obs = NULL, pred = NULL, thresh, right = FALSE,
interval = 0.01, quant = 0, na.rm = TRUE)
```

## Arguments

model	a binary-response model object of class "glm", "gam", "gbm", "randomForest" or "bart". If this argument is provided, 'obs' and 'pred' will be extracted with mod2obspred. Alternatively, you can input the 'obs' and 'pred' arguments instead of 'model'.
obs	alternatively to 'model' and together with 'pred', a numeric vector of observed presences (1) and absences (0) of a binary response variable. Alternatively (and if 'pred' is a 'SpatRaster'), a two-column matrix or data frame containing, respectively, the x (longitude) and y (latitude) coordinates of the presence points, in which case the 'obs' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
pred	alternatively to 'model' and together with 'obs', a vector with the correspond- ing predicted values of presence probability, habitat suitability, environmental favourability or alike. Must be of the same length and in the same order as 'obs'. Alternatively (and if 'obs' is a set of point coordinates), a 'SpatRaster' map of the predicted values for the entire evaluation region, in which case the 'pred' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
thresh	numeric threshold value within the limits of 'pred', or a criterion under which to compute the threshold – run modEvAmethods("getThreshold") for available options, and see Details in getThreshold for their description.

right	logical value indicating if the interval should be closed on the right (and open on the left) or vice versa, i.e., if the threshold value itself should be classified as 0 rather than 1. The default is FALSE.
interval	Argument to pass to optiThresh indicating the interval between the thresholds to test, if 'thresh' implies optimizing a threshold-based measure. The default is 0.01. Smaller values may provide more precise results but take longer to compute.
quant	Numeric value indicating the proportion of presences to discard if thresh="MTP" (minimum training presence). With the default value 0, MTP will be the threshold at which all observed presences are classified as such; with e.g. quant=0.05, MTP will be the threshold at which 5% presences will be classified as absences.
na.rm	Logical value indicating whether NA values should be ignored. Defaults to TRUE.

Several criteria have been proposed for selecting a threshold with which to convert continuous model predictions (of presence probability, habitat suitability or alike) into binary predictions of presence or absence. A threshold is required for computing threshold-based model evaluation metrics, such as those in threshMeasures. This function reclassifies the predictions of a model given a numeric threshold, or a threshold selection criterion implemented in getThreshold.

## Value

This function returns an object of the same class as 'pred' with the reclassified values after application of the threshold.

#### Author(s)

A. Marcia Barbosa

#### See Also

getThreshold, threshMeasures

## Examples

```
# load sample models:
data(rotif.mods)
```

# choose a particular model to play with: mod <- rotif.mods\$models[[1]]</pre>

```
applyThreshold(model = mod, thresh = "maxTSS")
```

# you can also use applyThreshold with vectors of observed and predicted values:

presabs <- mod\$y
prediction <- mod\$fitted.values</pre>

```
applyThreshold(pred = prediction, thresh = "meanPred")
applyThreshold(obs = presabs, pred = prediction, thresh = "preval")
applyThreshold(obs = presabs, pred = prediction, thresh = "MTP")
applyThreshold(obs = presabs, pred = prediction, thresh = "MTP",
quant = 0.05)
# 'obs' can also be a table of presence point coordinates
# and 'pred' a SpatRaster of predicted values
```

arrangePlots Arrange plots

## Description

Get an appropriate row/column combination (for par(mfrow)) for arranging a given number of plots within a plotting window.

## Usage

```
arrangePlots(n.plots, landscape = FALSE)
```

#### Arguments

n.plots	number of plots to be placed in the graphics device.
landscape	logical, whether the plotting window should be landscape/horizontal (number
	of columns larger than the number of rows) or not. The value does not make a
	difference if the number of plots makes for a square plotting window.

## Details

This function is used internally by optiThresh, but can also be useful outside it.

## Value

An integer vector of the form c(nr, nc) indicating, respectively, the number of rows and of columns of plots to set in the graphics device.

## Author(s)

A. Marcia Barbosa

## See Also

plot, layout

## AUC

## Examples

```
arrangePlots(10)
arrangePlots(10, landscape = TRUE)
# a more practical example:
data(iris)
names(iris)
# say you want to plot all columns in a nicely arranged plotting window:
par(mfrow = arrangePlots(ncol(iris)))
for (i in 1:ncol(iris)) {
    plot(1:nrow(iris), iris[, i])
}
```

AUC

Area Under the Curve

#### Description

This function calculates the Area Under the Curve of the receiver operating characteristic (ROC) plot, or alternatively the precision-recall (PR) plot, for either a model object or two matching vectors of observed binary (1 for occurrence vs. 0 for non-occurrence) and predicted continuous (e.g. occurrence probability) values, respectively.

## Usage

```
AUC(model = NULL, obs = NULL, pred = NULL, simplif = FALSE,
interval = 0.01, FPR.limits = c(0, 1), curve = "ROC",
method = "rank", plot = TRUE, diag = TRUE, diag.col = "grey",
diag.lty = 1, curve.col = "black", curve.lty = 1, curve.lwd = 2,
plot.values = TRUE, plot.digits = 3, plot.preds = FALSE,
grid = FALSE, xlab = "auto", ylab = "auto", ticks = FALSE,
na.rm = TRUE, rm.dup = FALSE, ...)
```

## Arguments

model a binary-response model object of class "glm", "gam", "gbm", "randomForest" or "bart". If this argument is provided, 'obs' and 'pred' will be extracted with mod2obspred. Alternatively, you can input the 'obs' and 'pred' arguments instead of 'model'.

obs	alternatively to 'model' and together with 'pred', a numeric vector of observed presences (1) and absences (0) of a binary response variable. Alternatively (and if 'pred' is a 'SpatRaster'), a two-column matrix or data frame containing, respectively, the x (longitude) and y (latitude) coordinates of the presence points, in which case the 'obs' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
pred	alternatively to 'model' and together with 'obs', a vector with the correspond- ing predicted values of presence probability, habitat suitability, environmental favourability or alike. Must be of the same length and in the same order as 'obs'. Alternatively (and if 'obs' is a set of point coordinates), a 'SpatRaster' map of the predicted values for the entire evaluation region, in which case the 'pred' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
simplif	logical, whether to use a faster version that returns only the AUC value (and the plot if 'plot = TRUE').
FPR.limits	(NOT YET IMPLEMENTED) numerical vector of length 2 indicating the limits of false positive rate between which to calculate a partial AUC. The default is $c(0, 1)$ , for considering the whole AUC.
curve	character indicating whether to compute the "ROC" (receiver operating chara- teristic) or the "PR" (precision-recall) curve.
interval	interval of threshold values at which to calculate the true and false positive rates. Defaults to 0.01 for relatively quick while still relatively accurate computation. Note that, if method = "rank" (the default if curve = "ROC"), this does not affect the obtained AUC value (although it can affect the size of the plotted curve, especially when prevalence is low), as the AUC is calculated with the Mann-Whitney-Wilcoxon statistic and is therefore threshold-independent. If method != "rank" (or, by extension, if curve = "PR" – see 'method' argument), setting 'interval' to smaller values will provide more accurate AUC values. The size of the 'interval' also affects the resulting 'meanPrecision', as this is averaged across all threshold values.
method	character indicating with which method to calculate the AUC value. Available options are "rank" (the default and most accurate, but implemented only if curve = "ROC") and "trapezoid" (the default if curve = "PR"). The latter is computed more accurately if 'interval' is decreased (see 'interval' argument).
plot	logical, whether or not to plot the curve. Defaults to TRUE.
diag	logical, whether or not to add the reference diagonal (if plot = TRUE). Defaults to TRUE.
diag.col	line colour for the reference diagonal (if diag = TRUE).
diag.lty	line type for the reference diagonal (if diag = TRUE).
curve.col	line colour for the curve.
curve.lty	line type for the curve.
curve.lwd	line width for the curve.
plot.values	logical, whether or not to show in the plot the values associated to the curve (e.g., the AUC). Defaults to TRUE.

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plot.digits	should be rounded. Defaults to 3. This argument is ignored if 'plot' or 'plot.values' are set to FALSE.
plot.preds	logical value indicating whether the proportions of 'pred' values for each thresh- old should be plotted as proportionally sized blue circles. Can also be provided as a character vector specifying if the circles should be plotted on the "curve" (the default) and/or at the "bottom" of the plot. The default is FALSE for no cir- cles, but it may be interesting to try it, especially if your curve has long straight lines or does not cover the full length of the plot.
grid	logical, whether or not to add a grid to the plot, marking the analysed thresholds. Defaults to FALSE.
xlab	label for the x axis. By default, a label is automatically generated according to the specified 'curve'.
ylab	label for the y axis. By default, a label is automatically generated according to the specified 'curve'.
ticks	logical, whether or not to add blue tick marks at the bottom of the plot to mark the thresholds at which there were values from which to to draw the curve. De- faults to FALSE.
na.rm	Logical value indicating if missing values should be ignored in computations. The default is TRUE.
rm.dup	If TRUE and if 'pred' is a SpatRaster and if there are repeated points within the same pixel, a maximum of one point per pixel is used to compute the presences. See examples in ptsrast2obspred. The default is FALSE.
	further arguments to be passed to the plot function.

...

#### Details

In the case of the "ROC" curve (the default), the AUC is a measure of the overall discrimination power of the predictions, or the probability that an occurrence site has a higher predicted value than a non-occurrence site. It can thus be calculated with the Wilcoxon rank sum statistic, as is done with the default method="rank". There's also an option to compute, instead of the ROC curve, the precision-recall ("PR") curve, which is more robust to imbalanced data, e.g. species rarity (Sofaer et al. 2019), as it doesn't value true negatives.

If 'curve' is set to "PR", or if 'method' is manually set to "trapezoid", the AUC value will be more accurate if 'interval' is decreased (see 'method' and 'interval' arguments above). The plotted curve will also be more accurate with smaller 'interval' values, especially for imbalanced datasets (which can cause an apparent disagreement between the look of the curve and the actual value of the AUC).

Mind that the AUC has been widely criticized (e.g. Lobo et al. 2008, Jimenez-Valverde et al. 2013), but is still among the most widely used metrics in model evaluation. It is highly correlated with species prevalence (as are all model discrimination and classification metrics), so prevalence is also output by the AUC function (if simplif = FALSE, the default) for reference.

Although there are functions to calculate the AUC in other R packages (e.g. **ROCR**, **Presence-Absence**, **verification**, **Epi**, **PRROC**, **PerfMeas**, **precrec**), the AUC function is more compatible with the remaining functions in **modEvA**, and it can be applied not only to a set of observed vs. predicted values, but also directly to a model object of class "glm", "gam", "gbm", "randomForest" or "bart".

#### Value

If simplif = TRUE, the function returns only the AUC value (a numeric value between 0 and 1). Otherwise (the default), it returns a list with the following components:

thresholds	a data frame of the true and false positives, the sensitivity, specificity and recall of the predictions, and the number of predicted values at each analysed thresh- old.
Ν	the total number of obervations.
prevalence	the proportion of presences (i.e., ones) in the data (which correlates with the AUC of the "ROC" plot).
AUC	the value of the AUC).
AUCratio	the ratio of the obtained AUC value to the null expectation $(0.5)$ .
meanPrecision	the arithmetic mean of precision (proportion of predicted presences actually ob- served as presences) across all threshold values (defined by 'interval'). It is close to the AUC of the precision-recall (PR) curve.

## Author(s)

A. Marcia Barbosa

## References

Lobo, J.M., Jimenez-Valverde, A. & Real, R. (2008). AUC: a misleading measure of the performance of predictive distribution models. Global Ecology and Biogeography 17: 145-151

Jimenez-Valverde, A., Acevedo, P., Barbosa, A.M., Lobo, J.M. & Real, R. (2013). Discrimination capacity in species distribution models depends on the representativeness of the environmental domain. Global Ecology and Biogeography 22: 508-516

Sofaer, H.R., Hoeting, J.A. & Jarnevich, C.S. (2019). The area under the precision-recall curve as a performance metric for rare binary events. Methods in Ecology and Evolution, 10: 565-577

#### See Also

threshMeasures

#### Examples

```
# load sample models:
data(rotif.mods)
""
```

```
# choose a particular model to play with:
mod <- rotif.mods$models[[1]]</pre>
```

# compute the AUC:

AUC(model = mod, simplif = TRUE)

AUC(model = mod, curve = "PR")

#### Boyce

```
AUC(model = mod, interval = 0.1, grid = TRUE)
AUC(model = mod, plot.preds = TRUE)
AUC(model = mod, ticks = TRUE)
AUC(model = mod, plot.preds = c("curve", "bottom"))
# you can also use vectors of observed and predicted values
# instead of a model object:
presabs <- mod$y
prediction <- mod$fitted.values
AUC(obs = presabs, pred = prediction)
AUC(obs = presabs, pred = prediction, plot.preds = TRUE)
# 'obs' can also be a table of presence point coordinates
# and 'pred' a SpatRaster of predicted values</pre>
```

Boyce

Boyce Index

#### Description

This function computes the (continuous) Boyce index (Boyce 2002; Hirzel et al. 2006) for either: 1) a model object; or 2) two paired numeric vectors of observed (binary, 1 for occurrence vs. 0 for no occurrence records) and predicted (continuous, e.g. occurrence probability) values; or 3) a set of presence point coordinates and a raster map with the predicted values for the entire model evaluation area. This metric is designed for evaluating model predictions against presence/background data (i.e. presence/available, where "available" includes both presences and absences; Boyce 2002), so the function uses the model predictions for the presence sites (ones) against the predictions for the entire dataset (ones and zeros). The code is largely based on the 'ecospat.boyce' function in the **ecospat** package (version 3.2.1), but it is modified to match the input types in the remaining functions of 'modEvA', and to return a more complete output.

#### Usage

```
Boyce(model = NULL, obs = NULL, pred = NULL, n.bins = NA,
bin.width = "default", res = 100, method = "spearman", rm.dup.classes = FALSE,
rm.dup.points = FALSE, plot = TRUE, plot.lines = TRUE, plot.values = TRUE,
plot.digits = 3, na.rm = TRUE, ...)
```

## Arguments

guinents	
model	a binary-response model object of class "glm", "gam", "gbm", "randomForest" or "bart". If this argument is provided, 'obs' and 'pred' will be extracted with mod2obspred. Alternatively, you can input the 'obs' and 'pred' arguments (e.g. for external test data) instead of 'model'.
obs	alternatively to 'model' and together with 'pred', a numeric vector of observed presences (1) and absences (0) of a binary response variable. Alternatively (and if 'pred' is a 'SpatRaster'), a two-column matrix or data frame containing, respectively, the x (longitude) and y (latitude) coordinates of the presence points, in which case the 'obs' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
pred	alternatively to 'model' and together with 'obs', a vector with the correspond- ing predicted values of presence probability, habitat suitability, environmental favourability or alike. Must be of the same length and in the same order as 'obs'. Alternatively (and if 'obs' is a set of point coordinates), a 'SpatRaster' map of the predicted values for the entire evaluation region, in which case the 'pred' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
n.bins	number of classes or bins (e.g. 10) in which to group the 'pred' values, or a vector with the bin thresholds. If n.bins = NA (the default), a moving window is used (see next parameters), so as to compute the "continuous Boyce index" (Hirzel et al. 2006).
bin.width	width of the moving window (if n.bins = NA), in the units of 'pred' (e.g. 0.1). By default, it is 1/10th of the 'pred' range).
res	resolution of the moving window (if n.bins = NA). By default it is 100 focals, providing 100 moving bins).
method	argument to be passed to cor indicating which correlation coefficient to use. The default is 'spearman' as per Boyce et al. (2002), but 'pearson' and 'kendall' can also be used.
rm.dup.classes	if TRUE (as in 'ecospat::ecospat.boyce') and if there are different bins with the same predicted/expected ratio, only one of each is used to compute the correlation. See Examples.
rm.dup.points	if TRUE and if 'pred' is a SpatRaster and if there are repeated points within the same pixel, a maximum of one point per pixel is used to compute the presences. See examples in ptsrast2obspred. The default is FALSE.
plot	logical, whether or not to plot the predicted/expected ratio against the median prediction of each bin. Defaults to TRUE.
plot.lines	logical, whether or not to add lines connecting the points in the plot (if plot=TRUE). Defaults to TRUE.
plot.values	logical, whether or not to show in the plot the value of the Boyce index. Defaults to TRUE.
plot.digits	number of digits to which the value in the plot should be rounded (if 'plot' and 'plot.values' are TRUE). Defaults to 3.
na.rm	Logical value indicating if missing values should be removed from computa- tions. The default is TRUE.

#### Boyce

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#### Details

The Boyce index is the correlation between model predictions and area-adjusted frequencies (i.e., observed vs. expected proportion of occurrences) along different prediction classes. In other words, it measures how model predictions differ from a random distribution of the observed presences across the prediction gradient (Boyce et al. 2002). It can take values between -1 and 1. Positive values indicate that presences are more frequent than expected by chance (given availability) in areas with higher predicted values. Values close to zero mean that predictions are no better than random, and negative values indicate counter predictions, i.e. that presences are more frequent in areas with lower predicted values.

#### Value

This function returns a list with the following components:

- bins a data frame with the number of values in each bin, their median and range of predicted values, and the corresponding predicted/expected ratio of presences.
- B the numeric value of the Boyce index, i.e. the coefficient of correlation between the median predicted value in each bin and the corresponding predicted/expected ratio.

If plot=TRUE (the default), the function also plots the predicted/expected ratio for the utilized bins along the prediction range. A good model should yield a monotonically increasing curve (but see Note).

#### Note

In bins with overly small sample sizes, the comparison between median prediction and random expectation may not be meaningful, although these bins will equally contribute to the overall Boyce index. When there are bins with less than 30 values, a warning is emitted and their points are plotted in red, but note that 30 is a largely arbitrary number. See the \$bins\$bin.N section of the console output, and use the 'bin.width' argument to enlarge the bins.

#### Author(s)

A. Marcia Barbosa, with significant chunks of code from the 'ecospat::ecospat.boyce' function by Blaise Petitpierre and Frank Breiner (**ecospat** package version 3.2.1).

#### References

Boyce, M.S., P.R. Vernier, S.E. Nielsen & F.K.A. Schmiegelow (2002) Evaluating resource selection functions. Ecological Modelling 157: 281-300

Hirzel, A.H., G. Le Lay, V. Helfer, C. Randin & A. Guisan (2006) Evaluating the ability of habitat suitability models to predict species presences. Ecological Modelling 199: 142-152

## Examples

```
# load sample models:
data(rotif.mods)
# choose a particular model to play with:
mod <- rotif.mods$models[[1]]
# compute the Boyce index:
Boyce(model = mod, main = "My model Boyce plot")
Boyce(model = mod, main = "My model Boyce plot", rm.dup.classes = TRUE)
# you can also use vectors of observed and predicted values
# instead of a model object:
presabs <- mod$y
prediction <- mod$fitted.values
Boyce(obs = presabs, pred = prediction)
# 'obs' can also be a table of presence point coordinates
# and 'pred' a SpatRaster of predicted values
```

confusionLabel Label predictions according to their confusion matrix category

## Description

This function labels the predictions of a binary-response model according to their confusion matrix categories, i.e., it classifies each prediction into a false positive, false negative, true positive or true negative, given a user-defined threshold value.

## Usage

```
confusionLabel(model = NULL, obs = NULL, pred = NULL, thresh, verbosity = 2,
na.rm = FALSE, rm.dup = FALSE)
```

#### Arguments

model	a binary-response model object of class "glm", "gam", "gbm", "randomForest" or "bart". If this argument is provided, 'obs' and 'pred' will be extracted with mod2obspred. Alternatively, you can input the 'obs' and 'pred' arguments (e.g. for external test data) instead of 'model'.
obs	alternatively to 'model' and together with 'pred', a numeric vector of observed presences (1) and absences (0) of a binary response variable. Alternatively (and if 'pred' is a 'SpatRaster'), a two-column matrix or data frame containing, respectively, the x (longitude) and y (latitude) coordinates of the presence points,

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	in which case the 'obs' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
pred	alternatively to 'model' and together with 'obs', a vector with the correspond- ing predicted values of presence probability, habitat suitability, environmental favourability or alike. Must be of the same length and in the same order as 'obs'. Alternatively (and if 'obs' is a set of point coordinates), a 'SpatRaster' map of the predicted values for the entire evaluation region, in which case the 'pred' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
thresh	numeric value of the threshold to separate predicted presences from predicted absences; can be "preval", to use the prevalence of 'obs' (or of the response variable in 'model') as the threshold, or any real number between 0 and 1. See Details in threshMeasures for an informed choice.
verbosity	integer specifying the amount of messages to display. Defaults to the maximum implemented; lower numbers (down to 0) decrease the number of messages.
na.rm	logical argument indicating whether to remove (with a warning saying how many) rows with NA in any of the 'obs' or 'pred' values. The default is FALSE.
rm.dup	If TRUE and if 'pred' is a SpatRaster and if there are repeated points within the same pixel, a maximum of one point per pixel is used to compute the presences. See examples in ptsrast2obspred. The default is FALSE.

## Value

This function returns a character vector of the same length as 'obs' and 'pred', or of the same number of rows as the data in 'model', containing the confusion matrix label for each value.

## Author(s)

A. Marcia Barbosa

## See Also

threshMeasures

## Examples

```
# load sample models:
data(rotif.mods)
# choose a particular model to play with:
mod <- rotif.mods$models[[1]]
confusionLabel(model = mod, thresh = 0.5)
# you can instead use vectors of observed and predicted values:
presabs <- mod$y
prediction <- mod$fitted.values</pre>
```

```
confusionLabel(obs = presabs, pred = prediction, thresh = 0.5)
# 'obs' can also be a table of presence point coordinates
# and 'pred' a SpatRaster of predicted values
```

Dsquared

Proportion of deviance explained by a GLM

## Description

This function calculates the (adjusted) amount of deviance accounted for by a generalized linear model.

## Usage

Dsquared(model = NULL, obs = NULL, pred = NULL, family = NULL, adjust = FALSE, npar = NULL, na.rm = TRUE, rm.dup = FALSE)

## Arguments

model	a model object of class "glm". If this argument is provided, 'obs' and 'pred' will be extracted with mod2obspred. Alternatively, you can input the 'obs' and 'pred' arguments instead of 'model'.
obs	alternatively to 'model' and together with 'pred', a numeric vector of observed presences (1) and absences (0) of a binary response variable. Alternatively (and if 'pred' is a 'SpatRaster'), a two-column matrix or data frame containing, respectively, the x (longitude) and y (latitude) coordinates of the presence points, in which case the 'obs' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
pred	alternatively to 'model' and together with 'obs', a vector with the correspond- ing predicted values of presence probability, habitat suitability, environmental favourability or alike. Must be of the same length and in the same order as 'obs'. Alternatively (and if 'obs' is a set of point coordinates), a 'SpatRaster' map of the predicted values for the entire evaluation region, in which case the 'pred' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
family	a character vector (i.e. in quotes) of length 1 specifying the family of the GLM. This argument is ignored if model is provided; otherwise (i.e. if 'obs' and 'pred' are provided rather than a model object), only families 'binomial' (logit link) and 'poisson' (log link) are currently implemented.
adjust	logical, whether or not to adjust the D-squared value for the number of observations and parameters in the model (see Details). The default is FALSE; TRUE requires either providing the model object, or specifying the number of parameters in the model that produced the pred values.

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## Dsquared

npar	an integer vector indicating the number of parameters in the model. This argument is ignored if model is provided or if adjust = FALSE.
na.rm	Logical value indicating whether missing values should be ignored in computa- tions. Defaults to TRUE.
rm.dup	If TRUE and if 'pred' is a SpatRaster and if there are repeated points within the same pixel, a maximum of one point per pixel is used to compute the presences. See examples in ptsrast2obspred. The default is FALSE.

## Details

Linear models come with an R-squared value that measures the proportion of variation that the model accounts for. The R-squared is provided with summary(model) in R. For generalized linear models (GLMs), the equivalent is the amount of deviance accounted for (D-squared; Guisan & Zimmermann 2000), but this value is not normally provided with the model summary. The Dsquared function calculates it. There is also an option to calculate the adjusted D-squared, which takes into account the number of observations and the number of predictors, thus allowing direct comparison among different models (Weisberg 1980, Guisan & Zimmermann 2000).

#### Value

This function returns a numeric value indicating the (adjusted) proportion of deviance accounted for by the model.

## Author(s)

A. Marcia Barbosa

#### References

Guisan, A. & Zimmermann, N.E. (2000) Predictive habitat distribution models in ecology. Ecological Modelling 135: 147-186

Weisberg, S. (1980) Applied Linear Regression. Wiley, New York

#### See Also

glm, plotGLM

## Examples

```
# load sample models:
data(rotif.mods)
```

# choose a particular model to play with: mod <- rotif.mods\$models[[1]]</pre>

Dsquared(model = mod)

Dsquared(model = mod, adjust = TRUE)

#### evaluate

```
# you can also use Dsquared with vectors of observed and predicted values
# instead of with a model object:
presabs <- mod$y
prediction <- mod$fitted.values
parameters <- attributes(logLik(mod))$df
Dsquared(obs = presabs, pred = prediction, family = "binomial")
Dsquared(obs = presabs, pred = prediction, family = "binomial",
adjust = TRUE, npar = parameters)
# 'obs' can also be a table of presence point coordinates
```

```
# and 'pred' a SpatRaster of predicted values
```

```
evaluate
```

Evaluate a model based on the elements of a confusion matrix.

#### Description

This function evaluates the classification performance of a model based on the values of a confusion matrix obtained at a particular threshold.

#### Usage

evaluate(a, b, c, d, N = NULL, measure = "CCR")

#### Arguments

а	number of correctly predicted presences
b	number of absences incorrectly predicted as presences
с	number of presences incorrectly predicted as absences
d	number of correctly predicted absences
Ν	total number of cases. If NULL (the default), it is calculated automatically by adding up a, b, c and d.)
measure	a character vector of length 1 indicating the the evaluation measure to use. Type 'modEvAmethods("threshMeasures")' for available options.

## Details

A number of measures can be used to evaluate continuous model predictions against observed binary occurrence data (Fielding & Bell 1997; Liu et al. 2011; Barbosa et al. 2013). The 'evaluate' function can calculate a few threshold-based classification measures from the values of a confusion matrix obtained at a particular threshold. The 'evaluate' function is used internally by threshMeasures. It can also be accessed directly by the user, but it is usually more practical to use 'threshMeasures', which calculates the confusion matrix automatically.

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#### evenness

## Value

The value of the specified evaluation measure.

### Note

Some measures (e.g. NMI, odds ratio) don't work with zeros in (some parts of) the confusion matrix. Also, TSS and NMI are not symmetrical, i.e. "obs" vs "pred" different from "pred" vs "obs".

## Author(s)

A. Marcia Barbosa

#### References

Barbosa A.M., Real R., Munoz A.R. & Brown J.A. (2013) New measures for assessing model equilibrium and prediction mismatch in species distribution models. Diversity and Distributions, 19: 1333-1338

Fielding A.H. & Bell J.F. (1997) A review of methods for the assessment of prediction errors in conservation presence/absence models. Environmental Conservation 24: 38-49

Liu C., White M., & Newell G. (2011) Measuring and comparing the accuracy of species distribution models with presence-absence data. Ecography, 34, 232-243.

#### See Also

threshMeasures

#### Examples

```
evaluate(23, 44, 21, 34)
```

evaluate(23, 44, 21, 34, measure = "TSS")

evenness

Evenness in a binary vector.

## Description

For building and evaluating species distribution models, the porportion of presences (prevalence) of a species and the balance between the number of presences and absences may be issues to take into account (e.g. Jimenez-Valverde & Lobo 2006, Barbosa et al. 2013). The evenness function calculates the presence-absence balance in a binary (e.g., presence/absence) vector.

#### Usage

evenness(obs)

#### Arguments

obs

a vector of binary observations (e.g. 1 or 0, male or female, disease or no disease, etc.)

## Value

A number ranging between 0 when all values are the same, and 1 when there are the same number of cases with each value in obs.

## Author(s)

A. Marcia Barbosa

## References

Barbosa A.M., Real R., Munoz A.R. & Brown J.A. (2013) New measures for assessing model equilibrium and prediction mismatch in species distribution models. Diversity and Distributions, 19: 1333-1338

Jimenez-Valverde A. & Lobo J.M. (2006) The ghost of unbalanced species distribution data in geographical model predictions. Diversity and Distributions, 12: 521-524.

#### See Also

prevalence

#### Examples

(x <- rep(c(0, 1), each = 5)) (y <- c(rep(0, 3), rep(1, 7))) (z <- c(rep(0, 7), rep(1, 3))) prevalence(x) evenness(x)

prevalence(y)
evenness(y)

prevalence(z)
evenness(z)

getBins

Get bins of continuous values.

#### Description

Get continuous predicted values into bins according to specific criteria.

## getBins

## Usage

```
getBins(model = NULL, obs = NULL, pred = NULL, id = NULL,
bin.method, n.bins = 10, fixed.bin.size = FALSE, min.bin.size = 15,
min.prob.interval = 0.1, quantile.type = 7, simplif = FALSE,
verbosity = 2, na.rm = TRUE, rm.dup = FALSE)
```

## Arguments

model	a binary-response model object of class "glm", "gam", "gbm", "randomForest" or "bart". If this argument is provided, 'obs' and 'pred' will be extracted with mod2obspred. Alternatively, you can input the 'obs' and 'pred' arguments instead of 'model'.
obs	alternatively to 'model' and together with 'pred', a numeric vector of observed presences (1) and absences (0) of a binary response variable. Alternatively (and if 'pred' is a 'SpatRaster'), a two-column matrix or data frame containing, respectively, the x (longitude) and y (latitude) coordinates of the presence points, in which case the 'obs' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
pred	alternatively to 'model' and together with 'obs', a vector with the correspond- ing predicted values of presence probability, habitat suitability, environmental favourability or alike. Must be of the same length and in the same order as 'obs'. Alternatively (and if 'obs' is a set of point coordinates), a 'SpatRaster' map of the predicted values for the entire evaluation region, in which case the 'pred' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
id	optional vector of row identifiers; must be of the same length and in the same order of obs and pred (or of the cases used to build model)
bin.method	the method with which to divide the values into bins. Type modEvAmethods("getBins") for available options and see Details for more information on these methods.
n.bins	the number of bins in which to divide the data.
fixed.bin.size	logical, whether all bins should have (approximally) the same size.
min.bin.size	integer value defining the minimum number of observations to include in each bin. The default is 15, the minimum required for accurate comparisons within bins (Jovani & Tella 2006, Jimenez-Valverde et al. 2013).
min.prob.inter	
	minimum range of probability values in each bin. The default is 0.1.
quantile.type	argument to pass to quantile specifying the algorithm to use if bin.method = "quantiles". The default is 7 (the quantile default in R), but check out other types, e.g. 3 (used by SAS), 6 (used by Minitab and SPSS) or 5 (appropriate for deciles, which correspond to the default n.bins = 10).
simplif	logical, whether to calculate a faster, simplified version (used internally in other functions). The default is FALSE.
verbosity	integer specifying the amount of messages or warnings to display. Defaults to the maximum implemented; lower numbers (down to 0) decrease the number of messages.

na.rm	logical argument indicating whether to remove (with a warning saying how many) rows with NA in any of the 'obs' or 'pred' values. The default is TRUE, as some 'bin.method' options will fail if there are NAs.
rm.dup	If TRUE and if 'pred' is a SpatRaster and if there are repeated points within the same pixel, a maximum of one point per pixel is used to compute the presences. See examples in ptsrast2obspred. The default is FALSE.

Mind that different bin.methods can lead to visibly different results regarding the bins and any operations that depend on them (such as HLfit). Currently available bin.methods are:

- round.prob: probability values are rounded to the number of digits of min.prob.interval - e.g., if min.prob.interval = 0.1 (the default), values under 0.05 get into bin 1 (rounded probability = 0), values between 0.05 and 0.15 get into bin 2 (rounded probability = 0.1), etc. until values with probability over 0.95, which get into bin 11. Arguments n.bins, fixed.bin.size and min.bin.size are ignored by this bin.method.

- prob.bins: probability values are grouped into bins of the given probability intervals - e.g., if min.prob.interval = 0.1 (the default), bin 1 gets the values between 0 and 0.1, bin 2 gets the values between 0.1 and 0.2, etc. until bin 10 which gets the values between 0.9 and 1. Arguments n.bins, fixed.bin.size and min.bin.size are ignored by this bin.method.

- size.bins: probability values are grouped into bins of (approximately) equal size, defined by argument min.bin.size. Arguments n.bins and min.prob.interval are ignored by this bin.method.

- n.bins: probability values are divided into the number of bins given by argument n.bins, and their sizes may or may not be forced to be (approximately) equal, depending on argument fixed.bin.size (which is FALSE by default). Arguments min.bin.size and min.prob.interval are ignored by this bin.method.

- quantiles: probability values are divided using R function quantile, with probability cutpoints defined by the given n.bins (i.e., deciles by default), and with the quantile algorithm defined by argument quantile.type. Arguments fixed.bin.size, min.bin.size and min.prob.interval are ignored by this bin.method.

#### Value

The output of getBins is a list with the following components:

prob.bin	the first and last value of each bin
bins.table	a data frame with the sample size, number of presences, number of absences, prevalence, mean and median probability, and the difference between predicted and observed values (mean probability - observed prevalence) in each bin.
Ν	the total number of observations in the analysis.
n.bins	the total number of bins obtained.

## Note

This function is still under development and may fail for some datasets and binning methods (e.g., ties may sometimes preclude binning under some bin.methods). Fixes and further binning methods are in preparation. Feedback is welcome.

## getModEqn

### Author(s)

A. Marcia Barbosa

## References

Jimenez-Valverde A., Acevedo P., Barbosa A.M., Lobo J.M. & Real R. (2013) Discrimination capacity in species distribution models depends on the representativeness of the environmental domain. Global Ecology and Biogeography 22: 508-516.

Jovani R. & Tella J.L. (2006) Parasite prevalence and sample size: misconceptions and solutions. Trends in Parasitology 22: 214-218.

## See Also

HLfit

## Examples

```
# load sample models:
```

data(rotif.mods)

# choose a particular model to play with:

```
mod <- rotif.mods$models[[1]]</pre>
```

# try getBins using different binning methods:

```
getBins(model = mod, bin.method = "quantiles")
```

getBins(model = mod, bin.method = "n.bins")

```
getBins(model = mod, bin.method = "n.bins", fixed.bin.size = TRUE)
```

getModEqn Get model equation

## Description

This function retrieves the equation of a model, to print or apply elsewhere.

#### Usage

```
getModEqn(model, type = "Y", digits = NULL, prefix = NULL,
suffix = NULL)
```

#### Arguments

model	a model object of class 'lm' or glm'.
type	the type of equation to get; can be either "Y" (the default, for the linear model equation), "P" (for probability) or "F" (for favourability).
digits	the number of significant digits to which to round the coefficient estimates in the equation.
prefix	the prefix to add to each variable name in the equation.
suffix	the suffix to add to each variable name in the equation.

## Details

The summary of a model in R gives you a table of the coefficient estimates and other parameters. Sometimes it may be useful to have a string of text with the model's equation, so that you can present it in an article (e.g. Real et al. 2005) or apply it in a (raster map) calculation, either in R (although here you can usually use the 'predict' function for this) or in a GIS software (e.g. Barbosa et al. 2010). The getModEqn function gets this equation for linear or generalized linear models.

By default it prints the "Y" linear equation, but for generalized linear models you can also set type = "P" (for the equation of probability) or type = "F" (for favourability, which modifies the intercept to eliminate the effect of modelled prevalence - see Real et al. 2006).

If the variables to which you want to apply the model have a prefix or suffix (e.g. something like prefix = "raster.stack\$" for the R 'raster' or 'terra' package, or prefix = "mydata\$" for a data frame, or suffix = "@1" in QGIS, or suffix = "@mapset" in GRASS), you can get these in the equation too, using the prefix and/or the suffix argument.

#### Value

A charachter string of the model equation.

#### Author(s)

A. Marcia Barbosa

#### References

Barbosa A.M., Real R. & Vargas J.M. (2010) Use of coarse-resolution models of species' distributions to guide local conservation inferences. Conservation Biology 24: 1378-87

Real R., Barbosa A.M., Martinez-Solano I. & Garcia-Paris, M. (2005) Distinguishing the distributions of two cryptic frogs (Anura: Discoglossidae) using molecular data and environmental modeling. Canadian Journal of Zoology 83: 536-545

Real R., Barbosa A.M. & Vargas J.M. (2006) Obtaining environmental favourability functions from logistic regression. Environmental and Ecological Statistics 13: 237-245

## getThreshold

## Examples

```
# load sample models:
data(rotif.mods)
# choose a particular model to play with:
mod <- rotif.mods$models[[1]]
getModEqn(mod)
getModEqn(mod, type = "P", digits = 3, suffix = "@mapset")
getModEqn(mod, type = "F", digits = 2)
```

getThreshold Predic

## Prediction threshold for a given criterion

## Description

This function computes the prediction threshold under a given criterion.

## Usage

```
getThreshold(model = NULL, obs = NULL, pred = NULL, threshMethod,
interval = 0.01, quant = 0, na.rm = TRUE)
```

## Arguments

model	a binary-response model object of class "glm", "gam", "gbm", "randomForest" or "bart". If this argument is provided, 'obs' and 'pred' will be extracted with mod2obspred. Alternatively, you can input the 'obs' and 'pred' arguments instead of 'model'.
obs	alternatively to 'model' and together with 'pred', a numeric vector of observed presences (1) and absences (0) of a binary response variable. Alternatively (and if 'pred' is a 'SpatRaster'), a two-column matrix or data frame containing, re- spectively, the x (longitude) and y (latitude) coordinates of the presence points, in which case the 'obs' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
pred	alternatively to 'model' and together with 'obs', a vector with the correspond- ing predicted values of presence probability, habitat suitability, environmental favourability or alike. Must be of the same length and in the same order as 'obs'. Alternatively (and if 'obs' is a set of point coordinates), a 'SpatRaster' map of the predicted values for the entire evaluation region, in which case the 'pred' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
threshMethod	Criterion under which to compute the threshold. Run modEvAmethods("getThreshold") for available options.

interval	Argument to pass to optiThresh indicating the interval between the thresholds to test. The default is 0.01. Smaller values may provide more precise results but take longer to compute.
quant	Numeric value indicating the proportion of presences to discard if threshMethod="MTP" (minimum training presence). With the default value 0, MTP will be the threshold at which all observed presences are classified as such; with e.g. quant=0.05, MTP will be the threshold at which 5% presences will be classified as absences.
na.rm	Logical value indicating whether NA values should be ignored. Defaults to TRUE.

Several criteria have been proposed for selecting a threshold with which to convert continuous model predictions (of presence probability, habitat suitability or alike) into binary predictions of presence or absence. A threshold is required for computing threshold-based model evaluation metrics, such as those in threshMeasures. This function implements a few of these threshold selection criteria, including those outlined in Liu et al. (2005, 2013) and a couple more:

- "preval", "trainPrev": prevalence (proportion of presences) in the supplied 'model' or 'obs'
- "meanPred": mean predicted value in the supplied 'model' or 'pred'
- "midPoint": median predicted value in the supplied 'model' or 'pred'
- "maxKappa": threshold that maximizes Cohen's kappa

- "maxCCR", "maxOA", "maxOPS": threshold that maximizes the Correct Classification Rate, aka Overall Accuracy, aka Overall Prediction Success

- "maxF": threshold that maximizes the F value
- "maxSSS": threshold that maximizes the sum of sensitivity and specificity
- "maxTSS": threshold that maximizes the True Skill Statistic
- "maxSPR": threshold that maximizes the sum of precision and recall
- "minDSS": threshold that minimizes the difference between sensitivity and specificity
- "minDPR": threshold that minimizes the difference between precision and recall
- "minD01": threshold that minimizes the distance between the ROC curve and the 0,1 point
- "minD11": threshold that minimizes the distance between the PR curve and the 1,1 point
- "equalPrev": predicted and observed prevalence equalization

- "MTP": minimum training presence, or the lowest predicted value where presence is recorded in 'obs' or 'model'. Optionally, with the 'quant' argument, this threshold leaves out predicted values lower than the value for the lowest specified proportion of presences

#### Value

This function returns a numeric value indicating the threshold selected under the specified 'thresh-Method'.

#### Author(s)

A. Marcia Barbosa

## HLfit

## References

Liu C., Berry P.M., Dawson T.P. & Pearson R.G. (2005) Selecting thresholds of occurrence in the prediction of species distributions. Ecography 28: 385-393

Liu C., White M. & Newell G. (2013) Selecting thresholds for the prediction of species occurrence with presence-only data. Journal of Biogeography 40: 778-789

## See Also

threshMeasures, optiThresh

## Examples

```
# load sample models:
data(rotif.mods)
# choose a particular model to play with:
mod <- rotif.mods$models[[1]]
getThreshold(model = mod, threshMethod = "maxTSS")
# you can also use getThreshold with vectors of observed and predicted values
# instead of with a model object:
presabs <- mod$y
prediction <- mod$fitted.values
getThreshold(obs = presabs, pred = prediction, threshMethod = "maxTSS")
getThreshold(obs = presabs, pred = prediction, threshMethod = "MTP")
getThreshold(obs = presabs, pred = prediction, threshMethod = "MTP",
quant = 0.05)
# 'obs' can also be a table of presence point coordinates
```

```
# and 'pred' a SpatRaster of predicted values
```

HI	_fit	
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Hosmer-Lemeshow goodness of fit

#### Description

This function calculates a model's calibration performance (reliability) with the Hosmer & Lemeshow goodness-of-fit statistic, which compares predicted probability to observed occurrence frequency at each portion of the probability range.

## Usage

```
HLfit(model = NULL, obs = NULL, pred = NULL, bin.method,
n.bins = 10, fixed.bin.size = FALSE, min.bin.size = 15,
min.prob.interval = 0.1, quantile.type = 7, simplif = FALSE,
verbosity = 2, alpha = 0.05, plot = TRUE, plot.values = TRUE,
plot.bin.size = TRUE, xlab = "Predicted probability",
ylab = "Observed prevalence", na.rm = TRUE, rm.dup = FALSE, ...)
```

## Arguments

model	a binary-response model object of class "glm", "gam", "gbm", "randomForest" or "bart". If this argument is provided, 'obs' and 'pred' will be extracted with mod2obspred. Alternatively, you can input the 'obs' and 'pred' arguments instead of 'model'.	
obs	alternatively to 'model' and together with 'pred', a numeric vector of observed presences (1) and absences (0) of a binary response variable. Alternatively (and if 'pred' is a 'SpatRaster'), a two-column matrix or data frame containing, respectively, the x (longitude) and y (latitude) coordinates of the presence points, in which case the 'obs' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.	
pred	alternatively to 'model' and together with 'obs', a vector with the correspond- ing predicted values of presence probability, habitat suitability, environmental favourability or alike. Must be of the same length and in the same order as 'obs'. Alternatively (and if 'obs' is a set of point coordinates), a 'SpatRaster' map of the predicted values for the entire evaluation region, in which case the 'pred' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.	
bin.method	argument to pass to getBins specifying the method for grouping the records into bins within which to compare predicted probability to observed prevalence; type modEvAmethods("getBins") for available options, and see Details for more information.	
n.bins	argument to pass to getBins specifying the number of bins to use if bin.method = n.bins or bin.method = quantiles. The default is 10.	
fixed.bin.size	argument to pass to getBins, a logical value indicating whether to force bins to have (approximately) the same size. The default is FALSE.	
min.bin.size	argument to pass to getBins specifying the minimum number of records in each bin. The default is 15, the minimum required for accurate comparisons within bins (Jovani & Tella 2006, Jimenez-Valverde et al. 2013).	
min.prob.interval		
	argument to pass to getBins specifying the minimum interval (range) of probability values within each bin. The default is 0.1.	
quantile.type	argument to pass to quantile specifying the algorithm to use if bin.method = "quantiles". The default is 7 (the quantile default in R), but check out other types, e.g. 3 (used by SAS), 6 (used by Minitab and SPSS) or 5 (appropriate for deciles, which correspond to the default n.bins = 10).	

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simplif	logical, wheter to perform a faster simplified version returning only the basic statistics. The default is FALSE.
verbosity	integer specifying the amount of messages or warnings to display. Defaults to the maximum implemented; lower numbers (down to 0) decrease the number of messages.
alpha	alpha value for confidence intervals if plot = TRUE.
plot	logical, whether to produce a plot of the results. The default is TRUE.
plot.values	logical, whether to report measure values in the plot. The default is TRUE.
plot.bin.size	logical, whether to report bin sizes in the plot. The default is TRUE.
xlab	label for the x axis.
ylab	label for the y axis.
na.rm	Logical value indicating whether missing values should be ignored in computa- tions. Defaults to TRUE.
rm.dup	If TRUE and if 'pred' is a SpatRaster and if there are repeated points within the same pixel, a maximum of one point per pixel is used to compute the presences. See examples in ptsrast2obspred. The default is FALSE.
	further arguments to pass to the <b>plot</b> function.

Most of the commonly used measures for evaluating model performance focus on the discrimination or the classification capacity, i.e., how well the model is capable of distinguishing or classifying presences and absences (often after the model's continuous predictions of presence probability or alike are converted to binary predictions of presence or absence). However, there is another important facet of model evaluation: calibration or reliability, i.e., the relationship between predicted probability and observed occurrence frequency (Pearce & Ferrier 2000; Jimenez-Valverde et al. 2013). The HLfit function measures model reliability with the Hosmer & Lemeshow goodness-offit statistic (Hosmer & Lemeshow 1980).

Note that this statistic has strong limitations and caveats (see e.g. http://www.statisticalhorizons.com/hosmerlemeshow, Allison 2014), mainly due to the need to group the values into bins within which to compare probability and prevalence, and the strong influence of the binning method on the results. The 'HLfit' function can use several binning methods, which are implemented and roughly explained in the getBins function and can be accessed by typing 'modEvAmethods("getBins")'. You should try 'HLfit' with different binning methods to see how if the results are robust.

## Value

HLfit returns a list with the following components:

bins.table	a data frame of the obtained bins and the values resulting from the hosmer-	
	Lemeshow goodness-of-fit analysis.	
chi.sq	the value of the Chi-squared test.	
DF	the number of degrees of freedom.	
p.value	the p-value of the Hosmer-Lemeshow test. Note that this is one of those tests for which higher p-values are better.	
RMSE	the root mean squared error.	

#### Note

The 4 lines of code from "observed" to "p.value" were adapted from the 'hosmerlem' function available at http://www.stat.sc.edu/~hitchcock/diseaseoutbreakRexample704.txt. The plotting code was loosely based on the calibration.plot function in package **PresenceAbsence**. HLfit still needs some code simplification, and may fail for some datasets and binning methods. Fixes are being applied. Feedback is welcome.

## Author(s)

A. Marcia Barbosa

#### References

Allison P.D. (2014) Measures of Fit for Logistic Regression. SAS Global Forum, Paper 1485

Hosmer D.W. & Lemeshow S. (1980) A goodness-of-fit test for the multiple logistic regression model. Communications in Statistics, A10: 1043-1069

Jimenez-Valverde A., Acevedo P., Barbosa A.M., Lobo J.M. & Real R. (2013) Discrimination capacity in species distribution models depends on the representativeness of the environmental domain. Global Ecology and Biogeography 22: 508-516

Jovani R. & Tella J.L. (2006) Parasite prevalence and sample size: misconceptions and solutions. Trends in Parasitology 22: 214-218

Pearce J. & Ferrier S. (2000) Evaluating the Predictive Performance of Habitat Models Developed using Logistic Regression. Ecological Modeling, 133: 225-245

#### See Also

getBins, MillerCalib

#### Examples

```
# load sample models:
```

data(rotif.mods)

# choose a particular model to play with:

```
mod <- rotif.mods$models[[1]]</pre>
```

# try HLfit using different binning methods:

HLfit(model = mod, bin.method = "round.prob", main = "HL GOF with round.prob (n=10)")

HLfit(model = mod, bin.method = "prob.bins", main = "HL GOF with prob.bins (n=10)")

HLfit(model = mod, bin.method = "size.bins",

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#### inputMunch

```
main = "HL GOF with size.bins (min size=15)")
HLfit(model = mod, bin.method = "size.bins", min.bin.size = 30,
main = "HL GOF with size.bins min size 30")
HLfit(model = mod, bin.method = "n.bins",
main = "HL GOF with 10 bins")
HLfit(model = mod, bin.method = "n.bins", fixed.bin.size = TRUE,
main = "HL GOF with 10 bins of fixed size")
HLfit(model = mod, bin.method = "n.bins", n.bins = 20,
main = "HL GOF with 20 bins")
HLfit(model = mod, bin.method = "quantiles",
main = "HL GOF with quantile bins (n=10)")
HLfit(model = mod, bin.method = "quantiles", n.bins = 20,
main = "HL GOF with quantile bins (n=20)")
# you can also use 'predPlot' with vectors of observed and predicted values
# instead of a model object:
presabs <- mod$y</pre>
prediction <- mod$fitted.values</pre>
HLfit(obs = presabs, pred = prediction, bin.method = "round.prob")
# 'obs' can also be a table of presence point coordinates
# and 'pred' a SpatRaster of predicted values
```

inputMunch

Munch inputs into 'obs' and 'pred' vectors

#### Description

This function is used internally by many other functions in this package to check and extract the 'obs' and 'pred' vectors from the user inputs.

#### Usage

```
inputMunch(model = NULL, obs = NULL, pred = NULL, rm.dup = FALSE, na.rm = FALSE)
```

#### Arguments

model a binary-response model object of class "glm", "gam", "gbm", "randomForest" or "bart". If this argument is provided, 'obs' and 'pred' will be extracted with mod2obspred. Alternatively, you can input the 'obs' and 'pred' arguments (e.g. for external test data) instead of 'model'.

obs	alternatively to 'model' and together with 'pred', a numeric vector of observed presences (1) and absences (0) of a binary response variable. Alternatively (and if 'pred' is a 'SpatRaster'), a two-column matrix or data frame containing, respectively, the x (longitude) and y (latitude) coordinates of the presence points, in which case the 'obs' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
pred	alternatively to 'model' and together with 'obs', a vector with the correspond- ing predicted values of presence probability, habitat suitability, environmental favourability or alike. Must be of the same length and in the same order as 'obs'. Alternatively (and if 'obs' is a set of point coordinates), a 'SpatRaster' map of the predicted values for the entire evaluation region, in which case the 'pred' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
rm.dup	logical argument to be passed to ptsrast2obspred indicating whether repeated points within the same pixel should be removed. The default is FALSE.
na.rm	logical argument indicating whether to remove (with a warning saying how many) rows with NA in any of the resulting 'obs' or 'pred' values. The default is FALSE.

#### Value

This function returns a two-column data frame containing the 'obs' and 'pred' values, or an error message if inputs are not as required.

## Author(s)

A. Marcia Barbosa

MESS

Multivariate Environmental Similarity Surfaces based on a data frame

## Description

This function performs the MESS analysis of Elith et al. (2010) to determine the extent of the environmental differences between model training and model projection (extrapolation) data. It is applicable to variables in a matrix or data frame.

## Usage

MESS(V, P, id.col = NULL, verbosity = 2)

## Arguments

V a matrix or data frame containing the variables (one in each column) in the training dataset.

Ρ	a matrix or data frame containing the same variables in the area to which the model(s) will be projected. Variables (columns) must be in the same order as in V, and colnames(P) must exist.
id.col	optionally, the index number of a column containing the row identifiers in P. If provided, this column will be excluded from MESS calculations but included in the output.
verbosity	Integer number indicating the amount of messages to display while computing the results. The default is to display all messages. Set verbosity=0 for no messages.

When model predictions are projected into regions, times or spatial resolutions not analysed in the training data, it may be important to measure the similarity between the new environments and those in the training sample (Elith et al. 2010), as models are not so reliable when predicting outside their domain (Barbosa et al. 2009). The Multivariate Environmental Similarity Surfaces (MESS) analysis measures the similarity in the analysed variables between any given locality in the projection dataset and the localities in the reference (training) dataset (Elith et al. 2010).

MESS analysis is implemented in the MAXENT software (Phillips et al. 2006) and in the **dismo** R package, but there it requires input variables in raster format. This implies not only the use of complex spatial data structures, but also that the units of analysis are rectangular pixels, whereas we often need to model distribution data recorded on less regular units (e.g. provinces, river basins), or on equal-area cells that are not necessarily rectangular (e.g. UTM cells, equal-area hexagons or other geometric shapes). The MESS function computes this analysis for variables in a data frame, where localities (in rows) may be of any size or shape.

#### Value

The function returns a data frame with the same column names as P, plus a column named TOTAL, quantifying the similarity between each point in the projection dataset and those in the reference dataset. Negative values indicate localities that are environmentally dissimilar from the reference region. The last column, MoD, indicates which of the column names of P corresponds to the most dissimilar variable, i.e., the limiting factor or the variable that drives the MESS in that locality (Elith et al. 2010).

#### Note

Newer and apparently more complete methods for analysing environmental dissimilarities have been developed, such as extrapolation detection (ExDet; Mesgaran et al. 2014) and Mobility-Oriented Parity analysis (MOP; Owens et al. 2013).

#### Author(s)

Alberto Jimenez-Valverde, A. Marcia Barbosa

#### References

Barbosa A.M., Real R. & Vargas J.M. (2009) Transferability of environmental favourability models in geographic space: the case of the Iberian desman (Galemys pyrenaicus) in Portugal and Spain. Ecological Modelling 220: 747-754

Elith J., Kearney M. & Phillips S. (2010) The art of modelling range-shifting species. Methods in Ecology and Evolution 1: 330-342

Mesgaran M.B., Cousens R.D. & Webber B.L. (2014) Here be dragons: a tool for quantifying novelty due to covariate range and correlation change when projecting species distribution models. Diversity and Distributions, 20: 1147-1159

Owens H.L., Campbell L.P., Dornak L.L., Saupe E.E., Barve N., Soberon J., Ingenloff K., Lira-Noriega A., Hensz C.M., Myers C.E. & Peterson A.T. (2013) Constraints on interpretation of ecological niche models by limited environmental ranges on calibration areas. Ecological Modelling, 263: 10-18

Phillips S.J., Anderson R.P. & Schapire R.E. (2006) Maximum entropy modeling of species geographic distributions. Ecological Modelling 190: 231-259

## See Also

OA; mess in package **dismo**; ecospat.climan in package **ecospat**; kuenm\_mop and kuenm\_mmop in package **kuenm** 

#### Examples

```
## Not run:
# load package 'fuzzySim' and its sample data:
require(fuzzySim)
data(rotif.env)
```

```
# add a column specifying the hemisphere:
```

unique(rotif.env\$CONTINENT)

rotif.env\$HEMISPHERE <- "Eastern"</pre>

```
rotif.env$HEMISPHERE[rotif.env$CONTINENT %in%
c("NORTHERN_AMERICA", "SOUTHERN_AMERICA")] <- "Western"</pre>
```

```
head(rotif.env)
```

```
# perform a MESS analysis
# suppose you'll extrapolate models from the Western hemisphere (Americas)
# to the Eastern hemisphere (rest of the world):
names(rotif.env) # variables are in columns 5:17
west <- subset(rotif.env, HEMISPHERE == "Western", select = 5:17)
east <- subset(rotif.env, HEMISPHERE == "Eastern", select = 5:17)</pre>
```

## MillerCalib

```
east.with.ID <- subset(rotif.env, HEMISPHERE == "Eastern",
select = c(1, 5:17))
head(east)
head(east.with.ID) # ID is in column 1
mess <- MESS(V = west, P = east)
mess.with.ID <- MESS(V = west, P = east.with.ID, id.col = 1)
head(mess)
head(mess)
head(mess[, "TOTAL"])
## End(Not run)
```

MillerCalib

Miller's calibration satistics for logistic regression models

## Description

This function calculates Miller's (1991) calibration statistics for a generalized linear model with binomial distribution and logistic link, namely the intercept and slope of the regression of the response variable on the logit of predicted probabilities. Optionally and by default, it also plots the corresponding regression line over the reference diagonal.

#### Usage

```
MillerCalib(model = NULL, obs = NULL, pred = NULL, plot = TRUE,
line.col = "black", diag = TRUE, diag.col = "grey",
plot.values = TRUE, digits = 2, xlab = "", ylab = "",
main = "Miller calibration", na.rm = TRUE, rm.dup = FALSE, ...)
```

#### Arguments

model	a binary-response model object of class "glm", "gam", "gbm", "randomForest" or "bart". If this argument is provided, 'obs' and 'pred' will be extracted with mod2obspred. Alternatively, you can input the 'obs' and 'pred' arguments instead of 'model'.
obs	alternatively to 'model' and together with 'pred', a numeric vector of observed presences (1) and absences (0) of a binary response variable. Alternatively (and if 'pred' is a 'SpatRaster'), a two-column matrix or data frame containing, respectively, the x (longitude) and y (latitude) coordinates of the presence points, in which case the 'obs' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
pred	alternatively to 'model' and together with 'obs', a vector with the correspond- ing predicted values of presence probability, habitat suitability, environmental favourability or alike. Must be of the same length and in the same order as 'obs'.

Alternatively (and if 'obs' is a set of point coordinates), a 'SpatRaster' map of the predicted values for the entire evaluation region, in which case the 'pred' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
logical, whether or not to produce a plot of the Miller regression line. Defaults to TRUE.
colour for the Miller regression line (if plot = TRUE).
logical, whether or not to add the reference diagonal (if plot = TRUE). Defaults to TRUE.
line colour for the reference diagonal.
logical, whether or not to report the values of the intercept and slope on the plot. Defaults to TRUE.
integer number indicating the number of digits to which the values in the plot should be rounded. Dafaults to 2. This argument is ignored if 'plot' or 'plot.values' are set to FALSE.
label for the x axis.
label for the y axis.
title for the plot.
Logical value indicating whether missing values should be ignored in computa- tions. Defaults to TRUE.
If TRUE and if 'pred' is a SpatRaster and if there are repeated points within the same pixel, a maximum of one point per pixel is used to compute the presences. See examples in ptsrast2obspred. The default is FALSE.
additional arguments to pass to plot.

Calibration or reliability measures how a model's predicted probabilities relate to observed species prevalence or proportion of presences in the modelled data (Pearce & Ferrier 2000; Wintle et al. 2005; Franklin 2010). If predictions are perfectly calibrated, the slope will equal 1 and the intercept will equal 0, so the model's calibration line will perfectly overlap with the reference diagonal. Note that Miller's statistics assess the model globally: a model is well calibrated if the average of all predicted probabilities equals the proportion of presences in the modelled data. Good calibration is always attained on the same data used for building the model (Miller 1991); Miller's calibration statistics are mainly useful when extrapolating a model outside those training data.

## Value

This function returns a list of two integer values:

intercept	the calibration intercept.
slope	the calibration slope.

If plot = TRUE, a plot will be produced with the model calibration line, optionally (if diag = TRUE) over the reference diagonal, and optionally (if plot.values = TRUE) with the intercept and slope values printed on it.

#### mod2obspred

## Author(s)

A. Marcia Barbosa

#### References

Franklin, J. (2010) Mapping Species Distributions: Spatial Inference and Prediction. Cambridge University Press, Cambridge.

Miller M.E., Hui S.L. & Tierney W.M. (1991) Validation techniques for logistic regression models. Statistics in Medicine, 10: 1213-1226

Pearce J. & Ferrier S. (2000) Evaluating the predictive performance of habitat models developed using logistic regression. Ecological Modelling, 133: 225-245

Wintle B.A., Elith J. & Potts J.M. (2005) Fauna habitat modelling and mapping: A review and case study in the Lower Hunter Central Coast region of NSW. Austral Ecology, 30: 719-738

## See Also

HLfit, Dsquared, RsqGLM

#### Examples

```
# load sample models:
data(rotif.mods)
# choose a particular model to play with:
mod <- rotif.mods$models[[1]]
MillerCalib(model = mod)
MillerCalib(model = mod, plot.values = FALSE)
MillerCalib(model = mod, main = "Model calibration line")
# you can also use MillerCalib with vectors of observed and predicted values
# instead of a model object:
MillerCalib(obs = mod$y, pred = mod$fitted.values)
# 'obs' can also be a table of presence point coordinates
# and 'pred' a SpatRaster of predicted values
```

mod2obspred

Extract observed and predicted values from a model object.

#### Description

This function takes a model object and returns the observed and (optionally) the fitted values in that model.

## Usage

mod2obspred(model, obs.only = FALSE)

## Arguments

model	a model object of class "glm", "gam", "gbm", "randomForest" or "bart" from
	which the response variable and fitted (predicted) values can be extracted. Note
	that, for "randomForest" models, only the out-of-bag prediction is available from
	the model object (see ?predict.randomForest if you have that package in-
	stalled), so here you'll get different results if you provide 'model' or the mod-
	elled 'obs' (and corresponding 'pred') values.
obs.only	logical value indicating whether only 'obs' should be obtained (saves computing time when 'pred' not needed – used e.g. by prevalence). Defaults to FALSE.

#### Value

A data frame with one column containing the observed and (if obs.only=FALSE, the default) another column containing the predicted values from 'model'.

#### Author(s)

A. Marcia Barbosa

#### See Also

prevalence

## Examples

```
data(rotif.mods)
mod <- rotif.mods$models[[1]]
obspred <- mod2obspred(mod)
head(obspred)</pre>
```

modEvAmethods Methods implemented in modEvA functions

## Description

This function allows retrieving the methods available for some of the functions in modEvA, such as threshMeasures, optiThresh, multModEv and getBins.

#### Usage

modEvAmethods(fun)

## multModEv

#### Arguments

fun a character vector of length 1 specifying the name (in quotes) of the function for which to obtain the available methods. Must be one of "threshMeasures", "optiThresh", "multModEv", "getThreshold" or "getBins".

#### Value

a character vector of the available methods for the specified function.

#### Author(s)

A. Marcia Barbosa

# See Also

threshMeasures, optiThresh, getBins, multModEv

## Examples

modEvAmethods("threshMeasures")

modEvAmethods("multModEv")

modEvAmethods("optiThresh")

modEvAmethods("getBins")

multModEv

Multiple model evaluation

#### Description

If you have a list of GLM model objects (created, e.g., with the multGLM function of the 'fuzzySim' R-Forge package), or a data frame with presence-absence data and the corresponding predicted values for a set of species, you can use the multModEv function to get a set of evaluation measures for all models simultaneously, as long as they all have the same sample size.

## Usage

```
multModEv(models = NULL, obs.data = NULL, pred.data = NULL,
measures = modEvAmethods("multModEv"), standardize = FALSE,
thresh = NULL, bin.method = NULL, verbosity = 0, ...)
```

# Arguments

models	a list of model object(s) of class "glm", all applied to the same data set. Evalua- tion is based on the cases included in the models.
obs.data	a data frame with observed (training or test) binary data. This argument is ignored if 'models' is provided.
pred.data	a data frame with the corresponding predicted (training or test) values, with both rows and columns in the same order as in 'obs.data'. This argument is ignored if 'models' is provided. Note that, for calibration measures (based on HLfit or MillerCalib), the results are only valid if the input predictions represent probability.
measures	character vector of the evaluation measures to calculate. The default is all imple- mented measures, which you can check by typing 'modEvAmethods("multModEv")'. But beware: calibration measures (i.e., HL and Miller) are only valid if your predicted values reflect actual presence probability (not favourability, habitat suitability or others); you should exclude them otherwise.
standardize	logical, whether to standardize measures that vary between -1 and 1 to the 0-1 scale (see standard01). The default is FALSE.
thresh	argument to pass to threshMeasures if any of 'measures' is calculated by that function. The default is NULL, but a valid method must be specified if any of 'measures' is threshold-based - i.e., any of those in 'modEvAmethods("threshMeasures")'.
bin.method	the method with which to divide the data into groups or bins, for calibration or reliability measures such as HLfit. The default is NULL, but a valid method must be specified if 'measures' includes "HL" or "HL.p". Type modEvAmethods("getBins") for available options), and see HLfit and getBins for more information.
verbosity	integer specifying the amount of messages or warnings to display. Defaults to 0, but can also be 1 or 2 for more messages from the functions within.
	optional arguments to pass to HLfit (if "HL" or "HL.p" are included in 'mea- sures'), namely n.bins, fixed.bin.size, min.bin.size, min.prob.interval or quan- tile.type.

# Value

A data frame with the value of each evaluation measure for each model.

# Author(s)

A. Marcia Barbosa

# See Also

threshMeasures

# OA

## Examples

```
data(rotif.mods)
eval1 <- multModEv(models = rotif.mods$models[1:6], thresh = 0.5,</pre>
bin.method = "n.bins", fixed.bin.size = TRUE)
head(eval1)
eval2 <- multModEv(models = rotif.mods$models[1:6],</pre>
thresh = "preval", measures = c("AUC", "AUCPR", "CCR",
"Sensitivity", "TSS"))
head(eval2)
# you can also calculate evaluation measures for a set of
# observed vs predicted data, rather than from model objects:
obses <- sapply(rotif.mods$models, `[[`, "y")</pre>
preds <- sapply(rotif.mods$models, `[[`, "fitted.values")</pre>
eval3 <- multModEv(obs.data = obses[ , 1:4],</pre>
pred.data = preds[ , 1:4], thresh = "preval",
bin.method = "prob.bins")
head(eval3)
```

0A

**Overlap Analysis** 

## Description

This function analyses the range of values of the given environmental variables at the sites where a species has been recorded present.

## Usage

OA(data, sp.cols, var.cols)

data	a data frame with your species' occurrence data and the predictor variables.
sp.cols	index number of the column containing the occurrence data of the species to be modelled. Currently only one species can be analysed at a time.
var.cols	index numbers of the columns containing the predictor variables to be used.

## Details

Overlap Analysis is one of the simplest forms of modelling species' distributions. It assesses the ranges of values of the given environmental variables at the sites where a species has been recorded present, and predicts where that species should be able to occur based on those presence data (e.g. Brito et al. 1999, Arntzen & Teixeira 2006).

OA can also be useful when extrapolating models outside their original scope (geographical area, time period or spatial resolution), as it can identify which localities are within the model's domain - i.e., within the analysed ranges of values of the variables, outside which the model may not be reliable (e.g. Barbosa et al. 2009). In this case, the response is not a species' presence, but rather the sites that have been included in the model. See also the MESS function for a comparison between modelled and extrapolation environments.

Input data for the OA function are a vector or column with ones and zeros (presences vs. absences of a species if we want to model its occurrence, or modelled vs. non-modelled sites if we want to know which non-modelled sites are within the modelled range), and a matrix or data frame with the corresponding values of the environmental variables to consider (one variable in each column, values in rows).

#### Value

A binary vector whith 1 where the values of all predictors lie within the ranges observed for the presence records, and 0 otherwise.

#### Author(s)

A. Marcia Barbosa

#### References

Arntzen J.W, Teixeira J. (2006) History and new developments in the mapping and modelling of the distribution of the golden-striped salamander, Chioglossa lusitanica. Zeitschrift fur Feldherpetologie, Supplement: 1-14.

Barbosa, A.M., Real, R. & Vargas, J.M. (2009) Transferability of environmental favourability models in geographic space: the case of the Iberian desman (Galemys pyrenaicus) in Portugal and Spain. Ecological Modelling 220: 747-754.

Brito J.C., Crespo E.G., Paulo O.S. (1999) Modelling wildlife distributions: Logistic Multiple Regression vs Overlap Analysis. Ecography 22: 251-260.

#### See Also

MESS

# Examples

```
## Not run:
# load package 'fuzzySim' and its sample data:
require(fuzzySim)
data(rotif.env)
```

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## optiPair

names(rotif.env)
OA(rotif.env, sp.cols = 18, var.cols = 5:17)

## End(Not run)

optiPair

*Optimize the classification threshold for a pair of related model evaluation measures.* 

## Description

This function can optimize a model's classification threshold based on a pair of model evaluation measures that balance each other, such as sensitivity-specificity, precision-recall (i.e., positive predictive power vs. sensitivity), or omission-commission, or underprediction-overprediction (Fielding & Bell 1997; Liu et al. 2011; Barbosa et al. 2013). The function plots both measures of the given pair against all thresholds with a given interval, and calculates the optimal sum, difference and mean of the two measures.

#### Usage

```
optiPair(model = NULL, obs = NULL, pred = NULL,
measures = c("Sensitivity", "Specificity"), interval = 0.01,
plot = TRUE, plot.sum = FALSE, plot.diff = FALSE, ylim = NULL,
na.rm = TRUE, exclude.zeros = TRUE, rm.dup = FALSE, ...)
```

model	a binary-response model object of class "glm", "gam", "gbm", "randomForest" or "bart". If this argument is provided, 'obs' and 'pred' will be extracted with mod2obspred. Alternatively, you can input the 'obs' and 'pred' arguments instead of 'model'.
obs	alternatively to 'model' and together with 'pred', a numeric vector of observed presences (1) and absences (0) of a binary response variable. Alternatively (and if 'pred' is a 'SpatRaster'), a two-column matrix or data frame containing, respectively, the x (longitude) and y (latitude) coordinates of the presence points, in which case the 'obs' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
pred	alternatively to 'model' and together with 'obs', a vector with the correspond- ing predicted values of presence probability, habitat suitability, environmental favourability or alike. Must be of the same length and in the same order as 'obs'. Alternatively (and if 'obs' is a set of point coordinates), a 'SpatRaster' map of the predicted values for the entire evaluation region, in which case the 'pred' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.

measures	a character vector of length 2 indicating the pair of measures whose curves to plot and whose combined threshold to optimize. Available measures can be obtained with 'modEvAmethods("threshMeasures")', but note that this function expects you to use two measures that counter-balance one another, such as c("Sensitivity", "Specificity") [the default], c("Omission", "Commission"), or c("Precision", "Recall").
interval	the interval of thresholds at which to calculate the measures. The default is $0.01. \label{eq:calculate}$
plot	logical indicating whether or not to plot the pair of measures.
plot.sum	logical, whether to plot the sum (+) of both measures in the pair. Defaults to FALSE.
plot.diff	logical, whether to plot the difference (-) between both measures in the pair. Defaults to FALSE.
ylim	a character vector of length 2 indicating the lower and upper limits for the y axis. The default is NULL for an automatic definition of 'ylim' based on the values of the measures and their sum and/or difference if any of these are set to TRUE.
na.rm	logical, whether NA values should be removed from the calculation of mini- mum/maximum/mean values to get the optimized measures. Defaults to TRUE.
exclude.zeros	logical, whether non-finite and zero values should be removed from the calculation of minimum/maximum/mean values to get the optimized measures. Defaults to TRUE.
rm.dup	If TRUE and if 'pred' is a SpatRaster and if there are repeated points within the same pixel, a maximum of one point per pixel is used to compute the presences. See examples in ptsrast2obspred. The default is FALSE.
	additional arguments to be passed to the plot function.

# Value

The output is a list with the following components:

measures.values		
	a data frame with the values of the chosen pair of measures, as well as their difference, sum and mean, at each threshold.	
MinDiff	numeric value, the minimum difference between both measures.	
ThreshDiff	numeric value, the threshold that minimizes the difference between both measures.	
MaxSum	numeric value, the maximum sum of both measures.	
ThreshSum	numeric value, the threshold that maximizes the sum of both measures.	
MaxMean	numeric value, the maximum mean of both measures.	
ThreshMean	numeric value, the threshold that maximizes the mean of both measures.	

If plot=TRUE (the default), a plot is also produced with the value of each of 'measures' at each threshold, and horizontal and vertical lines marking, respectively, the threshold and value at which the difference between the two 'measures' is minimal.

## optiPair

## Author(s)

A. Marcia Barbosa

#### References

Barbosa, A.M., Real, R., Munoz, A.-R. & Brown, J.A. (2013) New measures for assessing model equilibrium and prediction mismatch in species distribution models. Diversity and Distributions 19: 1333-1338

Fielding A.H. & Bell J.F. (1997) A review of methods for the assessment of prediction errors in conservation presence/absence models. Environmental Conservation 24: 38-49

Liu C., White M., & Newell G. (2011) Measuring and comparing the accuracy of species distribution models with presence-absence data. Ecography, 34, 232-243.

## See Also

optiThresh, threshMeasures

## Examples

```
# load sample models:
data(rotif.mods)
```

```
# choose a particular model to play with:
mod <- rotif.mods$models[[1]]</pre>
```

```
optiPair(model = mod)
```

optiPair(model = mod, measures = c("Precision", "Recall"))

optiPair(model = mod, measures = c("UPR", "OPR"))

optiPair(model = mod, measures = c("CCR", "F1score"))

```
# you can also use 'optiPair' with vectors of observed
# and predicted values, instead of a model object:
```

```
optiPair(obs = mod$y, pred = mod$fitted.values)
```

# 'obs' can also be a table of presence point coordinates
# and 'pred' a SpatRaster of predicted values

```
optiThresh
```

#### Description

The 'optiThresh' function calculates optimal thresholds for a number of model evaluation measures (see threshMeasures). Optimization is given for each measure, and/or for all measures according to particular criteria (e.g. Jimenez-Valverde & Lobo 2007; Liu et al. 2005; Nenzen & Araujo 2011). Results are given numerically and in plots.

#### Usage

```
optiThresh(model = NULL, obs = NULL, pred = NULL, interval = 0.01,
measures = modEvAmethods("threshMeasures"),
optimize = modEvAmethods("optiThresh"), simplif = FALSE, plot = TRUE,
sep.plots = FALSE, xlab = "Threshold", na.rm = TRUE, rm.dup = FALSE, ...)
```

model	a binary-response model object of class "glm", "gam", "gbm", "randomForest" or "bart". If this argument is provided, 'obs' and 'pred' will be extracted with mod2obspred. Alternatively, you can input the 'obs' and 'pred' arguments instead of 'model'.
obs	alternatively to 'model' and together with 'pred', a numeric vector of observed presences (1) and absences (0) of a binary response variable. Alternatively (and if 'pred' is a 'SpatRaster'), a two-column matrix or data frame containing, respectively, the x (longitude) and y (latitude) coordinates of the presence points, in which case the 'obs' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
pred	alternatively to 'model' and together with 'obs', a vector with the correspond- ing predicted values of presence probability, habitat suitability, environmental favourability or alike. Must be of the same length and in the same order as 'obs'. Alternatively (and if 'obs' is a set of point coordinates), a 'SpatRaster' map of the predicted values for the entire evaluation region, in which case the 'pred' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
interval	numeric value between 0 and 1 indicating the interval between the thresholds at which to calculate the evaluation measures. Defaults to 0.01.
measures	character vector indicating the names of the model evaluation measures for which to calculate optimal thresholds. The default is using all measures available in 'modEvAmethods("threshMeasures")'.
optimize	character vector indicating the threshold optimization criteria to use; "each" cal- culates the optimal threshold for each model evaluation measure, while the re- maining options optimize all measures according to the specified criterion. The default is using all criteria available in 'modEvAmethods("optiThresh")'.

## optiThresh

simplif	logical, whether to calculate a faster simplified version. Used internally in other functions.
plot	logical, whether to plot the values of each evaluation measure at all thresholds.
sep.plots	logical. If TRUE, each plot is presented separately (you need to be recording R plot history to be able to browse through them all); if FALSE(the default), all plots are presented together in the same plotting window.
xlab	character vector indicating the label of the x axis.
na.rm	Logical value indicating whether missing values should be ignored in computa- tions. Defaults to TRUE.
rm.dup	If TRUE and if 'pred' is a SpatRaster and if there are repeated points within the same pixel, a maximum of one point per pixel is used to compute the presences. See examples in ptsrast2obspred. The default is FALSE.
	additional arguments to pass to plot.

## Value

This function returns a list with the following components:

all.thresholds	a data frame with the values of all analysed measures at all analysed thresholds.
optimals.each	if "each" is among the threshold criteria specified in 'optimize', optimals.each is output as a data frame with the value of each measure at its optimal threshold, as well as the type of optimal for that measure (which may be the maximum for measures of goodness such as "Sensitivity", or the minimum for measures of badness such as "Omission").
optimals.criter	ia
	a data frame with the values of measure at the threshold that maximizes each of the criteria specified in 'optimize' (except for "each", see above).

## Note

"Sensitivity" is the same as "Recall", and "PPP" (positive predictive power) is the same as "Precision". "F1score"" is the harmonic mean of precision and recall.

# Note

Some measures cannot be calculated for thresholds at which there are zeros in the confusion matrix, hence the eventual 'NaN' or 'Inf' in results. Also, optimization may be deceiving for some measures; use 'plot = TRUE' and inspect the plot(s).

# Author(s)

A. Marcia Barbosa

## References

Jimenez-Valverde A. & Lobo J.M. (2007) Threshold criteria for conversion of probability of species presence to either-or presence-absence. Acta Oecologica 31: 361-369.

Liu C., Berry P.M., Dawson T.P. & Pearson R.G. (2005) Selecting thresholds of occurrence in the prediction of species distributions. Ecography 28: 385-393.

Nenzen H.K. & Araujo M.B. (2011) Choice of threshold alters projections of species range shifts under climate change. Ecological Modelling 222: 3346-3354.

#### See Also

```
threshMeasures, optiPair
```

#### Examples

```
# load sample models:
data(rotif.mods)
# choose a particular model to play with:
mod <- rotif.mods$models[[1]]</pre>
## Not run:
optiThresh(model = mod)
## End(Not run)
# change some of the parameters:
optiThresh(model = mod, pch = 20,
measures = c("CCR", "Sensitivity", "kappa", "TSS"), ylim = c(0, 1))
# you can also use optiThresh with vectors of observed and predicted
# values instead of with a model object:
## Not run:
optiThresh(obs = mod$y, pred = mod$fitted.values, pch = 20)
## End(Not run)
# 'obs' can also be a table of presence point coordinates
# and 'pred' a SpatRaster of predicted values
```

Plot a generalized linear model

## plotGLM

# Description

This function plots the observed (presence/absence) data and the predicted (probability) values of a Generalized Linear Model against the y regression equation (logit) values. Only logistic regression (binomial response, logit link) is currently implemented.

## Usage

```
plotGLM(model = NULL, obs = NULL, pred = NULL, link = "logit",
plot.values = TRUE, plot.digits = 3, xlab = "Logit (Y)",
ylab = "Predicted probability", main = "Model plot", na.rm = TRUE,
rm.dup = FALSE, ...)
```

model	a binary-response model object of class "glm". If this argument is provided, 'obs' and 'pred' will be extracted with mod2obspred. Alternatively, you can input the 'obs' and 'pred' arguments instead of 'model'.
obs	alternatively to 'model' and together with 'pred', a numeric vector of observed presences (1) and absences (0) of a binary response variable. Alternatively (and if 'pred' is a 'SpatRaster'), a two-column matrix or data frame containing, respectively, the x (longitude) and y (latitude) coordinates of the presence points, in which case the 'obs' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
pred	alternatively to 'model' and together with 'obs', a vector with the correspond- ing predicted values of presence probability, habitat suitability, environmental favourability or alike. Must be of the same length and in the same order as 'obs'. Alternatively (and if 'obs' is a set of point coordinates), a 'SpatRaster' map of the predicted values for the entire evaluation region, in which case the 'pred' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
link	the link function of the GLM; only 'logit' (the default) is implemented.
plot.values	logical, whether to include in the plot diagnostic values such as explained de- viance (calculated with the Dsquared function) and pseudo-R-squared measures (calculated with the RsqGLM function). Defaults to TRUE.
plot.digits	integer number indicating the number of digits to which the values in the plot should be rounded (if 'plot.values = TRUE'). Defaults to 3.
xlab	character string specifying the label for the x axis.
ylab	character string specifying the label for the y axis.
main	character string specifying the title for the plot.
na.rm	Logical value indicating whether missing values should be ignored in computations. Defaults to TRUE.
rm.dup	If TRUE and if 'pred' is a SpatRaster and if there are repeated points within the same pixel, a maximum of one point per pixel is used to compute the presences. See examples in ptsrast2obspred. The default is FALSE.
	additional arguments to pass to plot.

This function outputs a plot of model predictions against observations.

#### Author(s)

A. Marcia Barbosa

# References

Guisan A. & Zimmermann N.E. (2000) Predictive habitat distribution models in ecology. Ecological Modelling 135: 147-186

Weisberg S. (1980) Applied Linear Regression. Wiley, New York

## See Also

predPlot, predDensity

#### Examples

```
# load sample models:
data(rotif.mods)
# choose a particular model to play with:
mod <- rotif.mods$models[[1]]
plotGLM(model = mod)
plotGLM(model = mod, plot.values = FALSE)
# you can also use 'plotGLM' with vectors of observed and
# predicted values instead of with a model object:
plotGLM(obs = mod$y, pred = mod$fitted.values)
# 'obs' can also be a table of presence point coordinates
# and 'pred' a SpatRaster of predicted values
```

predDensity

Plot the density of predicted values for presences and absences.

#### Description

This function produces a histogram and/or a kernel density plot of predicted values for a binomial GLM, by default separately for the observed presences and absences, given a model object or a vector of predicted values and (optionally) a vector of the corresponding observed values.

## predDensity

## Usage

```
predDensity(model = NULL, obs = NULL, pred = NULL, separate = TRUE,
type = c("both"), legend.pos = "topright", main = "Density of predicted values",
na.rm = TRUE, rm.dup = FALSE)
```

# Arguments

model	a binary-response model object of class "glm", "gam", "gbm", "randomForest" or "bart". If this argument is provided, 'obs' and 'pred' will be extracted with mod2obspred. Alternatively, you can input the 'obs' and 'pred' arguments instead of 'model'.
obs	alternatively to 'model' and together with 'pred', a numeric vector of observed presences (1) and absences (0) of a binary response variable. Alternatively (and if 'pred' is a 'SpatRaster'), a two-column matrix or data frame containing, respectively, the x (longitude) and y (latitude) coordinates of the presence points, in which case the 'obs' vector will be extracted with ptsrast2obspred. This argument may be omitted (to show the density plot of all 'pred' values combined), and it is ignored if 'model' is provided.
pred	alternatively to 'model' (and optionally together with 'obs'), a vector with the corresponding predicted values of presence probability, habitat suitability, environmental favourability or alike. Must be of the same length and in the same order as 'obs' (if the latter is provided). Alternatively (and if 'obs' is a set of point coordinates), a 'SpatRaster' map of the predicted values for the entire evaluation region, in which case the 'pred' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
separate	logical value indicating whether prediction densities should be computed sepa- rately for observed presences (ones) and absences (zeros). Defaults to TRUE, but is necessarily changed to FALSE if either 'model' or 'obs' are not provided.
type	character vector specifying whether to produce a "histogram", a "density" plot, or "both" (the default). Partial argument matching is used.
legend.pos	character specifying the position for the legend; NA or "n" for no legend. Posi- tion can be "topright" (the default), "topleft, "bottomright"", "bottomleft", "top", "bottom", "left", "right", or "center". Partial argument matching is used.
main	main title for the plot.
na.rm	Logical value indicating whether missing values should be ignored in computa- tions. Defaults to TRUE.
rm.dup	If TRUE and if 'pred' is a SpatRaster and if there are repeated points within the same pixel, a maximum of one point per pixel is used to compute the presences. See examples in ptsrast2obspred. The default is FALSE.

# Details

For more details, please refer to the documentation of the functions mentioned under "See Also".

## Value

This function outputs and plots the object(s) specified in 'type' – by default, a density object and a histogram.

## Author(s)

A. Marcia Barbosa

#### See Also

hist, density, predPlot

## Examples

```
# load sample models:
data(rotif.mods)
# choose a particular model to play with:
mod <- rotif.mods$models[[1]]
predDensity(model = mod)
predDensity(model = mod, type = "histogram")
predDensity(model = mod, type = "density")
# you can also use 'predDensity' with vectors of
# observed and predicted values, instead of a model object:
presabs <- mod$y
prediction <- mod$fitted.values
predDensity(obs = presabs, pred = prediction)
predDensity(pred = prediction)
# 'obs' can also be a table of presence point coordinates
# and 'pred' a SpatRaster of predicted values
```

```
predPlot
```

Plot predicted values for presences and absences, classified according to a prediction threshold.

## Description

This function plots predicted values separated into observed presences and absences and coloured according to whether they are above or below a given prediction threshold. The plot imitates (with permission from the author) one of the graphical outputs of the 'summary' of models built with

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## predPlot

the **embarcadero** package (Carlson, 2020), but it can be applied to any 'glm' object or any set of observed and predicted values, and it allows specifying a user-defined threshold.

## Usage

```
predPlot(model = NULL, obs = NULL, pred = NULL, thresh = "preval",
main = "Classified predicted values", legend.pos = "n", pch = 1, cex = 0.5,
col = c("black", "grey"), na.rm = TRUE, rm.dup = FALSE, interval = 0.01,
quant = 0)
```

model	a binary-response model object of class "glm", "gam", "gbm", "randomForest" or "bart". If this argument is provided, 'obs' and 'pred' will be extracted with mod2obspred. Alternatively, you can input the 'obs' and 'pred' arguments instead of 'model'.
obs	alternatively to 'model' and together with 'pred', a numeric vector of observed presences (1) and absences (0) of a binary response variable. Alternatively (and if 'pred' is a 'SpatRaster'), a two-column matrix or data frame containing, respectively, the x (longitude) and y (latitude) coordinates of the presence points, in which case the 'obs' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
pred	alternatively to 'model' and together with 'obs', a vector with the correspond- ing predicted values of presence probability, habitat suitability, environmental favourability or alike. Must be of the same length and in the same order as 'obs'. Alternatively (and if 'obs' is a set of point coordinates), a 'SpatRaster' map of the predicted values for the entire evaluation region, in which case the 'pred' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
thresh	threshold value to separate predicted presences from predicted absences in 'pred'; can be "preval" (the default), to use the prevalence (i.e. proportion of presences) in 'obs', or any real number between 0 and 1. This value will be used to draw a vertical line on the plot and to colour the points (predicted values) according to whether they fall below or above the threshold. Run modEvAmethods("getThreshold") for available options, and see Details in getThreshold for their description.
main	Main title for the plot.
legend.pos	character value specifying the position for the legend on the plot. Can be "bot- tomleft", "bottom", "bottomright", "topleft", "left", "top", "topright", "right", "center", or NA or "n" for no legend (the default). Partial argument matching is used.
pch	plotting character for the presences and absences (see par).
cex	relative size of the plotting character (see par).
col	vector of length 2 indicating the colours with which to plot predicted presences and absences (points above and below the threshold), respectively.
na.rm	Logical value indicating whether missing values should be ignored in computa- tions. Defaults to TRUE.

rm.dup	If TRUE and if 'pred' is a SpatRaster and if there are repeated points within the same pixel, a maximum of one point per pixel is used to compute the presences. See examples in ptsrast2obspred. The default is FALSE.
interval	Argument to pass to optiThresh indicating the interval between the thresholds to test, if 'thresh' implies optimizing a threshold-based measure. The default is 0.01. Smaller values may provide more precise results but take longer to compute.
quant	Numeric value indicating the proportion of presences to discard if thresh="MTP" (minimum training presence). With the default value 0, MTP will be the threshold at which all observed presences are classified as such; with e.g. quant=0.05, MTP will be the threshold at which 5% presences will be classified as absences.

## Value

This function outputs a plot as per 'Description'.

#### Note

Points are jittered randomly along the y axis to minimize visual overlap. So, each run of 'pred-Plot' (unless you use set.seed first) will produce a different arrangement of points for the same data, although their x-axis values are faithful.

#### Author(s)

A. Marcia Barbosa

# References

Carlson C.J. (2020) embarcadero: Species distribution modelling with Bayesian additive regression trees in R. Methods in Ecology and Evolution, 11: 850-858.

#### See Also

predDensity, plotGLM

## Examples

```
# load sample models:
data(rotif.mods)
# choose a particular model to play with:
mod <- rotif.mods$models[[1]]
predPlot(model = mod)
predPlot(model = mod, thresh = 0.5)
```

# you can first select a threshold optimized according to a particular metric:

#### prevalence

```
## Not run:
threshold <- optiThresh(mod, measures = "TSS", optimize = "each")
threshold <- threshold$optimals.each[, "threshold"]
threshold
predPlot(model = mod, thresh = threshold)
## End(Not run)
# you can also use 'predPlot' with vectors of observed and predicted values
# instead of a model object:
presabs <- mod$y
prediction <- mod$fitted.values
predPlot(obs = presabs, pred = prediction)
predPlot(obs = presabs, pred = prediction, thresh = 0.5)
# 'obs' can also be a table of presence point coordinates
# and 'pred' a SpatRaster of predicted values
```

prevalence

Prevalence

## Description

For building and evaluating species distribution models, the porportion of presences of the species may be an issue to take into account (e.g. Jimenez-Valverde & Lobo 2006, Barbosa et al. 2013). The prevalence function calculates this measure.

#### Usage

prevalence(obs, model = NULL, event = 1, na.rm = TRUE)

obs	a vector or a factor of binary observations (e.g. 1 vs. 0, male vs. female, disease vs. no disease, etc.). This argument is ignored if 'model' is provided.
model	alternatively to 'obs', a binary-response model object of class "glm", "gam", "gbm", "randomForest" or "bart". If this argument is provided, 'obs' will be extracted with mod2obspred.
event	the value whose prevalence we want to calculate (e.g. 1, "present", etc.). This argument is ignored if 'model' is provided.
na.rm	logical, whether NA values should be excluded from the calculation. The default is TRUE.

Numeric value of the prevalence of event in the obs vector.

#### Author(s)

A. Marcia Barbosa

## References

Barbosa A.M., Real R., Munoz A.R. & Brown J.A. (2013) New measures for assessing model equilibrium and prediction mismatch in species distribution models. Diversity and Distributions, in press

Jimenez-Valverde A. & Lobo J.M. (2006) The ghost of unbalanced species distribution data in geographical model predictions. Diversity and Distributions, 12: 521-524.

#### See Also

evenness

## Examples

# calculate prevalence from binary vectors:

```
(x <- rep(c(0, 1), each = 5))
```

```
(y <- c(rep(0, 3), rep(1, 7)))
```

(z <- c(rep(0, 7), rep(1, 3)))

prevalence(x)

prevalence(y)

prevalence(z)

(w <- c(rep("yes", 3), rep("nope", 7)))</pre>

```
prevalence(w, event = "yes")
```

# calculate prevalence from a model object:

data(rotif.mods)

prevalence(mod = rotif.mods\$models[[1]])

## Description

This function takes presence points or coordinates and a raster map of model predictions, and it returns a data frame with two columns containing, respectively, the observed (presence or no presence) and the predicted value for each pixel. Duplicate points (i.e., points falling in the same pixel, whether or not they have the exact same coordinates) can be kept or removed.

#### Usage

```
ptsrast2obspred(pts, rst, rm.dup = FALSE, na.rm = FALSE, verbosity = 2)
```

#### Arguments

pts	a 'SpatVector' map of the presence points, or a two-column matrix or data frame containing their x (longitude) and y (latitude) coordinates, respectively.
rst	a one-layer 'SpatRaster' map of the model predictions, in the same CRS as 'pts'. If you have a raster map in another format, you can try to convert it with 'terra::rast()'
rm.dup	logical, whether repeated points within the same pixel should be removed. See Examples. The default is FALSE.
na.rm	logical, whether presence points with missing or non-finite values of 'rst' should be excluded from the output. The default is FALSE.
verbosity	integer value indicating the amount of messages to display. Defaults to 2, for the maximum amount of messages.

## Value

This function outputs a data frame with one column containing the observed (1 for presence, 0 for absence) and another column containing the corresponding predicted values from 'rst'.

## Author(s)

A. Marcia Barbosa

# Examples

```
## Not run:
# you can run these examples if you have the 'terra' package installed
require(terra)
# get an example raster map:
rst <- terra::rast(system.file("ex/elev.tif", package = "terra"))
rst <- terra::aggregate(rst, 10)</pre>
```

```
plot(rst)
```

```
# generate some random presence points within it:
set.seed(8)
presences <- terra::spatSample(as.polygons(ext(rst)), 10)</pre>
plot(presences, add = TRUE)
# use 'ptsrast2obspred' on this points + raster data:
# without removing duplicates (the default):
obspred <- ptsrast2obspred(pts = crds(presences), rst = rst)</pre>
obspred
nrow(obspred) # you get as many 'obs' as pixels + additional points per pixel
sum(obspred$obs) # as many presences as points that overlay 'pred'
# with removal of duplicates:
obspred_rmdup <- ptsrast2obspred(pts = crds(presences), rst = rst[[1]],</pre>
rm.dup = TRUE) # you get as many 'obs' as pixels
obspred_rmdup
nrow(obspred_rmdup) # you get as many 'obs' as pixels
sum(obspred_rmdup$obs) # as many presences as pixels that contain (one or more) points
```

## End(Not run)

range01

Shrink or stretch a vector to make it range between 0 and 1

#### Description

This function re-scales a numeric vector so that it ranges between 0 and 1. So, the lowest value becomes 0, the highest becomes 1, and the ones in the middle retain their rank and relative difference.

#### Usage

range01(x, na.rm = TRUE)

## Arguments

х	a numeric vector.
na.rm	logical, whether to remove NA values.

## Details

This function was borrowed from http://stackoverflow.com/questions/5468280/scale-a-series-between-two-points-in-r/5468527#5468527 and adapted to handle also missing values.

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## rotif.mods

## Value

A numeric vector of the same length as the input, now with the values ranging from 0 to 1.

#### Author(s)

A. Marcia Barbosa

# See Also

standard01

#### Examples

range01(0:10)

range01(-12.3 : 21.7)

rotif.mods

#### Rotifer distribution models

#### Description

A set of generalized linear models of rotifer species distributions on TDWG level 4 regions of the world (Fontaneto et al. 2012), together with their predicted values. Mind that these models are provided just as sample data and have limited application, due to limitations in the underlying distribution records. See Details for more information.

## Usage

data(rotif.mods)

#### Format

A list of 2 elements:

\$ predictions: a data.frame with 291 observations of 60 variables, namely the presence probability (P) and environmental favourability (F) for each of 30 species of rotifers, obtained from the rotif.env dataset in the 'fuzzySim' R-Forge package

\$ models: a list of the 30 generalized linear model (g1m) objects which generated those predictions.

## Details

These models were obtained with the 'multGLM' function and the rotif.env dataset from R-Forge package 'fuzzySim' using the following code:

require(fuzzySim)

data(rotif.env)

rotif.mods <- multGLM(data = rotif.env, sp.cols = 18:47, var.cols = 5:17, step = FALSE, trim = TRUE)

See package 'fuzzySim' (currently available on R-Forge at http://fuzzysim.r-forge.r-project. org) for more information on the source data that were used to build these models.

# References

Fontaneto D., Barbosa A.M., Segers H. & Pautasso M. (2012) The 'rotiferologist' effect and other global correlates of species richness in monogonont rotifers. Ecography, 35: 174-182.

## Examples

```
data(rotif.mods)
head(rotif.mods$predictions)
rotif.mods$models[[1]]
```

```
RsqGLM
```

R-squared measures for GLMs

## Description

This function calculates some (pseudo) R-squared statistics for binomial Generalized Linear Models.

#### Usage

```
RsqGLM(model = NULL, obs = NULL, pred = NULL, use = "pairwise.complete.obs",
plot = TRUE, ...)
```

model	a binary-response model object of class "glm". Alternatively, you can input the 'obs' and 'pred' arguments instead of 'model'.
obs	alternatively to 'model' and together with 'pred', a vector of observed presences (1) and absences (0) of a binary response variable. This argument is ignored if 'model' is provided.
pred	alternatively to 'model' and together with 'obs', a vector with the corresponding predicted values of presence probability. Must be of the same length and in the same order as 'obs'. This argument is ignored if 'model' is provided.
use	argument to be passed to cor for handling mising values.
plot	logical value indicating whether or not to display a barplot of the calculated measures.
	additional arguments to pass to the plot function (see Examples).

## **RsqGLM**

## Details

Implemented measures include the R-squareds of McFadden (1974), Cox-Snell (1989), Nagelkerke (1991, which corresponds to the corrected Cox-Snell, eliminating its upper bound), and Tjur (2009). See Allison (2014) for a brief review of these measures.

## Value

The function returns a named list of the calculated R-squared values.

# Note

Tjur's R-squared can only be calculated for models with binomial response variable; otherwise, NA will be returned.

## Author(s)

A. Marcia Barbosa

## References

Allison P. (2014) Measures of fit for logistic regression. SAS Global Forum, Paper 1485-2014

Cox, D.R. & Snell E.J. (1989) The Analysis of Binary Data, 2nd ed. Chapman and Hall, London

McFadden, D. (1974) Conditional logit analysis of qualitative choice behavior. In: Zarembka P. (ed.) Frontiers in Economics. Academic Press, New York

Nagelkerke, N.J.D. (1991) A note on a general definition of the coefficient of determination. Biometrika, 78: 691-692

Tjur T. (2009) Coefficients of determination in logistic regression models - a new proposal: the coefficient of discrimination. The American Statistician, 63: 366-372.

## See Also

Dsquared, AUC, threshMeasures, HLfit

#### Examples

```
# load sample models:
data(rotif.mods)
```

# choose a particular model to play with: mod <- rotif.mods\$models[[1]]</pre>

```
RsqGLM(model = mod)
```

# you can also use RsqGLM with vectors of observed and predicted values # instead of a model object:

RsqGLM(obs = mod\$y, pred = mod\$fitted.values)

```
# plotting arguments can be modified:
par(mar = c(6, 3, 2, 1))
RsqGLM(obs = mod$y, pred = mod$fitted.values, col = "seagreen", border = NA,
ylim = c(0, 1), las = 2, main = "Pseudo-R-squared values")
```

standard01

Standardize to 0-1 (or vice-versa)

#### Description

This function converts the score of a measure that ranges from -1 to 1 (e.g. a kappa or TSS value obtained for a model) into its (linearly) corresponding value in 0-to-1 scale, so that it can be compared directly with measures that range between 0 and 1 (such as CCR or AUC). It can also perform the conversion in the opposite direction.

## Usage

```
standard01(score, direction = c("-1+1to01", "01to-1+1"))
```

#### Arguments

score	numeric value indicating the score of the measure of interest.
direction	character value indicating the direction in which to perform the standardization.
	The default, "-1+1to01", can be switched to "01to-1+1".

#### Details

While most of the threshold-based measures of model evaluation range theoretically from 0 to 1, some of them (such as Cohen's kappa and the true skill statistic, TSS) may range from -1 to 1 (Allouche et al. 2006). Thus, the values of different measures may not be directly comparable (Barbosa 2015). We do not usually get negative values of TSS or kappa (nor values under 0.5 for CCR or AUC, for example) because that only happens when model predictions perform worse than random guesses; still, such values are mathematically possible, and can occur e.g. when extrapolating models to regions where where the species-environment relationships differ. This standardization is included as an option in the threshMeasures function.

## Value

The numeric value of 'score' when re-scaled to the 0-to-1 (or to the -1 to +1) scale.

#### Note

Note that this is not the same as re-scaling a vector so that it ranges between 0 and 1, which is done by range01.

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## threshMeasures

#### Author(s)

A. Marcia Barbosa

## References

Allouche O., Tsoar A. & Kadmon R. (2006) Assessing the accuracy of species distribution models: prevalence, kappa and the true skill statistic (TSS). Journal of Applied Ecology 43: 1223-1232

Barbosa, A.M. (2015) Re-scaling of model evaluation measures to allow direct comparison of their values. The Journal of Brief Ideas, 18 Feb 2015, DOI: 10.5281/zenodo.15487

#### See Also

threshMeasures, range01

## Examples

```
standard01(0.6)
standard01(0.6, direction = "-1+1to01")
standard01(0.6, direction = "01to-1+1")
```

threshMeasures Threshold-based measures of model evaluation

## Description

This function calculates a number of measures for evaluating the classification accuracy of a species distribution (or ecological niche, or bioclimatic envelope...) model against observed presenceabsence data (Fielding & Bell 1997; Liu et al. 2011; Barbosa et al. 2013), upon the choice of a threshold value above which the model is considered to predict that the species should be present.

#### Usage

```
threshMeasures(model = NULL, obs = NULL, pred = NULL, thresh,
measures = modEvAmethods("threshMeasures"), simplif = FALSE,
plot = TRUE, plot.ordered = FALSE, standardize = TRUE, verbosity = 2,
ylim = c(0, 1), interval = 0.01, quant = 0, na.rm = TRUE, rm.dup = FALSE, ...)
```

## Arguments

model a binary-response model object of class "glm", "gam", "gbm", "randomForest" or "bart". If this argument is provided, 'obs' and 'pred' will be extracted with mod2obspred. Alternatively, you can input the 'obs' and 'pred' arguments instead of 'model'.

obs	alternatively to 'model' and together with 'pred', a numeric vector of observed presences (1) and absences (0) of a binary response variable. Alternatively (and if 'pred' is a 'SpatRaster'), a two-column matrix or data frame containing, respectively, the x (longitude) and y (latitude) coordinates of the presence points, in which case the 'obs' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
pred	alternatively to 'model' and together with 'obs', a vector with the correspond- ing predicted values of presence probability, habitat suitability, environmental favourability or alike. Must be of the same length and in the same order as 'obs'. Alternatively (and if 'obs' is a set of point coordinates), a 'SpatRaster' map of the predicted values for the entire evaluation region, in which case the 'pred' vector will be extracted with ptsrast2obspred. This argument is ignored if 'model' is provided.
thresh	threshold to separate predicted presences from predicted absences in 'model' or 'pred'; can be a numeric value between 0 and 1, or any of the options provided with modEvAmethods("getThreshold"). See Details in ?getThreshold for a description of the available options, and also Details below for a more informed choice.
measures	character vector of the evaluation measures to use. By default, all measures available in 'modEvAmethods("threshMeasures")' are calculated.
simplif	logical, whether to calculate a faster, simplified version. Used internally by other functions in the package. Defaults to FALSE.
plot	logical, whether to produce a barplot of the calculated measures. Defaults to TRUE.
plot.ordered	logical, whether to plot the measures in decreasing order rather than in input order. Defaults to FALSE.
standardize	logical, whether to change measures that may range between -1 and +1 (namely kappa and TSS) to their corresponding value in the 0-to-1 scale (skappa and sTSS), so that they can compare directly to other measures (see standard01). The default is TRUE, but a message is displayed to inform the user about it.
verbosity	integer specifying the amount of messages to display. Defaults to the maximum implemented; lower numbers (down to 0) decrease the number of messages.
ylim	limits for the y axis.
interval	Numeric value, used if 'thresh' is a threshold optimization method such as "maxKappa" or "maxTSS", indicating the interval between the thresholds to test. The default is 0.01. Smaller values may provide more precise results but take longer to compute.
quant	Numeric value indicating the proportion of presences to discard if thresh="MTP" (minimum training presence). With the default value 0, MTP will be the threshold at which all observed presences are classified as such; with e.g. quant=0.05, MTP will be the threshold at which 5% presences will be classified as absences.
na.rm	Logical value indicating whether missing values should be ignored in computa- tions. Defaults to TRUE.
rm.dup	If TRUE and if 'pred' is a SpatRaster and if there are repeated points within the same pixel, a maximum of one point per pixel is used to compute the presences. See examples in ptsrast2obspred. The default is FALSE.

#### threshMeasures

#### . . .

additional arguments to be passed to the plot function.

#### Details

The threshold value can be chosen according to a number of criteria (see e.g. Liu et al. 2005, 2013; Jimenez-Valverde & Lobo 2007; Nenzen & Araujo 2011). You can choose a fixed numeric value, or set 'thresh' to "preval" (species' prevalence or proportion of presences **in the data in-put to this function**), or calculate optimal threshold values according to different criteria with the getThreshold, optiThresh or optiPair function. If you are using "environmental favourabil-ity" as input 'pred' data (Real et al. 2006; see 'Fav' function in R package **fuzzySim**), then the 0.5 threshold equates to using training prevalence in logistic regression (GLM with binomial error distribution and logit link function).

While most of these threshold-based measures range from 0 to 1, some of them (such as kappa and TSS) may range from -1 to 1 (Allouche et al. 2006), so their raw scores are not directly comparable. 'threshMeasures' includes an option (used by default) to standardize these measures to 0-1 (Barbosa 2015) using the standard@1 function, so that you obtain the standardized versions skappa and sTSS.

This function can also be used to calculate the agreement between different presence-absence (or other types of binary) data, as e.g. Barbosa et al. (2012) did for comparing mammal distribution data from atlas and range maps. Notice, however, that some of these measures, such as TSS or NMI, are not symmetrical (obs vs. pred is different from pred vs. obs).

## Value

If 'simplif = TRUE', the output is a numeric matrix with the name and value of each measure. If 'simplif = FALSE' (the default), the ouptut is a list with the following components:

Ν	the number of observations (records) in the analysis.
Prevalence	the prevalence (proportion of presences) in 'obs'.
Threshold	the threshold value used to calculate the 'measures'.
ConfusionMatri	X
	the confusion matrix obtained with the used threshold.

ThreshMeasures a numeric matrix with the name and value of each measure.

#### Note

"Sensitivity" is the same as "Recall", and "PPP" (positive predictive power) is the same as "Precision". "F1score"" is the harmonic mean of precision and recall.

## Note

"Sensitivity" is the same as "Recall", and "PPP" (positive predictive power) is the same as "Precision". Some of these measures (like NMI, UPR, OPR, PPP, NPP) cannot be calculated for thresholds at which there are zeros in the confusion matrix, so they can yield NaN values.

## Author(s)

A. Marcia Barbosa

#### References

Allouche O., Tsoar A. & Kadmon R. (2006) Assessing the accuracy of species distribution models: prevalence, kappa and the true skill statistic (TSS). Journal of Applied Ecology 43: 1223-1232.

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Barbosa A.M., Real R., Munoz A.R. & Brown J.A. (2013) New measures for assessing model equilibrium and prediction mismatch in species distribution models. Diversity and Distributions 19: 1333-1338

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Liu C., Berry P.M., Dawson T.P. & Pearson R.G. (2005) Selecting thresholds of occurrence in the prediction of species distributions. Ecography 28: 385-393

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Liu C., White M. & Newell G. (2013) Selecting thresholds for the prediction of species occurrence with presence-only data. Journal of Biogeography, 40: 778-789

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Real R., Barbosa A.M. & Vargas J.M. (2006) Obtaining environmental favourability functions from logistic regression. Environmental and Ecological Statistics 13: 237-245

#### See Also

optiThresh, optiPair, AUC

#### Examples

```
# load sample models:
data(rotif.mods)
# choose a particular model to play with:
mod <- rotif.mods$models[[1]]
threshMeasures(model = mod, simplif = TRUE, thresh = 0.5)
threshMeasures(model = mod, thresh = "preval")
threshMeasures(model = mod, plot.ordered = TRUE, thresh = "preval")
threshMeasures(model = mod, measures = c("CCR", "TSS", "kappa"),
thresh = "preval")
```

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## varPart

```
threshMeasures(model = mod, plot.ordered = TRUE, thresh = "preval")
# you can also use threshMeasures with vectors of observed and
# predicted values instead of with a model object:
threshMeasures(obs = mod$y, pred = mod$fitted.values, thresh = "preval")
# 'obs' can also be a table of presence point coordinates
# and 'pred' a SpatRaster of predicted values
```

varPart

Variation partitioning

#### Description

This function performs variation partitioning (Borcard et al. 1992) among two factors (e.g. Ribas et al. 2006) or three factors (e.g. Real et al. 2003) for either multiple linear regression models (LM) or generalized linear models (GLM).

#### Usage

```
varPart(A, B, C = NA, AB, AC = NA, BC = NA, ABC = NA,
model.type = NULL, A.name = "Factor A", B.name = "Factor B",
C.name = "Factor C", plot = TRUE, plot.digits = 3, cex.names = 1.5,
cex.values = 1.2, main = "", cex.main = 2, plot.unexpl = TRUE,
coloured = FALSE)
```

A	numeric value of the R-squared of the regression of the response variable on the variables related to factor 'A'
В	numeric value of the R-squared of the regression of the response variable on the variables related to factor 'B'
С	(optionally, if there are 3 factors) numeric value of the R-squared of the regression of the response on the variables related to factor 'C'
AB	numeric value of the R-squared of the regression of the response on the variables of factors 'A' and 'B' simultaneously
AC	(if there are 3 factors) numeric value of the R-squared of the regression of the response on the variables of factors 'A' and 'C' simultaneously
BC	(if there are 3 factors) numeric value of the R-squared of the regression of the response on the variables of factors 'B' and 'C' simultaneously
ABC	(if there are 3 factors) numeric value of the R-squared of the regression of the response on the variables of factors 'A', 'B' and 'C' simultaneously

model.type	deprecated argument, kept here for back-compatibility
A.name	character string indicating the name of factor 'A'
B.name	character string indicating the name of factor 'B'
C.name	character string indicating the name of factor 'C' (if there are 3 factors)
plot	logical, whether to plot the variation partitioning diagram. The default is TRUE.
plot.digits	integer value of the number of digits to which to round the values in the plot. The default is 3.
cex.names	numeric value indicating character expansion factor to define the size of the names of the factors displayed in the plot.
cex.values	numeric value indicating character expansion factor to define the size of the values displayed in the plot.
main	optional character string indicating the main title for the plot. The default is empty.
cex.main	numeric value indicating character expansion factor to define the font size of the plot title (if provided).
plot.unexpl	logical value indicating whether the amount of unexplained variation should be included in the plot. The default is TRUE.
coloured	logical value indicating whether or not to colour the circles in the plot. The default is FALSE for back-compatibility.

## Details

If you have linear models, input data for 'varPart' are the coefficients of determination (R-squared values) of the linear regressions of the target variable on all the variables in the model, on the variables related to each particular factor, and (when there are 3 factors) on the variables related to each pair of factors. The outputs are the amounts of variance explained exclusively by each factor, the amounts explained exclusively by the overlapping effects of each pair of factors, and the amount explained by the overlap of the 3 factors if this is the case (e.g. Real et al. 2003). The amount of variation not explained by the complete model is also provided.

If you have generalized linear models (GLMs) such as logistic regression (see glm), you have no true R-squared values; inputs can then be the squared coefficients of correlation between the model predictions given by each factor (or pair of factors) and the predictions of the complete model (e.g. Munoz & Real 2006), or the R-squared values of the corresponding logit (y) functions (Real et al. 2013), or an adjusted R-squared (De Araujo et al. 2013). In these cases, the "total variation" (AB or ABC, depending on whether you have two or three factors) is 1 (correlation of the predictions of the complete model with themselves), and output values are not the total amounts of variance (of the target variable) explained by factors and overlaps, but rather their proportional contribution to the total variation explained by the model.

## Value

The output consists of a data frame indicating the proportion of variance accounted for by each of the factors, and (if 'plot = TRUE') a Venn diagram of the contributions of each factor.

#### varPart

#### Note

These results derive from arithmetic operations between your input values, and they always sum up to 1; if your input is incorrect, the results will be incorrect as well, even if they sum up to 1.

This function had a bug up to modEvA version 0.8: a badly placed line break prevented the ABC overlap from being calculated correctly. Thanks to Jurica Levatic for pointing this out and helping to solve it!

Oswald van Ginkel also suggested a fix to some plotting awkwardness when using only two factors, and a nice option for colouring the plot. Many thanks!

## Author(s)

A. Marcia Barbosa

## References

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Real R., Romero D., Olivero J., Estrada A. & Marquez A.L. (2013) Estimating how inflated or obscured effects of climate affect forecasted species distribution. PLoS ONE 8: e53646.

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## Examples

```
# if you have a linear model (LM), use (non-adjusted) R-squared values
# for each factor and for their combinations as inputs:
# with 2 factors:
varPart(A = 0.456, B = 0.315, AB = 0.852, A.name = "Spatial",
B.name = "Environmental", main = "Small whale")
varPart(A = 0.456, B = 0.315, AB = 0.852, A.name = "Spatial",
B.name = "Environmental", main = "Small whale", col = TRUE)
```

# with 3 factors:

#### varPart

varPart(A = 0.456, B = 0.315, C = 0.281, AB = 0.051, BC = 0.444, AC = 0.569, ABC = 0.624, A.name = "Spatial", B.name = "Human", C.name = "Environmental", main = "Small whale")

varPart(A = 0.456, B = 0.315, C = 0.281, AB = 0.051, BC = 0.444, AC = 0.569, ABC = 0.624, A.name = "Spatial", B.name = "Human", C.name = "Environmental", main = "Small whale", col = TRUE)

# if you have a generalized linear model (GLM), # you can use squared correlation coefficients of the # predictions of each factor with those of the complete model:

varPart(A = (-0.005)^2, B = 0.698^2, C = 0.922^2, AB = 0.696^2, BC = 0.994^2, AC = 0.953^2, ABC = 1, A.name = "Topographic", B.name = "Climatic", C.name = "Geographic", main = "Big bird")

# but "Unexplained variation" can be deceiving in these cases
# (see Details); try also adding 'plot.unexpl = FALSE'

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