Package 'rstpm2'

July 14, 2022

Type Package

Title Smooth Survival Models, Including Generalized Survival Models

Version 1.5.7

Date 2022-07-13

Depends R (>= 3.0.2), methods, survival, splines

Imports graphics, Rcpp (>= 0.10.2), stats, mgcv, bbmle (>= 1.0.20), fastGHQuad, deSolve, utils, parallel

Suggests eha, testthat, ggplot2, lattice, readstata13, mstate, scales, survPen

LinkingTo Rcpp,RcppArmadillo,BH

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Description R implementation of generalized survival models (GSMs), smooth accelerated failure time (AFT) models and Markov multi-state mod-

els. For the GSMs, g(S(t|x))=eta(t,x) for a link function g, survival S at time t with covariates x and a linear predictor eta(t,x). The main assumption is that the time effect(s) are smooth <doi:10.1177/0962280216664760>. For fully parametric models with natural splines, this re-implements Stata's 'stpm2' function, which are flexible parametric survival models developed by Royston and colleagues. We have extended the parametric models to include any smooth parametric smoothers for time. We have also extended the model to include any smooth penalized smoothers from the 'mgcv' package, using penalized likelihood. These models include left truncation, right censoring, interval censoring, gamma frailties and normal random effects <doi:10.1002/sim.7451>, and copu-

las. For the smooth AFTs, $S(t|x) = S_0(t*eta(t,x))$, where the baseline survival function $S_0(t)=\exp(-\exp(eta_0(t)))$ is modelled for natural splines for eta_0, and the time-dependent cumulative acceleration factor $eta(t,x)=\int \exp(eta_1(t,x)) dt$ for log acceleration factor $eta_1(t,x)$. The Markov multi-state models allow for a range of models with smooth transitions to predict transition probabilities, length of stay, utilities and costs, with differences, ratios and standardisation.

URL https://github.com/mclements/rstpm2

BugReports https://github.com/mclements/rstpm2/issues

License GPL-2 | GPL-3

LazyData yes

Encoding UTF-8

NeedsCompilation yes

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Repository CRAN

Date/Publication 2022-07-13 22:50:02 UTC

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Description

Rstpm2-package

The package implements the stpm2 models from Stata. Such models use a flexible parametric formulation for survival models, using natural splines to model the log-cumulative hazard. Model predictions are rich, allowing for direct estimation of the hazard, survival, hazard ratios, hazard differences and survival differences. The models allow for time-varying effects, left truncation and relative survival.

The R implementation departs from the Stata implementation, using the ns() function, which is based on a projection of B-splines, rather than using truncated power splines as per Stata.

Details

Package: Rstpm2 Type: Package Version: 1.0

Date: 2011-07-06 License: GPL-2 LazyLoad: yes

Depends: methods, bbmle

Imports: splines, survival, stats, graphics

The package exports the stpm2 object, which inherits from the mle2 object from the bbmle package. Methods are specified for the stpm2 object, including predict and plot methods.

Author(s)

Mark Clements and Paul Lambert.

Maintainer: <mark.clements@ki.se>

See Also

stpm2

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Examples

aft

Parametric accelerated failure time model with smooth time functions

Description

This implements the accelerated failure time models $S_0(t \exp(beta x))$ and $S_0(int_0^t \exp(beta x(u)))$ du). The baseline function $S_0(t^*)$ is modelled as $\exp(-\exp(eta_0(\log(t^*))))$, where $eta_0(\log(t^*))$ is a linear predictor using natural splines.

Usage

```
aft(formula, data, smooth.formula = NULL, df = 3,
   tvc = NULL, control = list(parscale = 1, maxit = 1000),
   init = NULL, weights = NULL, timeVar = "", timeOVar = "",
   log.time.transform = TRUE,
   reltol = 1e-08, trace = 0, cure = FALSE, contrasts = NULL, subset = NULL,
   use.gr = TRUE, ...)
```

Cox regression, or a numeric vector of initial values.

Arguments

formula	a formula object, with the response on the left of a ~ operator, and the regression terms (excluding time) on the right. The response should be a survival object as returned by the Surv function. The terms can include linear effects for any time-varying coefficients. [required]
data	a data-frame in which to interpret the variables named in the formula argument. [at present: required]
smooth.formula	a formula for describing the time effects for the linear predictor, excluding the baseline $S_0(t^*)$, but including time-dependent acceleration factors. The time-dependent acceleration factors can be modelled with any smooth functions.
df	an integer that describes the degrees of freedom for the ns function for modelling the baseline log-cumulative hazards function (default=3).
tvc	a list with the names of the time-varying coefficients. This uses natural splines (e.g. tvc=list(hormon=3) is equivalent to smooth.formula=~+hormon:nsx(log(time),df=3)), which by default does <i>not</i> include an intercept (or main effect) term.
control	control argument passed to optim.
init	init should either be FALSE, such that initial values will be determined using

aft 5

weights an optional vector of 'prior weights' to be used in the fitting process. Should be

NULL or a numeric vector.

timeVar string variable defining the time variable. By default, this is determined from

the survival object, however this may be ambiguous if two variables define the

time.

time@Var string variable to determine the entry variable; useful for when more than one

data variable is used in the entry time.

log.time.transform

logical for whether to log-transform time when calculating the design matrix for

the derivative of S_0 with respect to time.

reltol relative tolerance for the model convergence

trace integer for whether to provide trace information from the optim procedure

cure logical for whether to model for cure (default=FALSE)

contrasts an optional list. See the contrasts.arg of model.matrix.default.

subset an optional vector specifying a subset of observations to be used in the fitting

process.

use.gr logical indicating whether to use gradients in the calculation

... additional arguments to be passed to the mle2.

Details

The implementation extends the mle2 object from the bbmle package. The model inherits all of the methods from the mle2 class.

Value

An stpm2-class object that inherits from mle2-class.

Author(s)

Mark Clements.

See Also

survreg, coxph

Examples

```
summary(aft(Surv(rectime,censrec==1)~hormon,data=brcancer,df=4))
```

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aft-class

Class "stpm2" ~~~

Description

Regression object for aft.

Objects from the Class

Objects can be created by calls of the form new("aft", ...) and aft(...).

Slots

```
args: Object of class "list" ~~
```

Extends

```
Class "mle2", directly.
```

Methods

```
plot signature(x = "aft", y = "missing"): ...
predict signature(object = "aft"): ...
predictnl signature(object = "aft", ...): ...
```

Examples

```
showClass("aft")
```

bhazard

Placemarker function for a baseline hazard function.

Description

Defined as the identity function.

Usage

bhazard(x)

Arguments

Х

Input (and output) value

Value

Returns the input value

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brcancer

German breast cancer data from Stata.

Description

```
See https://www.stata-press.com/data/r11/brcancer.dta.
```

Usage

```
data(brcancer)
```

Format

```
A data frame with 686 observations on the following 15 variables.
```

```
id a numeric vector
```

hormon hormonal therapy

```
x1 age, years
```

- x2 menopausal status
- x3 tumour size, mm
- x4 tumour grade
- x5 number of positive nodes
- x6 progesterone receptor, fmol
- x7 estrogen receptor, fmol

rectime recurrence free survival time, days

censrec censoring indicator

```
x4a tumour grade>=2
```

x4b tumour grade==3

x5e exp(-0.12*x5)

Examples

```
data(brcancer)
## maybe str(brcancer) ; plot(brcancer) ...
```

8 colon

coef<-

Generic method to update the coef in an object.

Description

Generic method to update the coef in an object.

Usage

```
coef(x) <- value</pre>
```

Arguments

x object to be updated

value value of the coefficient to be updated.

Details

This simple generic method is used for the numerical delta method.

Value

The updated object is returned.

Examples

```
##--- Should be DIRECTLY executable !! ----
##-- ==> Define data, use random,
##--or do help(data=index) for the standard data sets.
## The function is currently defined as
function (x, value)
UseMethod("coef<-")</pre>
```

colon

Colon cancer.

Description

Diagnoses of colon cancer.

Usage

```
data(colon)
```

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Format

```
A data frame with 15564 observations on the following 13 variables.

sex Sex (1=male, 2=female))
age Age at diagnosis
stage Clinical stage at diagnosis (1=Unknown, 2=Localised, 3=Regional, 4=Distant)
mmdx Month of diagnosis
yydx Year of diagnosis
surv_mm Survival time in months
surv_yy Survival time in years
status Vital status at last contact (1=Alive, 2=Dead: cancer, 3=Dead; other, 4=Lost to follow-up)
subsite Anatomical subsite of tumour (1=Coecum and ascending, 2=Transverse, 3=Descending
and sigmoid, 4=Other and NOS)
year8594 Year of diagnosis (1=Diagnosed 75-84, 2=Diagnosed 85-94)
agegrp Age in 4 categories (1=0-44, 2=45-59, 3=60-74, 4=75+)
dx Date of diagnosis
exit Date of exit
```

Details

Caution: there is a colon dataset in the survival package. We recommend using data(colon, package="rstpm2") to ensure the correct dataset is used.

Examples

```
data(colon,package="rstpm2") # avoids name conflict with survival::colon
## maybe str(colon); ...
```

cox.tvc

Test for a time-varying effect in the coxph model

Description

Test for a time-varying effect in the coxph model by re-fitting the partial likelihood including a time-varying effect, plot the effect size, and return the re-fitted model. The main advantage of this function over the tt() special is that it scales well for moderate sized datasets (cf. tt which expands the dataset and scales very poorly).

Usage

```
cox.tvc(obj, var=NULL, method="logt")
```

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Arguments

obj	A coxph object. Currently restricted to right censoring with Breslow ties and
	without stratification, etc.
var	String for the effect name. Currently assumes simple continuous effects.
method	A string representing the possible time transformations. Currently only "logt"

Value

Returns a tvcCoxph object (which inherits from the mle2 class) of the re-fitted model.

See Also

```
coxph, cox.zph
```

Examples

eform.stpm2

S3 method for to provide exponentiated coefficients with confidence intervals.

Description

S3 method for to provide exponentiated coefficents with confidence intervals.

Usage

```
eform(object, ...)
## S3 method for class 'stpm2'
eform(object, parm, level = 0.95, method = c("Profile", "Delta"), name = "exp(beta)")
## Default S3 method:
eform(object, parm, level = 0.95, method =
c("Delta", "Profile"), name = "exp(beta)", ...)
```

Arguments

object

```
parm not currently used

level significance level for the confidence interval

method method for confidence interval estimation
```

regression object

name for the fitted value

... other arguments

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grad

gradient function (internal function)

Description

Numerical gradient for a function at a given value (internal).

Usage

```
grad(func, x, ...)
```

Arguments

func Function taking a vector argument x (returns a vector of length>=1)

x vector of arguments for where the gradient is wanted.

... other arguments to the function

Details

(func(x+delta,...)-func(x-delta,...))/(2 delta) where delta is the third root of the machine precision times pmax(1,abs(x)).

Value

A vector if func(x) has length 1, otherwise a matrix with rows for x and columns for func(x).

Author(s)

Mark Clements.

See Also

numDelta()

gsm

Parametric and penalised generalised survival models

Description

This implements the generalised survival model g(S(t|x)) = eta, where g is a link function, S is survival, t is time, x are covariates and eta is a linear predictor. The linear predictor can include either parametric or penalised smoothers for the time effects, for time:covariate interactions and for covariate effects. The main model assumption is that the time effects in the linear predictor are smooth. This extends the class of flexible parametric survival models developed by Royston and colleagues. The model has been extended to include relative survival (excess hazards), Gamma frailties and normal random effects.

Usage

```
gsm(formula, data, smooth.formula = NULL, smooth.args = NULL,
                df = 3, cure = FALSE,
                tvc = NULL, tvc.formula = NULL,
                control = list(), init = NULL,
                weights = NULL, robust = FALSE, baseoff = FALSE,
                timeVar = "", time0Var = "", use.gr = NULL,
                optimiser=NULL, log.time.transform=TRUE,
                reltol=NULL, trace = NULL,
                link.type=c("PH","PO","probit","AH","AO"), theta.AO=0,
                contrasts = NULL, subset = NULL,
                robust_initial=NULL,
                coxph.strata = NULL, coxph.formula = NULL,
                logH.formula = NULL, logH.args = NULL,
                bhazard = NULL, bhazinit=NULL, copula=FALSE,
                frailty = !is.null(cluster) & !robust & !copula,
                cluster = NULL, logtheta=NULL,
                nodes=NULL, RandDist=c("Gamma","LogN"), recurrent = FALSE,
                adaptive = NULL, maxkappa = NULL,
                sp=NULL, criterion=NULL, penalty=NULL,
                smoother.parameters=NULL, Z=~1, outer_optim=NULL,
                alpha=1, sp.init=1,
                penalised=FALSE,
                ...)
stpm2(formula, data, weights=NULL, subset=NULL, coxph.strata=NULL, ...)
pstpm2(formula, data, weights=NULL, subset=NULL, coxph.strata=NULL, ...)
```

Arguments

formula a formula object, with the response on the left of a ~ operator, and the parametric

terms on the right. The response must be a survival object as returned by the

Surv function. Specials include cluster and bhazard. [required]

data a data.frame in which to interpret the variables named in the formula argument.

smooth. formula either a parametric formula or a penalised mgcv::gam formula for describing the

time effects and time-dependent effects and smoothed covariate effects on the

linear predictor scale (default=NULL). The default model is equal to ~s(log(time), k=-1)

where time is the time variable.

df an integer that describes the degrees of freedom for the ns function for modelling

the baseline log-cumulative hazard (default=3). Parametric model only.

smooth.args a list describing the arguments for the s function for modelling the baseline time

effect on the linear predictor scale (default=NULL).

tvc a list with the names of the time-varying coefficients. For a parametric model,

this uses natural splines (e.g. tvc=list(hormon=3) is equivalent to smooth.formula=~...+as.numeric

which by default does *not* include an intercept term, hence you should include a main effect. Note that this will convert a logical or factor variable to a numeric value, so the user should use indicators for factor terms. For a penalised model, this uses cubic splines (e.g. tvc=list(hormon=-1) is equivalent to

٠..

LVC

smooth.formula=~...+s(log(time), by=hormon, k=-1)), which by default *does* include an intercept (or main effect) term (and this code will remove any

main effect from formula).

tvc. formula separate formula for the time-varying effects. This is combined with smooth. formula

or the default smooth. formula.

baseoff Boolean used to determine whether fully define the model using tvc.formula

rather than combining logH. formula and tvc. formula

logH.args as per smooth.args. Deprecated. logH.formula as per smooth.formula. Deprecated.

cure logical for whether to estimate a cure model (parametric model only).

control list of arguments passed to gsm. control.

init init should either be NULL, such that initial values will be determined using

Cox regression, or a numeric vector of initial values.

coxph.strata variable in the data argument for stratification of the coxph model fit for esti-

mating initial values.

weights an optional vector of 'prior weights' to be used in the fitting process. Should be

NULL or a numeric vector.

robust Boolean used to determine whether to use a robust variance estimator.

bhazard variable for the baseline hazard for relative survival

bhazinit scalar used to adjust the background cumulative hazards for calculating initial

values. Default=0.1. Deprecated argument: use of the control argument is

preferred.

copula logical to indicate whether to use a copula model (experimental)

timeVar variable defining the time variable. By default, this is determined from the sur-

vival object, however this may be ambiguous if two variables define the time

sp fix the value of the smoothing parameters.

use.gr in R, a Boolean to determine whether to use the gradient in the optimisation. De-

fault=TRUE, Deprecated argument: use of the control argument is preferred.

criterion in Rcpp, determine whether to use "GCV" or "BIC" for the smoothing pa-

rameter selection.

penalty use either the "logH" penalty, which is the default penalty from mgcv, or the

"h" hazard penalty. Default="logH". Deprecated argument: use of the control

argument is preferred.

smoother.parameters

for the hazard penalty, a list with components which are lists with components

var, transform and inverse.

alpha an ad hoc tuning parameter for the smoothing parameter.

sp.init initial values for the smoothing parameters.

trace integer for trace reporting; 0 represents no additional reporting. Default=0. Dep-

recated argument: use of the control argument is preferred.

contrasts an optional list. See the contrasts.arg of model.matrix.default.

subset an optional vector specifying a subset of observations to be used in the fitting process. coxph.formula additional formula used to improve the fitting of initial values [optional and rarely used]. string variable to determine the entry variable; useful for when more than one time0Var data variable is used in the entry time. link.type type of link function. For "PH" (generalised proportional hazards), g(S)=log(log(S)); for "PO" (generalised proportional odds), g(S)=-logit(S); for "probit" (generalised probit), g(S)=-probit(S); for "AH" (generalised additive hazards), $g(S)=-\log(S)$; for "AO" (generalised Aranda-Ordaz), $g(S)=\log((S^{(-1)}+1))$ 1)/theta.AO). theta.A0 theta parameter for the Aranda-Ordaz link type. select which optimiser is used. Default="BFGS". Deprecated argument: use of optimiser the control argument is preferred. log.time.transform should a log-transformation be used for calculating the derivative of the design matrix with respect to time? (default=TRUE) recurrent logical for whether clustered, left truncated data are recurrent or for first event (where the latter requires an adjustment for the frailties or random effects) frailty logical for whether to fit a shared frailty model cluster variable that determines the cluster for the frailty. This can be a vector, a string for the column, or a name. This can also be specified using a special. logtheta initial value for log-theta used in the gamma shared frailty model (defaults to value from a coxph model fit) nodes number of integration points for Gaussian quadrature. Default=9. Deprecated argument: use of the control argument is preferred. RandDist type of distribution for the random effect or frailty adaptive logical for whether to use adaptive or non-adaptive quadrature, Default=TRUE. Deprecated argument: use of the control argument is preferred. double float value for the maximum value of the weight used in the constraint. maxkappa Default=1000. Deprecated argument: use of the control argument is preferred. Ζ formula for the design matrix for the random effects reltol list with components for search and final relative tolerances. Default=list(search=1e-10, final=1e-10, outer=1e-5). Deprecated argument: use of the control argument with arguments reltol.search, reltol.final and reltol.outer is preferred. Integer to indicate the algorithm for outer optimisation. If outer_optim=1 (deouter_optim fault), then use Neldear-Mead, otherwise use Nlm. logical for whether to use Nelder-Mead to find initial values (max 50 iterations). robust_initial This is useful for ill-posed initial values. Default= FALSE. Deprecated argument: use of the control argument is preferred. penalised logical to show whether to use penalised models with pstpm (penalised=TRUE) or parametrics models with stpm2 (penalised=FALSE).

additional arguments to be passed to the mle2.

Details

The implementation extends the mle2 object from the bbmle package.

The default smoothers for time on the linear predictor scale are nsxs(log(time), df=3) for the parametric model and s(log(time)) for the penalised model.

A frequently asked question is: why does rstpm2 give different spline estimates to flexsurv and Stata's stpm2? The short answer is that rstpm2 uses a different natural spline basis compared with flexsurv and Stata's stpm2 and slightly different knot placement than Stata's stpm2. If the knot placement is the same, then the predictions and other coefficients are expected to be very similar. As a longer answer, the default smoother in rstpm2 is to use an extension of the splines::ns function (rstpm2::nsx), which uses a QR projection of B-splines for natural splines. In contrast, flexsurv and Stata's stpm2 use truncated power splines for the natural spline basis (also termed 'restricted cubic splines'). The B-splines are known to have good numerical properties, while Stata's stpm2 implementation defaults to using matrix orthogonalisation to account for any numerical instability in the truncated power basis. Furthermore, rstpm2 allows for any smooth parametric function to be used as a smoother in stpm2/gsm, which is an extension over flexsurv and Stata's stpm2. Finally, it may be difficult to get rstpm2 and Stata's stpm2 to return the same estimates: although nsx includes an argument stata.stpm2.compatible = FALSE (change to TRUE for compatibility), the design matrix for rstpm2 is based on individuals with events, while Stata's stpm2 determines the spline knots from the individuals with events and the design matrix is otherwise based on all individuals.

Value

Either a stpm2-class or pstpm2-class object.

Author(s)

Mark Clements, Xing-Rong Liu, Benjamin Christoffersen.

Examples

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```
col=2)
   plot(fit.tvc,newdata=data.frame(hormon=0),type="sdiff",var="hormon")
   plot(fit.tvc,newdata=data.frame(hormon=0),type="hdiff",var="hormon")
   library(scales)
   cols <- c(alpha("red",alpha=0.2), alpha("blue",alpha=0.2))</pre>
   plot(fit.tvc,newdata=data.frame(hormon=0),type="hazard",ci.col=cols[1])
   lines(fit.tvc,newdata=data.frame(hormon=1),type="hazard",lty=2,ci.col=cols[2],
          ci=TRUE)
   legend("topright",legend=c("No hormonal treatment", "(95
       lty=c(1,1,2,1), lwd=c(1,10,1,10), col=c("black",cols[1],"black",cols[2]), bty="n")
   ## compare number of knots
   hormon0 <- data.frame(hormon=0)</pre>
   plot(fit,type="hazard",newdata=hormon0)
   AIC(fit)
   for (df in 4:6) {
       fit.new <- stpm2(Surv(rectime,censrec==1)~hormon,data=brcancer,df=df)</pre>
       plot(fit.new,type="hazard",newdata=hormon0,add=TRUE,ci=FALSE,line.col=df)
       print(AIC(fit.new))
   }
   ## compatibility with Stata's stpm2 using the smooth.formula argument (see Details)
   summary(stpm2(Surv(rectime,censrec==1)~hormon,data=brcancer,
                  smooth.formula=~nsx(log(rectime),df=3,stata.stpm2.compatible=TRUE)))
   summary(stpm2(Surv(rectime,censrec==1)~hormon,data=brcancer,
                  smooth.formula=~nsx(log(rectime),df=3,stata=TRUE)+
                  hormon:nsx(log(rectime),df=3,stata=TRUE)))
## End(Not run)
```

gsm.control

Defaults for the gsm call

Description

Set useful default and allow changes for the gsm call. This is meant to make the gsm call simpler.

Usage

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Arguments

parscale numeric vector or scalar for the scaling of the parameter values; default 1 maxit integer for the maximum number of iterations for the optimisation process

optimiser which optimiser to use for the outer optimisation trace integer indicating the trace level for each optimiser

nodes number of quadrature nodes

adaptive logical for whether to use adaptive or non-adaptive quadrature, Default=TRUE.

kappa.init initial value for the quadratic penalty for inequality constraints

eps.init initial value for epsilon

maxkappa double float value for the maximum value of the weight used in the constraint.

suppressWarnings.coxph.frailty

logical

robust_initial Not currently documented.

bhazinit Not currently documented.

use.gr Logical for whether to use gradients.

penalty Not currently documented.

outer_optim Not currently documented.

reltol.search Relative tolerance. Not currently documented.
reltol.final Relative tolerance. Not currently documented.
reltol.outer Relative tolerance. Not currently documented.

criterion Not currently documented.

incrVar

Utility that returns a function to increment a variable in a data-frame.

Description

A functional approach to defining an increment in one or more variables in a data-frame. Given a variable name and an increment value, return a function that takes any data-frame to return a data-frame with incremented values.

Usage

```
incrVar(var, increment = 1)
```

Arguments

var String for the name(s) of the variable(s) to be incremented

increment Value that the variable should be incremented.

Details

Useful for defining transformations for calculating rate ratios.

Value

A function with a single data argument that increments the variables in the data list/data-frame.

Examples

```
##---- Should be DIRECTLY executable !! ----
##-- ==> Define data, use random,
##--or do help(data=index) for the standard data sets.

## The function is currently defined as
function (var, increment = 1)
{
    n <- length(var)
    if (n > 1 && length(increment)==1)
        increment <- rep(increment, n)
    function(data) {
        for (i in 1:n) {
            data[[var[i]]] <- data[[var[i]]] + increment[i]
        }
        data
    }
    data
}</pre>
```

legendre.quadrature.rule.200

Legendre quadrature rule for n=200.

Description

Legendre quadrature rule for n=200.

Usage

```
data(legendre.quadrature.rule.200)
```

Format

A data frame with 200 observations on the following 2 variables.

```
x x values between -1 and 1 w weights
```

Examples

```
data(legendre.quadrature.rule.200)
## maybe str(legendre.quadrature.rule.200) ; ...
```

lines.stpm2

lines.stpm2 S3 methods for lines

Description

S3 methods for lines

Usage

```
## S3 method for class 'stpm2'
lines(x, newdata = NULL, type = "surv", col = 1, ci.col= "grey",
lty = par("lty"), ci = FALSE, rug = FALSE, var = NULL,
exposed = NULL, times = NULL,
type.relsurv = c("excess", "total", "other"),
ratetable = survival::survexp.us, rmap, scale = 365.24, ...)
## S3 method for class 'pstpm2'
lines(x, newdata = NULL, type = "surv", col = 1,
ci.col= "grey",
lty = par("lty"), ci = FALSE, rug = FALSE, var = NULL,
exposed = NULL, times = NULL, ...)
```

Arguments

X	an stpm2 object
newdata	required list of new data. This defines the unexposed newdata (<i>excluding</i> the event times).
type	specify the type of prediction
col	line colour
lty	line type
ci.col	confidence interval colour
ci	whether to plot the confidence interval band (default=TRUE)
rug	whether to add a rug plot of the event times to the current plot (default=TRUE)
var	specify the variable name or names for the exposed/unexposed (names are given as characters)
exposed	function that takes newdata and returns the exposed dataset. By default, this increments var (except for cure models, where it defaults to the last event time).
times	specifies the times. By default, this uses a span of the observed times.
type.relsurv	type of predictions for relative survival models: either "excess", "total" or "other"
scale	scale to go from the days in the ratetable object to the analysis time used in the analysis
rmap	an optional list that maps data set names to the ratetable names. See survexp
ratetable	a table of event rates used in relative survival when type.relsurv is "total" or "other" $$
	additional arguments (add to the plot command)

markov_msm

Predictions for continuous time, nonhomogeneous Markov multi-state models using parametric and penalised survival models.

Description

A numerically efficient algorithm to calculate predictions from a continuous time, nonhomogeneous Markov multi-state model. The main inputs are the models for the transition intensities, the initial values, the transition matrix and the covariate patterns. The predictions include state occupancy probabilities (possibly with discounting and utilities), length of stay and costs. Standard errors are calculated using the delta method. Includes, differences, ratios and standardisation.

Usage

```
markov_msm(x, trans, t = c(0,1), newdata = NULL, init=NULL,
              tmvar = NULL,
           sing.inf = 1e+10, method="adams", rtol=1e-10, atol=1e-10, slow=FALSE,
              min.tm=1e-8,
              utility=function(t) rep(1, nrow(trans)),
              utility.sd=rep(0,nrow(trans)),
              use.costs=FALSE,
         transition.costs=function(t) rep(0, sum(!is.na(trans))), # per transition
              transition.costs.sd=rep(0,sum(!is.na(trans))),
              state.costs=function(t) rep(0,nrow(trans)), # per unit time
              state.costs.sd=rep(0,nrow(trans)),
              discount.rate = 0,
              block.size=500,
              spline.interpolation=FALSE,
              debug=FALSE,
              ...)
## S3 method for class 'markov msm'
vcov(object, ...)
## S3 method for class 'markov_msm'
as.data.frame(x, row.names=NULL, optional=FALSE,
                                   ci=TRUE,
                                   P.conf.type="logit", L.conf.type="log",
   C.conf.type="log",
                                   P.range=c(0,1), L.range=c(0,Inf),
   C.range=c(0,Inf),
                                   state.weights=NULL, obs.weights=NULL,
                                    ...)
## S3 method for class 'markov_msm_diff'
as.data.frame(x, row.names=NULL, optional=FALSE,
                                   P.conf.type="plain", L.conf.type="plain",
   C.conf.type="plain",
                                   P.range=c(-Inf,Inf), L.range=c(-Inf,Inf),
   C.range=c(-Inf,Inf),
```

```
...)
## S3 method for class 'markov_msm_ratio'
as.data.frame(x, row.names=NULL, optional=FALSE, ...)
standardise(x, ...)
## S3 method for class 'markov_msm'
standardise(x,
                                 weights = rep(1,nrow(x$newdata)),
                                 normalise = TRUE, ...)
## S3 method for class 'markov_msm'
plot(x, y, stacked=TRUE, which=c('P','L'),
                          xlab="Time", ylab=NULL, col=2:6, border=col,
                          ggplot2=FALSE, lattice=FALSE, alpha=0.2,
                          strata=NULL,
                          ...)
## S3 method for class 'markov_msm'
subset(x, subset, ...)
## S3 method for class 'markov_msm'
diff(x, y, ...)
ratio_markov_msm(x, y, ...)
## S3 method for class 'markov_msm'
rbind(..., deparse.level=1)
## S3 method for class 'markov_msm'
transform(`_data`, ...)
collapse_markov_msm(object, which=NULL, sep="; ")
zeroModel(object)
hrModel(object,hr=1,ci=NULL,seloghr=NULL)
aftModel(object,af=1,ci=NULL,selogaf=NULL)
addModel(...)
hazFun(f, tmvar="t", ...)
splineFun(time, rate, method="natural", scale=1,...)
```

Arguments

For markov_msm:

list of functions or parametric or penalised survival models. Currently the models include combinations of stpm2, pstpm2, glm, gam, survPen or an object of class "zeroModel" from zeroModel based on one of the other classes. The order in the list matches the indexing in the trans argument. The functions can optionally use a t argument for time and/or a newdata argument. Uncertainty in the models are incorporated into the gradients, while uncertainty in the functions are currently not modelled.

trans

Transition matrix describing the states and transitions in the multi-state model. If S is the number of states in the multi-state model, trans should be an S x S matrix, with (i,j)-element a positive integer if a transition from i to j is possible in the multi-state model, NA otherwise. In particular, all diagonal elements should be NA. The integers indicating the possible transitions in the multi-state model should be sequentially numbered, $1, \ldots, K$, with K the number of transitions. See msprep

t numerical vector for the times to evaluation the predictions. Includes the start time data. frame of the covariates to use in the predictions newdata vector of the initial values with the same length as the number of states. Defaults init to the first state having an initial value of 1 (i.e. "[<-"(rep(0, nrow(trans)), 1, 1)). specifies the name of the time variable. This should be set for regression models tmvar that do not specify this (e.g. glm) or where the time variable is ambiguous If there is a singularity in the observed hazard, for example a Weibull distribution sing.inf with shape < 1 has infinite hazard at t=0, then as a workaround, the hazard is assumed to be a large finite number, sing.inf, at this time. The results should not be sensitive to the exact value assumed, but users should make sure by adjusting this parameter in these cases. method For markov_msm, the method used by the ordinary differential equation solver. Defaults to Adams method ("adams") for non-stiff differential equations. For splineFun, the method jused for spline interpolation; see splinefun. relative error tolerance, either a scalar or an array as long as the number of states. rtol Passed to 1sode atol absolute error tolerance, either a scalar or an array as long as the number of states. Passed to 1sode logical to show whether to use the slow R-only implementation. Useful for deslow bugging. Currently needed for costs. min.tm Minimum time used for evaluations. Avoids log(0) for some models. utility a function of the form function(t) that returns a utility for each state at time t for the length of stay values utility.sd a function of the form function(t) that returns the standard deviation for the utility for each state at time t for the length of stay values logical for whether to use costs. Default: FALSE use.costs transition.costs a function of the form function(t) that returns the cost for each transition transition.costs.sd a function of the form function(t) that returns the standard deviation for the cost for each transition state.costs a function of the form function(t) that returns the cost per unit time for each state.costs.sd a function of the form function(t) that returns the standard deviation for the cost per unit time for each state discount.rate numerical value for the proportional reduction (per unit time) in the length of stay and costs block.size divide newdata into blocks. Uses less memory but is slower. Reduce this number if the function call runs out of memory. spline.interpolation logical for whether to use spline interpolation for the transition hazards rather

than the model predictions directly (default=TRUE).

debug logical flag for whether to keep the full output from the ordinary differential

equation in the res component (default=FALSE).

... other arguments. For markov_msm, these are passed to the ode solver from

the deSolve package. For plot.markov_msm, these arguments are passed to

plot.default

For as.data.frame.markov_msm:

row.names add in row names to the output data-frame

optional (not currently used)

ci logical for whether to include confidence intervals. Default: TRUE

P. conf. type type of transformation for the confidence interval calculation for the state occu-

pancy probabilities. Default: log-log transformation. This is changed for diff

and ratio_markov_msm objects

L.conf.type type of transformation for the confidence interval calculation for the length of

stay calculation. Default: log transformation. This is changed for diff and

ratio_markov_msm objects

C.conf.type type of transformation for the confidence interval calculation for the length of

stay calculation. Default: log transformation. This is changed for diff and

ratio_markov_msm objects

P. range valid values for the state occupancy probabilities. Default: (0,1). This is changed

for diff and ratio_markov_msm objects

L.range valid values for the state occupancy probabilities. Default: (0,Inf). This is

changed for diff and ratio_markov_msm objects

C. range valid values for the state occupancy probabilities. Default: (0,Inf). This is

changed for diff and ratio_markov_msm objects

state.weights Not currently documented

obs.weights Not currently documented

For standardise.markov_msm:

weights numerical vector to use in standardising the state occupancy probabilities, length

of stay and costs. Default: 1 for each observation.

normalise logical for whether to normalise the weights to 1. Default: TRUE

For plot.markov_msm:

y (currently ignored)

stacked logical for whether to stack the plots. Default: TRUE

xlab x-axis label ylab x-axis label

col colours (ignored if ggplot2=TRUE)

border border colours for the polygon (ignored if ggplot=TRUE)

ggplot2 use ggplot2

alpha alpha value for confidence bands (ggplot)

lattice use lattice

strata formula for the stratification factors for the plot

For subset.markov_msm:

subset expression that is evaluated on the newdata component of the object to filter (or

restrict) for the covariates used for predictions

For transform.markov_msm:

_data an object of class "markov_msm"

For rbind.markov_msm:

deparse.level not currently used

For collapse.states:

which either an index of the states to collapse or a character vector of the state names

to collapse

sep separator to use for the collapsed state names

For zeroModel to predict zero rates:

object survival regression object to be wrapped

For hrModel to predict rates times a hazard ratio:

hr hazard ratio

seloghr alternative specification for the se of the log(hazard ratio); see also ci argument

For aftModel to predict accelerated rates:

af acceleration factor

selogaf alternative specification for the se of the log(acceleration factor); see also ci

argument

addModel predict rates based on adding rates from different models

hazFun provides a rate function without uncertainty:

f rate function, possibly with tmvar and/or newdata as arguments

splineFun predicts rates using spline interpolation:

time exact times

rate rates as per time

scale rate multiplier (e.g. scale=365.25 for converting from daily rates to yearly

rates)

Details

The predictions are calculated using an ordinary differential equation solver. The algorithm uses a single run of the solver to calculate the state occupancy probabilities, length of stay, costs and their partial derivatives with respect to the model parameters. The predictions can also be combined to calculate differences, ratios and standardised.

The current implementation supports a list of models for each transition.

The current implementation also only allows for a vector of initial values rather than a matrix. The predictions will need to be re-run for different vectors of initial values.

For as.data.frame.markov_msm_ratio, the data are provided in log form, hence the default transformations and bounds are as per as.data.frame.markov_msm_diff, with untransformed data on the real line.

TODO: allow for one model to predict for the different transitions.

Value

markov_msm returns an object of class "markov_msm".

The function summary is used to obtain and print a summary and analysis of variance table of the results. The generic accessor functions coef and vcov extract various useful features of the value returned by markov_msm.

An object of class "markov_msm" is a list containing at least the following components:

time a numeric vector with the times for the predictions

P an array for the predicted state occupancy probabilities. The array has three

dimensions: time, state, and observations.

L an array for the predicted sojourn times (or length of stay). The array has three

dimensions: time, state, and observations.

Pu an array for the partial derivatives of the predicted state occupancy probabilities

with respect to the model coefficients. The array has four dimensions: time,

state, coefficients, and observations.

Lu an array for the partial derivatives of the predicted sojourn times (or length

of stay) with respect to the model coefficients. The array has four dimensions:

time, state, coefficients, and observations.

newdata a data. frame with the covariates used for the predictions

vcov the variance-covariance matrix for the models of the transition intensities

trans copy of the trans input argument

call the call to the function

For debugging:

res data returned from the ordinary differential equation solver. This may include

more information on the predictions

Author(s)

Mark Clements

See Also

```
pmatrix.fs, probtrans
```

Examples

```
## Not run:
library(readstata13)
library(mstate)
library(ggplot2)
library(survival)
## Two states: Initial -> Final
## Note: this shows how to use markov_msm to estimate survival and risk probabilities based on
## smooth hazard models.
two_states <- function(model, ...) {</pre>
```

```
transmat = matrix(c(NA,1,NA,NA),2,2,byrow=TRUE)
    rownames(transmat) <- colnames(transmat) <- c("Initial", "Final")</pre>
    rstpm2::markov_msm(list(model), ..., trans = transmat)
}
## Note: the first argument is the hazard model. The other arguments are arguments to the
## markov_msm function, except for the transition matrix, which is defined by the new function.
death = gsm(Surv(time,status)~factor(rx), data=survival::colon, subset=(etype==2), df=3)
cr = two_states(death, newdata=data.frame(rx="0bs"), t = seq(0,2500, length=301))
plot(cr,ggplot=TRUE)
## Competing risks
## Note: this shows how to adapt the markov_msm model for competing risks.
competing_risks <- function(listOfModels, ...) {</pre>
    nRisks = length(listOfModels)
    transmat = matrix(NA,nRisks+1,nRisks+1)
    transmat[1,1+(1:nRisks)] = 1:nRisks
    rownames(transmat) <- colnames(transmat) <- c("Initial",names(listOfModels))</pre>
    rstpm2::markov_msm(listOfModels, ..., trans = transmat)
## Note: The first argument for competing_risks is a list of models. Names from that list are
## used for labelling the states. The other arguments are as per the markov_msm function,
## except for the transition matrix, which is defined by the competing_risks function.
recurrence = gsm(Surv(time, status)~factor(rx), data=survival::colon, subset=(etype==1), df=3)
death = gsm(Surv(time,status)~factor(rx), data=survival::colon, subset=(etype==2), df=3)
cr = competing_risks(list(Recurrence=recurrence, Death=death),
                     newdata=data.frame(rx=levels(survival::colon$rx)),
                     t = seq(0, 2500, length=301))
## Plot the probabilities for each state for three different treatment arms
plot(cr, ggplot=TRUE) + facet_grid(~ rx)
## And: differences in probabilities
cr_diff = diff(subset(cr,rx=="Lev+5FU"),subset(cr,rx=="0bs"))
plot(cr_diff, ggplot=TRUE, stacked=FALSE)
## Extended example: Crowther and Lambert (2017)
## library(rstpm2); library(readstata13); library(ggplot2)
mex.1 <- read.dta13("http://fmwww.bc.edu/repec/bocode/m/multistate_example.dta")</pre>
transmat <- rbind("Post-surgery"=c(NA,1,2),</pre>
                   "Relapsed"=c(NA,NA,3),
                   "Died"=c(NA,NA,NA))
colnames(transmat) <- rownames(transmat)</pre>
mex.2 <- transform(mex.1,osi=(osi=="deceased")+0)</pre>
levels(mex.2$size)[2] <- ">20-50 mm" # fix typo
mex <- mstate::msprep(time=c(NA,"rf","os"),status=c(NA,"rfi","osi"),</pre>
                      data=mex.2,trans=transmat,id="pid",
                      keep=c("age", "size", "nodes", "pr_1", "hormon"))
mex <- transform(mex,</pre>
                 size2=(unclass(size)==2)+0, # avoids issues with TRUE/FALSE
                 size3=(unclass(size)==3)+0,
                 hormon=(hormon=="yes")+0,
                 Tstart=Tstart/12,
                 Tstop=Tstop/12)
c.ar <- stpm2(Surv(Tstart,Tstop,status) ~ age + size2 + size3 + nodes + pr_1 + hormon,</pre>
```

```
data = mex, subset=trans==1, df=3, tvc=list(size2=1,size3=1,pr_1=1))
c.ad <- stpm2(Surv(Tstart, Tstop, status) \sim age + size + nodes + pr_1 + hormon,
              data = mex, subset=trans==2, df=1)
c.rd <- stpm2( Surv(Tstart,Tstop,status) ~ age + size + nodes + pr_1 + hormon,</pre>
              data=mex, subset=trans==3, df=3, tvc=list(pr_1=1))
##
nd <- expand.grid(nodes=seq(0,20,10), size=levels(mex$size))</pre>
nd <- transform(nd, age=54, pr_1=3, hormon=0,</pre>
                size2=(unclass(size)==2)+0,
                size3=(unclass(size)==3)+0)
## Predictions
system.time(pred1 <- rstpm2::markov\_msm(list(c.ar,c.ad,c.rd), t = seq(0,15,length=301),
                                         newdata=nd, trans = transmat)) # ~2 seconds
pred1 <- transform(pred1, Nodes=paste("Nodes =",nodes), Size=paste("Size",size))</pre>
## Figure 3
plot(pred1, ggplot=TRUE) + facet_grid(Nodes ~ Size) + xlab("Years since surgery")
plot(pred1, ggplot=TRUE, flipped=TRUE) +
    facet_grid(Nodes ~ Size) + xlab("Years since surgery")
plot(pred1, strata=~nodes+size, xlab="Years since surgery", lattice=TRUE)
plot(subset(pred1, nodes==0 & size=="<=20 mm"), stacked=FALSE, ggplot=TRUE) +</pre>
    facet_grid(. ~ state) +
    xlab("Years since surgery")
## Figure 5
a <- diff(subset(pred1, nodes==0 & size=="<=20 mm"),
          subset(pred1,nodes==0 & size==">20-50 mm"))
a <- transform(a, label = "Prob(Size<=20 mm)-Prob(20mm<Size<50mm)")</pre>
b <- ratio_markov_msm(subset(pred1, nodes==0 & size=="<=20 mm"),</pre>
                       subset(pred1,nodes==0 & size==">20-50 mm"))
b <- transform(b,label="Prob(Size<=20 mm)-Prob(20mm<Size<50mm)")</pre>
##
c <- diff(subset(pred1, nodes==0 & size=="<=20 mm"),</pre>
          subset(pred1,nodes==0 & size==">50 mm"))
c <- transform(c, label = "Prob(Size<=20 mm)-Prob(Size>=50mm)")
d <- ratio_markov_msm(subset(pred1, nodes==0 & size=="<=20 mm"),</pre>
                       subset(pred1,nodes==0 & size==">50 mm"))
d <- transform(d,label= "Prob(Size<=20 mm)-Prob(Size>=50mm)")
##
e <- diff(subset(pred1, nodes==0 & size==">20-50 mm"),
          subset(pred1,nodes==0 & size==">50 mm"))
e <- transform(e,label="Prob(20mm<Size<50 mm)-Prob(Size>=50mm)")
f <- ratio_markov_msm(subset(pred1,nodes==0 & size==">20-50 mm"),
                      subset(pred1,nodes==0 & size==">50 mm"))
f <- transform(f, label = "Prob(20mm<Size<50 mm)-Prob(Size>=50mm)")
## combine
diffs <- rbind(a,c,e)</pre>
ratios <- rbind(b,d,f)
## Figure 5
plot(diffs, stacked=FALSE, ggplot2=TRUE) + xlab("Years since surgery") +
    ylim(c(-0.4, 0.4)) + facet_grid(label ~ state)
plot(ratios, stacked=FALSE, ggplot2=TRUE) + xlab("Years since surgery") +
    ylim(c(0, 3)) + facet_grid(label ~ state)
```

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```
## Figure 6
plot(subset(pred1, nodes==0 & size=="<=20 mm"), stacked=FALSE, which="L", ggplot2=TRUE) +
    facet_grid(. ~ state) + xlab("Years since surgery")
## Figure 7
plot(diffs, stacked=FALSE, which="L", ggplot2=TRUE) + xlab("Years since surgery") +
    ylim(c(-4, 4)) + facet_grid(label ~ state)
plot(ratios, stacked=FALSE, which="L", ggplot2=TRUE) + xlab("Years since surgery") +
    ylim(c(0.1, 10)) + coord_trans(y="log10") + facet_grid(label ~ state)
## End(Not run)</pre>
```

markov_sde

Predictions for continuous time, nonhomogeneous Markov multi-state models using Aalen's additive hazards models.

Description

A numerically efficient algorithm to calculate predictions from a continuous time, nonhomogeneous Markov multi-state model. The main inputs are are a list of Aalen's additive hazards models, the initial values, the transition matrix and the covariate patterns. The predictions include state occupancy probabilities and length of stay. Standard errors are calculated using the delta method. Includes differences and standardisation.

Usage

Arguments

models

list of models. Currently allows only for aalen regression models.

trans

Transition matrix describing the states and transitions in the multi-state model. If S is the number of states in the multi-state model, trans should be an S x S matrix, with (i,j)-element a positive integer if a transition from i to j is possible in the multi-state model, NA otherwise. In particular, all diagonal elements should

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be NA. The integers indicating the possible transitions in the multi-state model should be sequentially numbered, 1,...,K, with K the number of transitions. See

msprep

newdata data. frame of the covariates to use in the predictions

init vector of the initial values with the same length as the number of states. Defaults

to the first state having an initial value of 1 (i.e. "[<-"(rep(0, nrow(trans)), 1, 1))).

nLebesgue Number of steps for the continuous integration

los logical variable for whether to estimate the length of stay nout number of rows to represent the continuous changes weights numeric vector to represent differences or standardisation

For plot.markov_sde:

y (currently ignored)

stacked logical for whether to stack the plots. Default: TRUE

index indicator of which row of newdata to plot

which character to indicate either transition probabilities ("P") or length of stay ("L")).

Default: "P".

xlab x-axis label ylab x-axis label

col colours (ignored if ggplot2=TRUE)

border border colours for the polygon (ignored if ggplot=TRUE)

ggplot2 use ggplot2

alpha alpha value for confidence bands (ggplot)

lattice use lattice

strata formula for the stratification factors for the plot

For as.data.frame.markov_sde:

row.names add in row names to the output data-frame

optional (not currently used)

ci logical for whether to include confidence intervals. Default: TRUE

P. conf. type type of transformation for the confidence interval calculation for the state occu-

pancy probabilities. Default: logit transformation. This is changed to "identity"

if any of the weights are negative

L.conf.type type of transformation for the confidence interval calculation for the length of

stay calculation. Default: log transformation. "identity" if any of the weights

are negative

P. range valid values for the state occupancy probabilities. Default: (0,1).

L. range valid values for the state occupancy probabilities. Default: (0,Inf).

For standardise.markov_sde:

x object to extract standardised values

... other arguments. For plot.markov_sde, these arguments are passed to plot.default.

For standardise.markov_sde, these arguments are not used, as the standardi-

sation must be done earlier in markov_sde.

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Details

Uses an approach developed by Ryalen and colleagues. This is a re-implementation in C++.

The current implementation only allows for a vector of initial values rather than a matrix. The predictions will need to be re-run for different vectors of initial values.

Value

```
markov_sde returns an object of class "markov_sde".
```

Author(s)

Mark Clements

See Also

markov_msm

nsx

Generate a Basis Matrix for Natural Cubic Splines (with eXtensions)

Description

Generate the B-spline basis matrix for a natural cubic spline (with eXtensions).

Usage

```
nsx(x, df = NULL, knots = NULL, intercept = FALSE,
    Boundary.knots = range(x), derivs = if (cure) c(2, 1) else c(2, 2),
    log = FALSE, centre = FALSE,
    cure = FALSE, stata.stpm2.compatible = FALSE)
```

Arguments

.,	the muedieten	i.ahla	Missina		oma allarriad
X	the predictor	variable.	VIISSING	values a	are allowed.

df degrees of freedom. One can supply df rather than knots; ns() then chooses

df - 1 - intercept + 4 - sum(derivs) knots at suitably chosen quantiles of x

(which will ignore missing values).

knots breakpoints that define the spline. The default is no knots; together with the

natural boundary conditions this results in a basis for linear regression on x. Typical values are the mean or median for one knot, quantiles for more knots.

See also Boundary.knots.

intercept if TRUE, an intercept is included in the basis; default is FALSE.

Boundary knots boundary points at which to impose the natural boundary conditions and anchor

the B-spline basis (default the range of the data). If both knots and Boundary. knots are supplied, the basis parameters do not depend on x. Data can extend beyond

Boundary.knots

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derivs	an integer vector of length 2 with values between 0 and 2 giving the derivative constraint order at the left and right boundary knots; an order of 2 constrains the second derivative to zero (f"(x)=0); an order of 1 constrains the first and second derivatives to zero (f'(x)=f"(x)=0); an order of 1 constrains the zero, first and second derivatives to zero (f(x)=f"(x)=f"(x)=0)
log	a Boolean indicating whether the underlying values have been log transformed; (deprecated: only used to calculate derivatives in rstpm2:::stpm2Old
centre	if specified, then centre the splines at this value (i.e. f(centre)=0) (default=FALSE)
cure	a Boolean indicated whether to estimate cure; changes the default derivs argument, such that the right boundary has the first and second derivatives constrained to zero; defaults to FALSE
stata.stpm2.co	mpatible
	a Boolean to determine whether to use Stata stpm's default knot placement; defaults to FALSE

Value

A matrix of dimension length(x) * df where either df was supplied or if knots were supplied, df = length(knots) + 1 + intercept. Attributes are returned that correspond to the arguments to ns, and explicitly give the knots, Boundary.knots etc for use by predict.nsx().

nsx() is based on the functions ns and spline.des. It generates a basis matrix for representing the family of piecewise-cubic splines with the specified sequence of interior knots, and the natural boundary conditions. These enforce the constraint that the function is linear beyond the boundary knots, which can either be supplied, else default to the extremes of the data. A primary use is in modeling formula to directly specify a natural spline term in a model.

The extensions from ns are: specification of the derivative constraints at the boundary knots; whether to centre the knots; incorporation of cure using derivatives; compatible knots with Stata's stpm2; and an indicator for a log-transformation of x for calculating derivatives.

References

Hastie, T. J. (1992) Generalized additive models. Chapter 7 of *Statistical Models in S* eds J. M. Chambers and T. J. Hastie, Wadsworth & Brooks/Cole.

See Also

```
ns, bs, predict.nsx, SafePrediction
```

Examples

```
require(stats); require(graphics); require(splines)
nsx(women$height, df = 5)
summary(fm1 <- lm(weight ~ ns(height, df = 5), data = women))
## example of safe prediction
plot(women, xlab = "Height (in)", ylab = "Weight (lb)")
ht <- seq(57, 73, length.out = 200)
lines(ht, predict(fm1, data.frame(height=ht)))</pre>
```

nsxD

nsxD Generate a Basis Matrix for the first derivative of Natural Cubic Splines (with eXtensions)

Description

Generate the B-spline basis matrix for the first derivative of a natural cubic spline (with eXtensions).

Usage

```
nsxD(x, df = NULL, knots = NULL, intercept = FALSE,
    Boundary.knots = range(x), derivs = if (cure) c(2, 1) else c(2, 2),
    log = FALSE, centre = FALSE,
    cure = FALSE, stata.stpm2.compatible = FALSE)
```

Arguments

X	the predictor variable. Missing values are allowed.
df	degrees of freedom. One can supply df rather than knots; ns() then chooses df - 1 - intercept + 4 - sum(derivs) knots at suitably chosen quantiles of x (which will ignore missing values).
knots	breakpoints that define the spline. The default is no knots; together with the natural boundary conditions this results in a basis for linear regression on x. Typical values are the mean or median for one knot, quantiles for more knots. See also Boundary.knots.
intercept	if TRUE, an intercept is included in the basis; default is FALSE.

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Boundary .knots boundary points at which to impose the natural boundary conditions and anchor

the B-spline basis (default the range of the data). If both knots and Boundary. knots are supplied, the basis parameters do not depend on x. Data can extend beyond

Boundary.knots

derivs an integer vector of length 2 with values between 0 and 2 giving the derivative

constraint order at the left and right boundary knots; an order of 2 constrains the second derivative to zero (f''(x)=0); an order of 1 constrains the first and second derivatives to zero (f'(x)=f''(x)=0); an order of 1 constrains the zero, first and

second derivatives to zero (f(x)=f'(x)=f''(x)=0)

log a Boolean indicating whether the underlying values have been log transformed;

(deprecated: only used to calculate derivatives in rstpm2:::stpm2Old

centre if specified, then centre the splines at this value (i.e. f(centre)=0) (default=FALSE)

cure a Boolean indicated whether to estimate cure; changes the default derivs ar-

gument, such that the right boundary has the first and second derivatives con-

strained to zero; defaults to FALSE

stata.stpm2.compatible

a Boolean to determine whether to use Stata stpm's default knot placement;

defaults to FALSE

Value

A matrix of dimension length(x) * df where either df was supplied or if knots were supplied, df = length(knots) + 1 + intercept. Attributes are returned that correspond to the arguments to ns, and explicitly give the knots, Boundary.knots etc for use by predict.nsxD().

nsxD() is based on the functions ns and spline.des. It generates a basis matrix for representing the family of piecewise-cubic splines with the specified sequence of interior knots, and the natural boundary conditions. These enforce the constraint that the function is linear beyond the boundary knots, which can either be supplied, else default to the extremes of the data. A primary use is in modeling formula to directly specify a natural spline term in a model.

The extensions from ns are: specification of the derivative constraints at the boundary knots; whether to centre the knots; incorporation of cure using derivatives; compatible knots with Stata's stpm2; and an indicator for a log-transformation of x for calculating derivatives.

References

Hastie, T. J. (1992) Generalized additive models. Chapter 7 of *Statistical Models in S* eds J. M. Chambers and T. J. Hastie, Wadsworth & Brooks/Cole.

See Also

```
ns, bs, predict.nsx, SafePrediction
```

Examples

```
require(stats); require(graphics); require(splines)
nsx(women$height, df = 5)
summary(fm1 <- lm(weight ~ ns(height, df = 5), data = women))</pre>
```

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```
## example of safe prediction
plot(women, xlab = "Height (in)", ylab = "Weight (lb)")
ht <- seq(57, 73, length.out = 200)
lines(ht, predict(fm1, data.frame(height=ht)))</pre>
```

numDeltaMethod

Calculate numerical delta method for non-linear predictions.

Description

Given a regression object and an independent prediction function (as a function of the coefficients), calculate the point estimate and standard errors

Usage

```
numDeltaMethod(object, fun, gd=NULL, ...)
```

Arguments

object	A regression object with methods coef and vcov.
fun	An independent prediction function with signature function (coef, \dots).
gd	Specified gradients
	Other arguments passed to fun.

Details

A more user-friendly interface is provided by predictnl.

plot-methods 35

Value

Estimate Point estimates
SE Standard errors

See Also

See Also predictnl.

Examples

```
##---- Should be DIRECTLY executable !! ----
##-- ==> Define data, use random,
##--or do help(data=index) for the standard data sets.

## The function is currently defined as
function (object, fun, ...)
{
    coef <- coef(object)
    est <- fun(coef, ...)
    Sigma <- vcov(object)
    gd <- grad(fun, coef, ...)
    se.est <- as.vector(sqrt(colSums(gd * (Sigma %*% gd))))
    data.frame(Estimate = est, SE = se.est)
}</pre>
```

plot-methods

plots for an stpm2 fit

Description

Given an stpm2 fit, return a plot

Usage

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Arguments

x an stpm2 object

y not used (for generic compatibility)

newdata required list of new data. This defines the unexposed newdata (excluding the

event times).

type specify the type of prediction

xlab x-axis label line.col line colour

ci.col confidence interval colour

ci whether to plot the confidence interval band (default=TRUE)

add whether to add to the current plot (add=TRUE) or make a new plot (add=FALSE)

(default=FALSE)

rug whether to add a rug plot of the event times to the current plot (default=TRUE)

var specify the variable name or names for the exposed/unexposed (names are given

as characters)

exposed function that takes newdata and returns the exposed dataset. By default, this

increments var (except for cure models, where it defaults to the last event time).

times specifies the times. By default, this uses a span of the observed times.

... additional arguments (add to the plot command)

Methods

```
x = "stpm2", y = "missing" an stpm2 fit
```

See Also

stpm2

popmort	Background mortality rates for the colon dataset.

Description

Background mortality rates for the colon dataset.

Usage

data(popmort)

predict-methods 37

Format

```
A data frame with 10600 observations on the following 5 variables. sex Sex (1=male, 2=female) prob One year probability of survival rate All cause mortality rate age Age by single year of age through to age 105 years year Calendar period
```

Examples

```
data(popmort)
## maybe str(popmort); ...
```

predict-methods

Predicted values for an stpm2 or pstpm2 fit

Description

Given an stpm2 fit and an optional list of new data, return predictions

Usage

```
## S4 method for signature 'stpm2'
predict(object, newdata=NULL,
                type=c("surv","cumhaz","hazard","density","hr","sdiff",
                "hdiff", "loghazard", "link", "meansurv", "meansurvdiff", "meanhr",
                "odds", "or", "margsurv", "marghaz", "marghr", "meanhaz", "af",
                "fail", "margfail", "meanmargsurv", "uncured", "rmst", "probcure",
                "lpmatrix", "gradh", "gradH", "rmstdiff"),
               grid=FALSE, seqLength=300,
               type.relsurv=c("excess","total","other"), scale=365.24,
               rmap, ratetable=survival::survexp.us,
               se.fit=FALSE,link=NULL,exposed=NULL,var=NULL,
               keep.attributes=FALSE, use.gr=TRUE,level=0.95,
               n.gauss.quad=100,full=FALSE,...)
    ## S4 method for signature 'pstpm2'
predict(object, newdata=NULL,
               type=c("surv","cumhaz","hazard","density","hr","sdiff",
                "hdiff", "loghazard", "link", "meansurv", "meansurvdiff", "meanhr",
                "odds", "or", "margsurv", "marghaz", "marghr", "meanhaz", "af",
                "fail", "margfail", "meanmargsurv", "rmst", "lpmatrix",
                "gradh", "gradH", "rmstdiff"),
               grid=FALSE, seqLength=300,
               se.fit=FALSE,link=NULL,exposed=NULL,var=NULL,
               keep.attributes=FALSE, use.gr=TRUE,level=0.95,
               n.gauss.quad=100,full=FALSE,...)
```

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Arguments

object an stpm2 or pstpm2 object

newdata optional list of new data (required if type in ("hr", "sdiff", "hdiff", "meansurvdiff", "or", "uncured")).

For type in ("hr", "sdiff", "hdiff", "meansurvdiff", "or", "af", "uncured"), this defines the unexposed newdata. This can be combined with grid to get a regular set of

event times (i.e. newdata would not include the event times).

specify the type of prediction: type

• "surv"survival probabilities

- "cumhaz"cumulative hazard
- · "hazard"hazard
- · "density"density
- · "hr"hazard ratio
- "sdiff"survival difference
- "hdiff"hazard difference
- "loghazard"log hazards
- "meansurv"mean survival
- "meansurvdiff"mean survival difference
- "odds"odds
- · "or"odds ratio
- "margsurv"marginal (population) survival
- "marghaz"marginal (population) hazard
- "marghr"marginal (population) hazard ratio
- "meanhaz"mean hazard
- "meanhr"mean hazard ratio
- "af"attributable fraction
- "fail"failure (=1-survival)
- "margfail"marginal failure (=1-marginal survival)
- "meanmargsurv"mean marginal survival, averaged over the frailty distribution
- "uncured" distribution for the uncured
- "rmst"restricted mean survival time
- "rmstdiff"restricted mean survival time difference
- "probcure"probability of cure
- "lpmatrix"design matrix

grid whether to merge newdata with a regular sequence of event times (default=FALSE)

seqLength length of the sequence used when grid=TRUE

type.relsurv type of predictions for relative survival models: either "excess", "total" or "other"

scale to go from the days in the ratetable object to the analysis time used in

the analysis

an optional list that maps data set names to the ratetable names. See survexp rmap

a table of event rates used in relative survival when type.relsurv is "total" or ratetable

"other"

scale

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se.fit	whether to calculate confidence intervals (default=FALSE)		
link	allows a different link for the confidence interval calculation (default=NULL, such that switch(type,surv="cloglog",cumhaz="log",hazard="log",hr="log",sdiff="I", hdiff="I",loghazard="I",link="I",odds="log",or="log",margsurv="cloglog", marghaz="log",marghr="log"))		
exposed	a function that takes newdata and returns a transformed data-frame for those exposed or the counterfactual. By default, this increments var (except for cure models, where it defaults to the last event time).		
var	specify the variable name or names for the exposed/unexposed (names are given as characters)		
keep.attributes			
	Boolean to determine whether the output should include the newdata as an attribute (default=TRUE)		
use.gr	Boolean to determine whether to use gradients in the variance calculations when they are available (default=TRUE)		
level	confidence level for the confidence intervals (default=0.95)		
n.gauss.quad	number of Gauassian quadrature points used for integrations (default=100)		
full	logical for whether to return a full data-frame with predictions and newdata combined. Useful for lattice and ggplot2 plots. (default=FALSE)		
	additional arguments (for generic compatibility)		

Details

The confidence interval estimation is based on the delta method using numerical differentiation.

Value

A data-frame with components Estimate, lower and upper, with an attribute "newdata" for the newdata data-frame.

Methods

```
object= "stpm2" an stpm2 fit
```

See Also

stpm2

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predict.nsx

Evaluate a Spline Basis

Description

Evaluate a predefined spline basis at given values.

Usage

```
## S3 method for class 'nsx'
predict(object, newx, ...)
```

Arguments

object the result of a call to nsx having attributes describing knots, degree, etc.

newx the x values at which evaluations are required.

... Optional additional arguments. At present no additional arguments are used.

Value

An object just like object, except evaluated at the new values of x.

These are methods for the generic function predict for objects inheriting from classes "nsx". See predict for the general behavior of this function.

See Also

nsx.

Examples

```
basis <- nsx(women$height, df = 5)
newX <- seq(58, 72, length.out = 51)
# evaluate the basis at the new data
predict(basis, newX)</pre>
```

predictnl

Estimation of standard errors using the numerical delta method.

Description

A simple, yet exceedingly useful, approach to estimate the variance of a function using the numerical delta method. A number of packages provide functions that analytically calculate the gradients; we use numerical derivatives, which generalises to models that do not offer analytical derivatives (e.g. ordinary differential equations, integration), or to examples that are tedious or error-prone to calculate (e.g. sums of predictions from GLMs).

predictnl 41

Usage

```
## Default S3 method:
predictnl(object, fun, newdata=NULL, gd=NULL, ...)
## S3 method for class 'lm'
predictnl(object, fun, newdata=NULL, ...)
## S3 method for class 'predictnl'
print(x, ...)
## S3 method for class 'formula'
predict(object,data,newdata,na.action,type="model.matrix",...)
## S3 method for class 'predictnl'
confint(object, parm, level=0.95, ...)
```

Arguments

object An object with coef, vcov and `coef<-` methods (required).

fun A function that takes object as the first argument, possibly with newdata and

other arguments (required). See notes for why it is often useful to include

newdata as an argument to the function.

newdata An optional argument that defines newdata to be passed to fun.

gd An optional matrix of gradients. If this is not specified, then the gradients are

calculated using finite differences.

parm currently ignored

level significance level for 2-sided confidence intervals

x a predictnl object to be printed.data object used to define the model frame

na.action passed to model.frame

type currently restricted to "model.matrix"... Other arguments that are passed to fun.

Details

The signature for fun is either fun(object, ...) or fun(object, newdata=NULL, ...).

The different predictn1 methods call the utility function numDeltaMethod, which in turn calls the grad function for numerical differentiation. The numDeltaMethod function calls the standard coef and vcov methods, and the non-standard `coef<-` method for changing the coefficients in a regression object. This non-standard method has been provided for several regression objects and essentially mirrors the coef method.

One potential issue is that some predict methods do not re-calculate their predictions for the fitted dataset (i.e. when newdata=NULL). As the predictnl function changes the fitted coefficients, it is required that the predictions are re-calculated. One solution is to pass newdata as an argument to both predictnl and fun; alternatively, newdata can be specified in fun. These approaches are described in the examples below. The numDeltaMethod method called by predictnl provides a warning when the variance estimates are zero, which may be due to this cause.

For completeness, it is worth discussing why the example predictnl(fit,predict) does not work for when fit is a glm object. First, predict.glm does not update the predictions for the

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fitted data. Second, the default predict method has a signature predict(object, ...), which does not include a newdata argument. We could then either (i) require that a newdata argument be passed to the fun function for all examples, which would make this corner case work, or (ii) only pass the newdata argument if it is non-null or in the formals for the fun function, which would fail for this corner case. The current API defaults to the latter case (ii). To support this approach, the predictnl.lm method replaces a null newdata with object\$data. We also provide a revised numdelta:::predict.lm method that performs the same operation, although its use is not encouraged due to its clumsiness.

Value

Returns an object of class an object with class c("predictnl", "data.frame") elements c("fit", "se.fit", "Estimate", and with methods print and confint. Note that the Estimate and SE fields are deprecated and their use is discouraged, as we would like to remove them from future releases.

Author(s)

Mark Clements

Examples

predictnl-methods

~~ Methods for Function predictnl ~~

Description

```
~~ Methods for function predictnl ~~
```

Methods

predictnl signature(object = "mle2", ...): Similar to predictnl.default, using S4 methods.

pstpm2-class 43

pstpm2-class

Class "pstpm2"

Description

Regression object for pstpm2.

Objects from the Class

Objects can be created by calls of the form new("pstpm2", ...) and pstpm2(...).

Slots

```
xlevels: Object of class "list" ~~
contrasts: Object of class "listOrNULL" ~~
terms: Object of class "terms" ~~
gam: Object of class "gam" ~~
logli: Object of class "function" ~~
timeVar: Object of class "character" ~~
time@Var: Object of class "character" ~~
time@Expr: Object of class "nameOrcall" ~~
timeExpr: Object of class "nameOrcall" ~~
like: Object of class "function" ~~
model.frame: Object of class "list" ~~
delayed: Object of class "logical" ~~
frailty: Object of class "logical" ~~
x: Object of class "matrix" ~~
xd: Object of class "matrix" ~~
termsd: Object of class "terms" ~~
Call: Object of class "character" ~~
y: Object of class "Surv" ~~
sp: Object of class "numeric" ~~
nevent: Object of class "numeric" ~~
link: Object of class "list" ~~
edf: Object of class "numeric" ~~
edf_var: Object of class "numeric" ~~
df: Object of class "numeric" ~~
call: Object of class "language" ~~
call.orig: Object of class "language" ~~
```

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```
coef: Object of class "numeric" ~~

fullcoef: Object of class "numeric" ~~

vcov: Object of class "matrix" ~~

min: Object of class "numeric" ~~

details: Object of class "list" ~~

minuslogl: Object of class "function" ~~

method: Object of class "character" ~~

data: Object of class "list" ~~

formula: Object of class "character" ~~

optimizer: Object of class "character" ~~

args: Object of class "list" ~~
```

Extends

```
Class "mle2", directly.
```

Methods

```
plot signature(x = "pstpm2", y = "missing"): ...
lines signature(x = "pstpm2", ...): ...
anova signature(object = "pstpm2", ...): ...
AIC signature(object = "pstpm2", ..., k=2): ...
AICc signature(object = "pstpm2", ..., nobs=NULL, k=2): ...
BIC signature(object = "pstpm2", ..., nobs = NULL): ...
qAICc signature(object = "pstpm2", ..., nobs = NULL, dispersion = 1, k = 2): ...
qAIC signature(object = "pstpm2", ..., dispersion = 1, k = 2): ...
summary signature(object = "pstpm2", ...): ...
eform signature(object = "pstpm2", ...): ...
predictnl signature(object = "pstpm2", ...): ...
```

```
showClass("pstpm2")
```

residuals-methods 45

residuals-methods

Residual values for an stpm2 or pstpm2 fit

Description

Given an stpm2 or pstpm2 fit, return residuals

Usage

```
## S4 method for signature 'stpm2'
residuals(object, type=c("li","gradli"))
    ## S4 method for signature 'pstpm2'
residuals(object, type=c("li","gradli"))
```

Arguments

object an stpm2 or pstpm2 object type specify the type of residuals:

- "li"log-likelihood components (not strictly residuals)
- "gradli"gradient of the log-likelihood components (not strictly residuals)

Details

The gradients are analytical.

Value

A vector or matrix.

Methods

```
object= "stpm2" an stpm2 fit
```

See Also

stpm2

46 smoothpwc

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rston	12-11	nter	na⊥

Internal functions for the rstpm2 package.

Description

Various utility functions used internally to the rstpm2 package.

Usage

```
lhs(formula)
rhs(formula)
lhs(formula) <- value
rhs(formula) <- value</pre>
```

Arguments

formula A formula

value A symbolic value to replace the current value.

smoothpwc

Utility to use a smooth function in markov_msm based on piece-wise constant values

Description

Utility to use a smooth function in markov_msm based on piece-wise constant values

Usage

```
smoothpwc(midts, rates, tmvar = "t", offsetvar = "", ...)
```

Arguments

midts mid-point values for time in each segment rates rates at those mid-points (or for the interval)

tmvar string for the time variable offsetvar string for a time offset variable

... other arguments

Details

Uses splines to smooth the log-rates. This assumes that the rates are strictly greater than zero.

stpm2-class 47

Value

a function that is used in markov_msm

Examples

stpm2-class

Class "stpm2" ~~~

Description

Regression object for stpm2.

Objects from the Class

Objects can be created by calls of the form new("stpm2", ...) and stpm2(...).

Slots

```
xlevels: Object of class "list" ~~
contrasts: Object of class "listOrNULL" ~~
terms: Object of class "terms" ~~
logli: Object of class "function" ~~
lm: Object of class "lm" ~~
timeVar: Object of class "character" ~~
time@Var: Object of class "character" ~~
timeExpr: Object of class "nameOrcall" ~~
delayed: Object of class "logical" ~~
```

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```
frailty: Object of class "logical" ~~
    interval: Object of class "logical" ~~
    model.frame: Object of class "list" ~~
    call.formula: Object of class "formula" ~~
    x: Object of class "matrix" ~~
    xd: Object of class "matrix" ~~
    termsd: Object of class "terms" ~~
   Call: Object of class "character" ~~
    y: Object of class "Surv" ~~
    link: Object of class "list" ~~
    call: Object of class "language" ~~
    call.orig: Object of class "language" ~~
    coef: Object of class "numeric" ~~
    fullcoef: Object of class "numeric" ~~
    vcov: Object of class "matrix" ~~
    min: Object of class "numeric" ~~
    details: Object of class "list" ~~
    minuslogl: Object of class "function" ~~
    method: Object of class "character" ~~
    data: Object of class "list" ~~
    formula: Object of class "character" ~~
    optimizer: Object of class "character" ~~
    args: Object of class "list" ~~
Extends
    Class "mle2", directly.
Methods
   plot signature(x = "stpm2", y = "missing"): ...
   lines signature(x = "stpm2", ...): ...
    predictnl signature(object = "stpm2", ...): ...
    summary signature(object = "stpm2", ...): ...
    eform signature(object = "stpm2", ...): ...
```

```
showClass("stpm2")
```

tvcCoxph-class 49

tvcCoxph-class

Class "tvcCoxph"

Description

Experimental approach to modelling time-dependent effects in Cox regression.

Objects from the Class

Objects can be created by calls of the form new("tvcCoxph", ...) or cox.tvc(...). See the "mle2" documentation.

Slots

```
call: Object of class "language" ~~
call.orig: Object of class "language" ~~
coef: Object of class "numeric" ~~
fullcoef: Object of class "numeric" ~~
vcov: Object of class "matrix" ~~
min: Object of class "numeric" ~~
details: Object of class "list" ~~
minuslogl: Object of class "function" ~~
method: Object of class "character" ~~
data: Object of class "character" ~~
optimizer: Object of class "character" ~~
```

Extends

```
Class "mle2", directly.
```

Methods

```
plot signature(x = "tvcCoxph", y = "missing"): ...
```

```
showClass("tvcCoxph")
```

update-methods

Methods for Function update

Description

Methods for function update

Methods

update signature(object = "stpm2", ...): Similar to update.default, using S4 methods.

vuniroot

Vectorised One Dimensional Root (Zero) Finding

Description

The function vuniroot searches the interval from lower to upper for a root (i.e., zero) of the vectorised function f with respect to its first argument.

Setting extendInt to a non-"no" string, means searching for the correct interval = c(lower, upper) if sign(f(x)) does not satisfy the requirements at the interval end points; see the 'Details' section.

Usage

Arguments

f the function for which the root is sought.

interval a matrix with two columns containing the end-points of the interval to be searched

for the root.

... additional named or unnamed arguments to be passed to f

lower, upper the lower and upper end points of the interval to be searched.

f.lower, f.upper

the same as f(upper) and f(lower), respectively. Passing these values from the caller where they are often known is more economical as soon as f() contains

non-trivial computations.

extendInt character string specifying if the interval c(lower, upper) should be extended

or directly produce an error when f() does not have differing signs at the endpoints. The default, "no", keeps the search interval and hence produces an error.

Can be abbreviated.

check.conv logical indicating whether a convergence warning of the underlying vuniroot

should be caught as an error and if non-convergence in maxiter iterations should

be an error instead of a warning.

tol the desired accuracy (convergence tolerance).

maxiter the maximum number of iterations.

trace integer number; if positive, tracing information is produced. Higher values giv-

ing more details.

Details

Note that arguments after . . . must be matched exactly.

Either interval or both lower and upper must be specified: the upper endpoint must be strictly larger than the lower endpoint.

The function values at the endpoints must be of opposite signs (or zero), for extendInt="no", the default. Otherwise, if extendInt="yes", the interval is extended on both sides, in search of a sign change, i.e., until the search interval [l, u] satisfies $f(l) \cdot f(u) \leq 0$.

If it is known how f changes sign at the root x_0 , that is, if the function is increasing or decreasing there, extendInt can (and typically should) be specified as "upX" (for "upward crossing") or "downX", respectively. Equivalently, define $S:=\pm 1$, to require $S=\mathrm{sign}(f(x_0+\epsilon))$ at the solution. In that case, the search interval [l,u] possibly is extended to be such that $S\cdot f(l)\leq 0$ and $S\cdot f(u)\geq 0$.

vuniroot() uses a C++ subroutine based on "zeroin" (from Netlib) and algorithms given in the reference below. They assume a continuous function (which then is known to have at least one root in the interval).

Convergence is declared either if f(x) == 0 or the change in x for one step of the algorithm is less than tol (plus an allowance for representation error in x).

If the algorithm does not converge in maxiter steps, a warning is printed and the current approximation is returned.

f will be called as f(x, ...) for a numeric value of x.

The argument passed to f has special semantics and used to be shared between calls. The function should not copy it.

Value

A list with at least three components: root and f.root give the location of the root and the value of the function evaluated at that point. iter gives the number of iterations used.

Further components may be added in future: component init.it was added in R 3.1.0.

Source

Based on 'zeroin.c' in http://www.netlib.org/c/brent.shar.

References

Brent, R. (1973) Algorithms for Minimization without Derivatives. Englewood Cliffs, NJ: Prentice-Hall.

See Also

uniroot for the standard single root solver polyroot for all complex roots of a polynomial; optimize, nlm.

```
require(utils) # for str
## some platforms hit zero exactly on the first step:
## if so the estimated precision is 2/3.
f \leftarrow function(x, a) x - a
str(xmin < -vuniroot(f, lower=c(0, 0), upper=c(1,1), tol = 0.0001, a = c(1/3,2/3)))
## handheld calculator example: fixed point of cos(.):
vuniroot(function(x) cos(x) - x, lower = -pi, upper = pi, tol = 1e-9)$root
str(vuniroot(function(x) x*(x^2-1) + .5, lower = -2, upper = 2,
            tol = 0.0001)
str(vuniroot(function(x) x*(x^2-1) + .5, lower = -2, upper = 2,
            tol = 1e-10)
## Find the smallest value x for which exp(x) > 0 (numerically):
r <- vuniroot(function(x) 1e80*exp(x) - 1e-300, cbind(-1000, 0), tol = 1e-15)
str(r, digits.d = 15) # around -745, depending on the platform.
exp(r$root)
               # = 0, but not for r$root * 0.999...
minexp <- r$root * (1 - 10*.Machine$double.eps)</pre>
exp(minexp)
               # typically denormalized
##--- vuniroot() with new interval extension + checking features: --------
f1 \leftarrow function(x) (121 - x^2)/(x^2+1)
f2 \leftarrow function(x) \exp(-x)*(x - 12)
tools::assertCondition(vuniroot(f1, cbind(0,10)),
                       "error", verbose=TRUE)
tools::assertCondition(vuniroot(f2, cbind(0, 2)),
                       "error", verbose=TRUE)
##--> error: f() .. end points not of opposite sign
## where as 'extendInt="yes"' simply first enlarges the search interval:
u1 <- vuniroot(f1, cbind(0,10),extendInt="yes", trace=1)</pre>
u2 <- vuniroot(f2, cbind(0,2), extendInt="yes", trace=2)
stopifnot(all.equal(u1$root, 11, tolerance = 1e-5),
          all.equal(u2$root, 12, tolerance = 6e-6))
## The *danger* of interval extension:
## No way to find a zero of a positive function, but
## numerically, f(-|M|) becomes zero :
tools::assertCondition(u3 <- vuniroot(exp, cbind(0,2), extendInt="yes", trace=TRUE),
```

```
"error", verbose=TRUE)
## Nonsense example (must give an error):
tools::assertCondition( vuniroot(function(x) 1, cbind(\emptyset,1), extendInt="yes"),
                       "error", verbose=TRUE)
## Convergence checking :
sinc_< - function(x) ifelse(x == 0, 1, sin(x)/x)
curve(sinc_, -6,18); abline(h=0,v=0, lty=3, col=adjustcolor("gray", 0.8))
vuniroot(sinc_, cbind(0,5), extendInt="yes", maxiter=4) #-> "just" a warning
## now with check.conv=TRUE, must signal a convergence error :
vuniroot(sinc_, cbind(0,5), extendInt="yes", maxiter=4, check.conv=TRUE)
### Weibull cumulative hazard (example origin, Ravi Varadhan):
cumhaz \leftarrow function(t, a, b) b * (t/b)^a
froot <- function(x, u, a, b) cumhaz(x, a, b) - u
n <- 10
u <- -log(runif(n))</pre>
a <- 1/2
b <- 1
## Find failure times
ru <- vuniroot(froot, u=u, a=a, b=b, interval= cbind(rep(1.e-14,n), rep(1e4,n)),</pre>
               extendInt="yes")$root
ru2 <- vuniroot(froot, u=u, a=a, b=b, interval= cbind(rep(0.01,n), rep(10,n)),
                extendInt="yes")$root
stopifnot(all.equal(ru, ru2, tolerance = 6e-6))
r1 <- vuniroot(froot, u= 0.99, a=a, b=b, interval= cbind(0.01, 10),
             extendInt="up")
stopifnot(all.equal(0.99, cumhaz(r1$root, a=a, b=b)))
## An error if 'extendInt' assumes "wrong zero-crossing direction":
vuniroot(froot, u= 0.99, a=a, b=b, interval= cbind(0.1, 10), extendInt="down")
```

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