## Package 'rtmpt'

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Title Fitting RT-MPT Models

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Imports coda, data.table, loo, methods, Ryacas, stats, stringr,

truncnorm, utils

Suggests knitr, rmarkdown

VignetteBuilder knitr

NeedsCompilation yes

**SystemRequirements** GSL (>=2.3)

**Description** Fit response-time extended multinomial processing tree (RT-MPT) models by Klauer and

Kellen (2018) <doi:10.1016/j.jmp.2017.12.003>. The RT-MPT class not only incorporate

frequencies like traditional multinomial processing tree (MPT) models, but also laten-

cies. This enables it

to estimate process completion times and encoding plus motor execution times next to the process probabilities

of traditional MPTs. 'rtmpt' is a Bayesian framework and posterior samples are sampled using a Metropolis-Gibbs

sampler like the one described in the Klauer and Kellen (2018), but with some modifications. Other than in

the original C++ program we use the free and open source GNU Scientific Li-

brary (GSL). There is also the

possibility to suppress single process completion times.

**License** GPL (>= 2)

**Encoding UTF-8** 

LazyData true

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## **R** topics documented:

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## Description

Mapping response categories with encoding and motor execution times (deltas). Unlike the processes there are no names for the different deltas and therefore a mapping from response categories to different deltas must be specified.

## Usage

```
delta2delta(model, trees, categories, mappings = 0)
set_deltas_equal(model, trees, categories, mappings = 0)
```

## Arguments

model	A list of the class rtmpt_model.
trees	Character or numerical vector giving the trees
categories	Character or numerical vector identifying category/ies within the specified trees for which the deltas should be changed.
mappings	Numerical vector of length length(categories) providing the mappings. Default is 0.

## Value

A list of the class rtmpt\_model.

## Author(s)

Raphael Hartmann

#### See Also

theta2const, tau2zero, theta2theta, and tau2tau,

## **Examples**

```
# Detect-Guess variant of the Two-High Threshold model.
# The encoding and motor execution times will be set to different responses
mdl_2HTM <- "
# targets
do+(1-do)*g
(1-do)*(1-g)
# lures
(1-dn)*g
dn+(1-dn)*(1-g)
# do: detect old; dn: detect new; g: guess
model <- to_rtmpt_model(mdl_file = mdl_2HTM)</pre>
## changing the model to have two different encoding and motor execution
## times for "old" and "new" responses.
new_model \leftarrow delta2delta(model = model, trees = c(0, 1),
                     categories = c(1,3), mappings = c(1,1))
new_model
## changing the model to have two different encoding and response execution
## times for "old" and "new" responses.
new_model \leftarrow set_deltas_equal(model = model, trees = c(0, 1),
                         categories = c(1,3), mappings = c(1,1))
new_model
```

fit\_rtmpt

Posterior sample, diagnostics and some optional stuff for RT-MPT models

## **Description**

Given model and data, this function calls an altered version of the C++ program by Klauer and Kellen (2018) to sample from the posterior distribution via a Metropolis-Gibbs sampler and storing

it in an mcmc.list called samples. Posterior predictive checks developed by Klauer (2010), deviance information criterion (DIC; Spiegelhalter et al., 2002), 99% and 95% highest density intervals (HDI) together with the median will be provided for the main parameters in a list called diags. Optionally, the indices widely applicable information criterion (WAIC; Watanabe, 2010; Vehtari et al., 2017) and leave-one-out cross-validation (LOO; Vehtari et al., 2017) can be saved. Additionally the log-likelihood (LogLik) can also be stored. Some specifications of the function call are also saved in specs.

## Usage

```
fit_rtmpt(
  model,
  data,
  n.chains = 4,
  n.iter = 5000,
  n.burnin = 200,
  n.thin = 1,
  Rhat_max = 1.05,
  Irep = 1000,
  prior_params = NULL,
  indices = FALSE,
  save_log_lik = FALSE,
  old_label = FALSE
)
```

## **Arguments**

model A list of the class rtmpt\_model.

data Optimally, a list of class rtmpt\_data. Also possible is a data. frame or a path to

the text file. Both, data.frame and the text file must contain the column names "subj", "group", "tree", "cat", and "rt" preferably but not necessarily in this order. The values of the latter must be in milliseconds. It is always advised to use to\_rtmpt\_data first, which gives back an rtmpt\_data list with informations

about the changes in the data, that were needed.

n.chains Number of chains to use. Default is 4. Must be larger than 1 and smaller or

equal to 16.

n.iter Number of samples per chain. Default is 5000.

n.burnin Number of warm-up samples. Default is 200.

n. thin Thinning factor. Default is 1.

Rhat\_max Maximal Potential scale reduction factor: A lower threshold that needs to be

reached before the actual sampling starts. Default is 1.05

Irep Every Irep samples an interim state with the current maximal potential scale reduction factor is shown. Default is 1000. The following statements must hold

true for Irep:

• n. burnin is smaller than or equal to Irep,

• Irep is a multiple of n. thin and

• n. iter is a multiple of Irep / n. thin.

prior\_params

Named list with prior parameters. All parameters have default values, that lead to uninformative priors. Vectors are not allowed. Allowed parameters are:

- mean\_of\_exp\_mu\_beta: This is the a priori expected exponential rate (E(exp(beta)) = E(lambda)) and 1/mean\_of\_exp\_mu\_beta is the a priori expected process time (1/E(exp(beta)) = E(tau)). The default mean is set to 10, such that the expected a priori process time is 0.1 seconds.
- var\_of\_exp\_mu\_beta: The a priori group-specific variance of the exponential rates. Since exp(mu\_beta) is Gamma distributed, the rate of the distribution is just mean divided by variance and the shape is the mean times the rate. The default is set to 100.
- mean\_of\_mu\_gamma: This is the a priori expected mean parameter of the
  encoding and response execution times, which follow a normal distribution
  truncated from below at zero, so E(mu\_gamma) < E(gamma). The default is
  0.</li>
- var\_of\_mu\_gamma: The a priori group-specific variance of the mean parameter. Its default is 10.
- mean\_of\_omega\_sqr: This is the a priori expected residual variance (E(omega^2)).
   Its distribution differs from the one used in the paper. Here it is a Gamma distribution instead of an improper one. The default is 0.005.
- var\_of\_omega\_sqr: The a priori variance of the residual variance (Var(omega^2)). The default is 0.01. The default of the mean and variance is equivalent to a shape and rate of 0.0025 and 0.5, respectively.
- df\_of\_sigma\_sqr: A priori degrees of freedom for the individual variance
  of the response executions. The individual variance has a scaled inverse
  chi-squared prior with df\_of\_sigma\_sqr degrees of freedom and omega^2
  as scale. 2 is the default and it should be an integer.
- sf\_of\_scale\_matrix\_SIGMA: The original scaling matrix (S) of the (scaled) inverse Wishart distribution for the process related parameters is an identity matrix S=I. sf\_of\_scale\_matrix\_SIGMA is a scaling factor, that scales this matrix (S=sf\_of\_scale\_matrix\_SIGMA\*I). Its default is 1.
- sf\_of\_scale\_matrix\_GAMMA: The original scaling matrix (S) of the (scaled) inverse Wishart distribution for the encoding and motor execution parameters is an identity matrix S=I. sf\_of\_scale\_matrix\_GAMMA is a scaling factor, that scales this matrix (S=sf\_of\_scale\_matrix\_GAMMA\*I). Its default is 1.
- prec\_epsilon: This is epsilon in the paper. It is the precision of mu\_alpha and all xi (scaling parameter in the scaled inverse Wishart distribution). Its default is also 1.
- add\_df\_to\_invWish: If P is the number of parameters or rather the size of the scale matrix used in the (scaled) inverse Wishart distribution then add\_df\_to\_invWish is the number of degrees of freedom that can be added to it. So DF = P + add\_df\_to\_invWish. The default for add\_df\_to\_invWish is 1, such that the correlations are uniformly distributed within [-1,1].

indices

Model selection indices. If set to TRUE the log-likelihood for each iteration and trial will be stored temporarily and with that the WAIC and LOO will be calculated via the loo package. If you want to have this log-likelihood matrix stored

in the output of this function, you can set save\_log\_lik to TRUE. The default for indices is FALSE.

save\_log\_lik If set to TRUE and indices = TRUE the log-likelihood matrix for each iteration

and trial will be saved in the output as a matrix. Its default is FALSE.

old\_label If set to TRUE the old labels of "subj" and "group" of the data will be used in the

elements of the output list. Default is FALSE.

#### Value

A list of the class rtmpt\_fit containing

• samples: the posterior samples as an mcmc.list object,

- diags: some diagnostics like deviance information criterion, posterior predictive checks for the frequencies and latencies, potential scale reduction factors, and also the 99% and 95% HDIs and medians for the group-level parameters,
- specs: some model specifications like the model, arguments of the model call, and information about the data transformation,
- indices (optional): if enabled, WAIC and LOO,
- LogLik (optional): if enabled, the log-likelihood matrix used for WAIC and LOO.
- summary includes posterior mean and median of the main parameters.

#### Author(s)

Raphael Hartmann

## References

Hartmann, R., Johannsen, L., & Klauer, K. C. (2020). rtmpt: An R package for fitting response-time extended multinomial processing tree models. *Behavior Research Methods*, 52(3), 1313–1338.

Hartmann, R., & Klauer, K. C. (2020). Extending RT-MPTs to enable equal process times. *Journal of Mathematical Psychology*, *96*, 102340.

Klauer, K. C. (2010). Hierarchical multinomial processing tree models: A latent-trait approach. *Psychometrika*, 75(1), 70-98.

Klauer, K. C., & Kellen, D. (2018). RT-MPTs: Process models for response-time distributions based on multinomial processing trees with applications to recognition memory. *Journal of Mathematical Psychology*, 82, 111-130.

Spiegelhalter, D. J., Best, N. G., Carlin, B. P., & Van Der Linde, A. (2002). Bayesian measures of model complexity and fit. *Journal of the royal statistical society: Series b (statistical methodology)*, 64(4), 583-639.

Vehtari, A., Gelman, A., & Gabry, J. (2017). Practical Bayesian model evaluation using leave-one-out cross-validation and WAIC. *Statistics and Computing*, 27(5), 1413-1432.

Watanabe, S. (2010). Asymptotic equivalence of Bayes cross validation and widely applicable information criterion in singular learning theory. *Journal of Machine Learning Research*, 11(Dec), 3571-3594.

## **Examples**

```
# Detect-Guess variant of the Two-High Threshold model.
# The encoding and motor execution times are assumed to be equal for each response.
mdl_2HTM <- "
# targets
do+(1-do)*g
(1-do)*(1-g)
# lures
(1-dn)*g
dn+(1-dn)*(1-g)
# do: detect old; dn: detect new; g: guess
model <- to_rtmpt_model(mdl_file = mdl_2HTM)</pre>
data_file <- system.file("extdata/data.txt", package="rtmpt")</pre>
data <- read.table(file = data_file, header = TRUE)</pre>
data_list <- to_rtmpt_data(raw_data = data, model = model)</pre>
# This might take some time
rtmpt_out <- fit_rtmpt(model = model, data = data_list, Rhat_max = 1.1)</pre>
rtmpt_out
# Type ?SimData for another working example.
```

fit\_rtmpt\_SBC

Simulation-based calibration for RT-MPT models

## Description

Simulate data from RT-MPT models using rtmpt\_model objects. The difference to sim\_rtmpt\_data is that here only scalars are allowed. This makes it usable for simulation-based calibration (SBC; Talts et al., 2018). You can specify the random seed, number of subjects, number of trials, and some parameters (same as prior\_params from fit\_rtmpt).

## Usage

```
fit_rtmpt_SBC(
  model,
  seed,
  n.eff_samples = 99,
  n.chains = 4,
  n.iter = 5000,
  n.burnin = 200,
```

```
n.thin = 1,
Rhat_max = 1.05,
Irep = 1000,
n.subj = 40,
n.trials = 30,
prior_params = NULL,
sim_list = NULL)
```

#### Arguments

model A list of the class rtmpt\_model.

seed Random seed number.

n.eff\_samples Number of effective samples. Default is 99, leading to 100 possible ranks (from

0 to 99).

n.chains Number of chains to use. Default is 4. Must be larger than 1 and smaller or

equal to 16.

n.iter Number of samples per chain. Default is 5000. Must be larger or equal to

n.eff\_samples.

n.burnin Number of warm-up samples. Default is 200.

n. thin Thinning factor. Default is 1.

Rhat\_max Maximal Potential scale reduction factor: A lower threshold that needs to be

reached before the actual sampling starts. Default is 1.05

Irep Every Irep samples an interim state with the current maximal potential scale

reduction factor is shown. Default is 1000. The following statements must hold

true for Irep:

• n.burnin is smaller than or equal to Irep,

• Irep is a multiple of n. thin and

• n.iter is a multiple of Irep / n.thin.

n. subj Number of subjects. Default is 40.

prior\_params

n. trials Number of trials per tree. Default is 30.

11. Cl 1a13 Rullioci of trials per tree. Default is 50

Named list of parameters from which the data will be generated. This must be the same named list as prior\_params from fit\_rtmpt and has the same defaults. It is not recommended to use the defaults since they lead to many probabilities close or equal to 0 and/or 1 and to RTs close or equal to 0. Allowed parameters are:

- mean\_of\_exp\_mu\_beta: This is the expected exponential rate (E(exp(beta)) = E(lambda)) and 1/mean\_of\_exp\_mu\_beta is the expected process time (1/E(exp(beta)) = E(tau)). The default mean is set to 10, such that the expected process time is 0.1 seconds.
- var\_of\_exp\_mu\_beta: The group-specific variance of the exponential rates.
   Since exp(mu\_beta) is Gamma distributed, the rate of the distribution is just mean divided by variance and the shape is the mean times the rate. The default is set to 100.

• mean\_of\_mu\_gamma: This is the expected *mean parameter* of the encoding and response execution times, which follow a normal distribution truncated from below at zero, so E(mu\_gamma) < E(gamma). The default is 0.

- var\_of\_mu\_gamma: The group-specific variance of the mean parameter. Its
  default is 10.
- mean\_of\_omega\_sqr: This is the expected residual variance (E(omega^2)).
   The default is 0.005.
- var\_of\_omega\_sqr: The variance of the residual variance (Var(omega^2)). The default is 0.01. The default of the mean and variance is equivalent to a shape and rate of 0.0025 and 0.5, respectivly.
- df\_of\_sigma\_sqr: degrees of freedom for the individual variance of the response executions. The individual variance follows a scaled inverse chisquared distribution with df\_of\_sigma\_sqr degrees of freedom and omega^2 as scale. 2 is the default and it should be an integer.
- sf\_of\_scale\_matrix\_SIGMA: The original scaling matrix (S) of the (scaled) inverse Wishart distribution for the process related parameters is an identity matrix S=I. sf\_of\_scale\_matrix\_SIGMA is a scaling factor, that scales this matrix (S=sf\_of\_scale\_matrix\_SIGMA\*I). Its default is 1.
- sf\_of\_scale\_matrix\_GAMMA: The original scaling matrix (S) of the (scaled) inverse Wishart distribution for the encoding and motor execution parameters is an identity matrix S=I. sf\_of\_scale\_matrix\_GAMMA is a scaling factor that scales this matrix (S=sf\_of\_scale\_matrix\_GAMMA\*I). Its default is 1.
- prec\_epsilon: This is epsilon in the paper. It is the precision of mu\_alpha and all xi (scaling parameter in the scaled inverse Wishart distribution). Its default is also 1.
- add\_df\_to\_invWish: If P is the number of parameters or rather the size
   of the scale matrix used in the (scaled) inverse Wishart distribution then
   add\_df\_to\_invWish is the number of degrees of freedom that can be added
   to it. So DF = P + add\_df\_to\_invWish. The default for add\_df\_to\_invWish
   is 1, such that the correlations are uniformly distributed within [-1,1].

sim\_list

Object of class rtmpt\_sim. This is also an output object. Can be used to re-fit the model if n.eff\_samples was not achieved in a previous fitting attempt. It will then use the data stored in this object. Default is NULL and this object will be created anew.

#### Value

A list of the class rtmpt\_sbc containing

- ranks: the rank statistic for all parameters,
- sim\_list: an object of the class rtmpt\_sim,
- fit\_list: an object of the class rtmpt\_fit,
- specs: some specifications like the model, seed number, etc.,

## Author(s)

Raphael Hartmann

## References

Talts, S., Betancourt, M., Simpson, D., Vehtari, A., & Gelman, A. (2018). Validating Bayesian inference algorithms with simulation-based calibration. *arXiv preprint arXiv:1804.06788*.

## **Examples**

}

```
# Detect-Guess variant of the Two-High Threshold model.
# The encoding and motor execution times are assumed to be different for each response.
mdl_2HTM <- "
# targets
d+(1-d)*g
           ; 0
(1-d)*(1-g); 1
# lures
(1-d)*g
         ; 0
d+(1-d)*(1-g); 1
# d: detect; g: guess
model <- to_rtmpt_model(mdl_file = mdl_2HTM)</pre>
params <- list(mean_of_exp_mu_beta = 10,</pre>
             var_of_exp_mu_beta = 10,
             mean_of_mu_gamma = 0.5,
             var_of_mu_gamma = 0.0025,
             mean_of_omega_sqr = 0.005,
             var_of_omega_sqr = 0.000025,
             df_of_sigma_sqr = 10,
             sf_of_scale_matrix_SIGMA = 0.1,
             sf_of_scale_matrix_GAMMA = 0.01,
             prec_epsilon = 10,
             add_df_{to_invWish} = 5)
R = 2 # typically 2000 with n.eff_samples = 99, but this will run many days
rank_mat <- matrix(NA, ncol = 393, nrow = 2)</pre>
for (r in 1:R) {
 SBC_out <- fit_rtmpt_SBC(model, seed = r*123, prior_params = params,</pre>
                       n.eff_samples = 99, n.thin = 5,
                       n.iter = 5000, n.burnin = 2000, Irep = 5000)
 rank_mat[r, ] <- SBC_out$ranks</pre>
```

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set\_params

Set constants for probability parameters and suppress process times in a rtmpt\_model list

## **Description**

By using parameter = "probs" you can specify which of the probability parameters should be set to a constant by using values between zero and one. If you use NA the probability will be estimated. By using parameter = "tau\_minus" or parameter = "tau\_plus" you can suppress process times/rates. Here 0 will suppress the named process and NA allows the process time/rate to be estimated.

## Usage

```
set_params(model, parameter, names, values = NA)
```

## **Arguments**

model

A list of the class rtmpt\_model.

parameter

Character of length one indicating the parameter to change. Allowed characters:

- "probs": probability parameters
- "tau\_minus": rate parameters of the exponential distribution of the process times that lead to a negative outcome
- "tau\_plus": rate parameters of the exponential distribution of the process times that lead to a positive outcome

names

Character vector with process names.

values

Numerical vector of length length(names). By using parameter = "probs" you have the following options

- NA: estimate the named probability
- 0 < values < 1: set the named probability to a constant value between zero and one

Example: set\_params(model = model, parameter = "probs", names = c("do", "dn", "g"), values = c(NA,NA,.5)) will set the guessing "old" (g) to the constant 0.5 in the 2HT model. By using parameter = "tau\_minus" or parameter = "tau\_plus" you have two options:

- NA: estimate the process time/rate
- 0: suppress the process time/rate

Example: set\_params(model = model, parameter = "tau\_minus", names = c("do", "dn", "g"), value = c(NA, NA, 0)) will suppress the process-completion time for guessing "new" in the 2HT model. This of course does not make sense here, but for some models it might be useful if you assume that a time-consuming process is not associated with certain process-outcome pairs (e.g., for technical parameters not corresponding to a psychological process).

set\_resps

## Value

A list of the class rtmpt\_model.

#### Author(s)

Raphael Hartmann

#### See Also

delta2delta

## **Examples**

```
# Detect-Guess variant of the Two-High Threshold model.
# The encoding and motor execution times are assumed to be equal for each category.
# The process completion times for both failed detections will be suppressed.
mdl_2HTM <- "
# targets
do+(1-do)*g
(1-do)*(1-g)
# lures
(1-dn)*g
dn+(1-dn)*(1-g)
# do: detect old; dn: detect new; g: guess
model <- to_rtmpt_model(mdl_file = mdl_2HTM)</pre>
## removing the process times for the failed detection ("tau_minus")
## of the detection parameters ("dn", "do")
model <- set_params(model = model, parameter = "tau_minus",</pre>
                names = c("dn", "do"), values = c(0,0))
```

set\_resps

Set responses in an rtmpt\_model

## **Description**

Change the responses for a tree and the categories within that tree.

## Usage

```
set_resps(model, tree, categories, values = 0)
```

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## **Arguments**

model A list of the class rtmpt\_model.

tree Character or numerical value of the tree for which the responses should be

changed.

categories Character or numerical vector identifying category/ies within the specified tree

for which the responses should be changed.

values Numerical vector of length length(categories) providing the responses. De-

fault is 0.

#### Value

A list of the class rtmpt\_model.

#### Author(s)

Raphael Hartmann

## See Also

set\_params

## **Examples**

```
# Detect-Guess variant of the Two-High Threshold model.
# The encoding and motor execution times will be set to different values
   for each response.
mdl_2HTM <- "
# targets
do+(1-do)*g
(1-do)*(1-g)
# lures
(1-dn)*g
dn+(1-dn)*(1-g)
# do: detect old; dn: detect new; g: guess
model <- to_rtmpt_model(mdl_file = mdl_2HTM)</pre>
## changing the model to have two different encoding and response execution
## times for "old" and "new" responses.
for(i in c(0,1)) model <- set_resps(model = model, tree = i,
                            categories = i*2+1, values = 1)
```

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SimData

Data simulated from the restricted 2HTM

## **Description**

Data set generated from a restricted Two-High Threshold model.

## Usage

SimData

## **Format**

```
A data frame with five variables:
subj subjects number
group group label of the subjects
tree condition of the current trial
cat observed response category
rt observed response time in ms
```

## **Details**

Fourty subjects with thirty trials per condition (Studied items, new Items) were simulated.

## **Examples**

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```
# this might take some time to run
rtmpt_out <- fit_rtmpt(model = model, data = data)
# convergence
## traceplot and summary of the first six parameters
coda::traceplot(rtmpt_out$samples[,1:6])
summary(rtmpt_out)</pre>
```

sim\_rtmpt\_data

Simulate data from RT-MPT models

## **Description**

Simulate data from RT-MPT models using rtmpt\_model objects. You can specify the random seed, number of subjects, number of trials per tree, and some parameters (mainly the same as prior\_params from fit\_rtmpt).

## Usage

```
sim_rtmpt_data(model, seed, n.subj, n.trials, params = NULL)
```

#### **Arguments**

model A list of the class rtmpt\_model.

seed Random seed number.

n.subj Number of subjects.

n.trials Number of trials per tree.

params

Named list of parameters from which the data will be generated. This must be the same named list as prior\_params from fit\_rtmpt, except for "mean\_of\_mu\_alpha" and "var\_of\_mu\_alpha", and has the same defaults. The difference to prior\_params is, that vectors are allowed, but must match the length of the parameters in the model. It is not recommended to use the defaults since they lead to many probabilities close or equal to 0 and/or 1 and to RTs close or equal to 0. Allowed parameters are:

- mean\_of\_mu\_alpha: Probit transformed mean probability. If you want to have a group-level mean probability of 0.6, use mean\_of\_mu\_alpha = qnorm(0.6) in the params list. Default is 0 or qnorm(.5).
- var\_of\_mu\_alpha: Variance of the probit transformed group-level mean probability. If specified, mu\_alpha will be sampled from N(mean\_of\_mu\_alpha, var\_of\_mu\_alpha). If not, mu\_alpha = mean\_of\_mu\_alpha.
- mean\_of\_exp\_mu\_beta: This is the expected exponential rate (E(exp(beta)) = E(lambda)) and 1/mean\_of\_exp\_mu\_beta is the expected process time (1/E(exp(beta)) = E(tau)). The default mean is set to 10, such that the expected process time is 0.1 seconds. For a mean process time of 200 ms, wirte mean\_of\_exp\_mu\_beta = 1000/200.

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var\_of\_exp\_mu\_beta: The group-specific variance of the exponential rates.
 Since exp(mu\_beta) is Gamma distributed, the rate of the distribution is just mean divided by variance and the shape is the mean times the rate. If specified, exp(mu\_beta) is sampled from Gammashape = mean\_of\_exp\_mu\_beta^2/var\_of\_exp\_m = mean\_of\_exp\_mu\_beta/var\_of\_exp\_mu\_beta). If not, mu\_alpha = mean\_of\_exp\_mu\_beta.

- mean\_of\_mu\_gamma: This is the expected *mean parameter* of the encoding and response execution times, which follow a normal distribution truncated from below at zero, so E(mu\_gamma) < E(gamma). The default is 0. For a mean motor time of 550 ms write mean\_of\_mu\_gamma = 550/1000.
- var\_of\_mu\_gamma: The group-specific variance of the *mean parameter*. If specified, mu\_gamma is sampled from N(mean\_of\_mu\_gamma, var\_of\_mu\_gamma). If not, mu\_gamma = mean\_of\_mu\_gamma.
- mean\_of\_omega\_sqr: This is the expected residual variance (E(omega^2)).
   The default is 0.005.
- var\_of\_omega\_sqr: The variance of the residual variance (Var(omega^2)).
   If specified, omega\_sqr is sampled from GAMMA(shape = mean\_of\_omega\_sqr^2/var\_of\_omega\_ = mean\_of\_omega\_sqr/var\_of\_omega\_sqr).
   If not, omega\_sqr = mean\_of\_omega\_sqr.
   0.01. The default of the mean and variance is equivalent to a shape and rate of 0.0025 and 0.5, respectivly.
- df\_of\_sigma\_sqr: Degrees of freedom for the individual variance of the response executions. The individual variance follows a scaled inverse chisquared distribution with df\_of\_sigma\_sqr degrees of freedom and omega^2 as scale. 2 is the default and it should be an integer.
- sf\_of\_scale\_matrix\_SIGMA: The original scaling matrix (S) of the (scaled) inverse Wishart distribution for the process related parameters is an identity matrix S=I. sf\_of\_scale\_matrix\_SIGMA is a scaling factor, that scales this matrix (S=sf\_of\_scale\_matrix\_SIGMA\*I). Its default is 1.
- sf\_of\_scale\_matrix\_GAMMA: The original scaling matrix (S) of the (scaled) inverse Wishart distribution for the encoding and motor execution parameters is an identity matrix S=I. sf\_of\_scale\_matrix\_GAMMA is a scaling factor that scales this matrix (S=sf\_of\_scale\_matrix\_GAMMA\*I). Its default is 1.
- prec\_epsilon: This is epsilon in the paper. It is the precision of xi (scaling parameter in the scaled inverse Wishart distribution). Its default is also 1.
- add\_df\_to\_invWish: If P is the number of parameters or rather the size of the scale matrix used in the (scaled) inverse Wishart distribution then add\_df\_to\_invWish is the number of degrees of freedom that can be added to it. So DF = P + add\_df\_to\_invWish. The default for add\_df\_to\_invWish is 1, such that the correlations are uniformly distributed within [-1,1].
- SIGMA: Variance-covariance matrix of the process-related parameters. It must match the number of process-related parameters to be estimated. If scalars or vectors are given, they will be transformed into diagonal matrices using diag(SIGMA). If not specified it will be randomly generated using diag(xi)%\*%rinvwishart(nu,S)%\*%diag(xi), where nu is the number of process-related group-level parameters to be estimated plus add\_df\_to\_invWish, S is the identity matrix multiplied by sf\_of\_scale\_matrix\_SIGMA, and xi (randomly generated from N(1,1/prec\_epsilon)) are the scaling factors

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for the scaled inverse wishart distribution. If SIGMA is used, sf\_of\_scale\_matrix\_SIGMA and add\_df\_to\_invWish will be ignored for the process-related parameters.

• GAMMA: Variance-covariance matrix of the motor time parameters. It must match the number of motor time parameters to be estimated. If scalars or vectors are given, they will be transformed into diagonal matrices using diag(SIGMA). If not specified it will be randomly generated using diag(xi)%\*%rinvwishart(nu,S) where nu is the number of motor time group-level parameters to be estimated plus add\_df\_to\_invWish, S is the identity matrix multiplied by sf\_of\_scale\_matrix\_GAMMA, and xi (randomly generated from N(1,1/prec\_epsilon)) are the scaling factors for the scaled inverse wishart distribution. If GAMMA is used, sf\_of\_scale\_matrix\_GAMMA and add\_df\_to\_invWish will be ignored for the motor time parameters.

#### Value

A list of the class rtmpt\_sim containing

- data: the data.frame with the simulated data,
- gen\_list: a list containing lists of the group-level and subject-specific parameters for the
  process-related parameters and the motor-related parameters, and the trial-specific probabilities, process-times, and motor-times,
- specs: some specifications like the model, seed number, etc.,

#### Author(s)

Raphael Hartmann

## **Examples**

```
params <- list(mean_of_mu_alpha = 0,</pre>
               #var_of_mu_alpha = 1
               mean_of_exp_mu_beta = 10,
               var_of_exp_mu_beta = 10,
               mean_of_mu_gamma = 0.5,
               var_of_mu_gamma = 0.0025,
               mean_of_omega_sqr = 0.005,
               var_of_omega_sqr = 0.000025,
               df_of_sigma_sqr = 10,
               sf_of_scale_matrix_SIGMA = 0.1,
               sf_of_scale_matrix_GAMMA = 0.01,
               prec_epsilon = 10,
               add_df_{to_invWish} = 5)
sim_dat <- sim_rtmpt_data(model, seed = 123, n.subj = 40, n.trials = 30, params = params)</pre>
# fixed group-level parameters
params <- list(mean_of_mu_alpha = 0,</pre>
               mean_of_exp_mu_beta = 10,
               mean_of_mu_gamma = 0.5,
               mean_of_omega_sqr = 0.005,
               df_of_sigma_sqr = 10,
               sf_of_scale_matrix_SIGMA = 0.1,
               sf_of_scale_matrix_GAMMA = 0.01,
               prec_epsilon = 10,
               add_df_to_invWish = 5,
               SIGMA = diag(9), # independent process-related params
               GAMMA = diag(2)) # independent motor time params
sim_dat <- sim_rtmpt_data(model, seed = 123, n.subj = 40, n.trials = 30, params = params)</pre>
```

sim\_rtmpt\_data\_SBC

Simulate data from an RT-MPT model

## **Description**

Simulate data from RT-MPT models using rtmpt\_model objects. The difference to sim\_rtmpt\_data is that here only scalars are allowed. This makes it usable for simulation-based calibration (SBC; Talts et al., 2018). You can specify the random seed, number of subjects, number of trials, and some parameters (same as prior\_params from fit\_rtmpt).

## Usage

```
sim_rtmpt_data_SBC(model, seed, n.subj, n.trials, params = NULL)
```

## **Arguments**

model

A list of the class rtmpt\_model.

seed

Random seed number.

n.subj

<- Number of subjects.

n.trials

<- Number of trials per tree.

params

Named list of parameters from which the data will be generated. This must be the same named list as prior\_params from fit\_rtmpt and has the same defaults. It is not recommended to use the defaults since they lead to many probabilities close or equal to 0 and/or 1 and to RTs close or equal to 0. Allowed parameters are:

- mean\_of\_exp\_mu\_beta: This is the expected exponential rate (E(exp(beta)) = E(lambda)) and 1/mean\_of\_exp\_mu\_beta is the expected process time (1/E(exp(beta)) = E(tau)). The default mean is set to 10, such that the expected process time is 0.1 seconds.
- var\_of\_exp\_mu\_beta: The group-specific variance of the exponential rates. Since exp(mu\_beta) is Gamma distributed, the rate of the distribution is just mean divided by variance and the shape is the mean times the rate. The default is set to 100.
- mean\_of\_mu\_gamma: This is the expected *mean parameter* of the encoding and response execution times, which follow a normal distribution truncated from below at zero, so E(mu\_gamma) < E(gamma). The default is 0.
- var\_of\_mu\_gamma: The group-specific variance of the mean parameter. Its
  default is 10.
- mean\_of\_omega\_sqr: This is the expected residual variance (E(omega^2)).
   The default is 0.005.
- var\_of\_omega\_sqr: The variance of the residual variance (Var(omega^2)). The default is 0.01. The default of the mean and variance is equivalent to a shape and rate of 0.0025 and 0.5, respectivly.
- df\_of\_sigma\_sqr: degrees of freedom for the individual variance of the response executions. The individual variance follows a scaled inverse chisquared distribution with df\_of\_sigma\_sqr degrees of freedom and omega^2 as scale. 2 is the default and it should be an integer.
- sf\_of\_scale\_matrix\_SIGMA: The original scaling matrix (S) of the (scaled) inverse Wishart distribution for the process related parameters is an identity matrix S=I. sf\_of\_scale\_matrix\_SIGMA is a scaling factor, that scales this matrix (S=sf\_of\_scale\_matrix\_SIGMA\*I). Its default is 1.
- sf\_of\_scale\_matrix\_GAMMA: The original scaling matrix (S) of the (scaled) inverse Wishart distribution for the encoding and motor execution parameters is an identity matrix S=I. sf\_of\_scale\_matrix\_GAMMA is a scaling factor that scales this matrix (S=sf\_of\_scale\_matrix\_GAMMA\*I). Its default is 1.
- prec\_epsilon: This is epsilon in the paper. It is the precision of mu\_alpha and all xi (scaling parameter in the scaled inverse Wishart distribution). Its default is also 1.
- add\_df\_to\_invWish: If P is the number of parameters or rather the size of the scale matrix used in the (scaled) inverse Wishart distribution then add\_df\_to\_invWish is the number of degrees of freedom that can be added to it. So DF = P + add\_df\_to\_invWish. The default for add\_df\_to\_invWish is 1, such that the correlations are uniformly distributed within [-1,1].

#### Value

A list of the class rtmpt\_sim containing

- data: the data.frame with the simulated data,
- gen\_list: a list containing lists of the group-level and subject-specific parameters for the
  process-related parameters and the motor-related parameters, and the trial-specific probabilities, process-times, and motor-times,
- specs: some specifications like the model, seed number, etc.,

#### Author(s)

Raphael Hartmann

#### References

Talts, S., Betancourt, M., Simpson, D., Vehtari, A., & Gelman, A. (2018). Validating Bayesian inference algorithms with simulation-based calibration. *arXiv preprint arXiv:1804.06788*.

## **Examples**

```
mdl_2HTM <- "
# targets
do+(1-do)*g
(1-do)*(1-g)
                ; 1
# lures
(1-dn)*g
dn+(1-dn)*(1-g); 1
# do: detect old; dn: detect new; g: guess
model <- to_rtmpt_model(mdl_file = mdl_2HTM)</pre>
params <- list(mean_of_exp_mu_beta = 10,</pre>
               var_of_exp_mu_beta = 10,
               mean_of_mu_gamma = 0.5,
               var_of_mu_gamma = 0.0025,
               mean_of_omega_sqr = 0.005,
               var_of_omega_sqr = 0.000025,
               df_of_sigma_sqr = 10,
               sf_of_scale_matrix_SIGMA = 0.1,
               sf_of_scale_matrix_GAMMA = 0.01,
               prec_epsilon = 10,
               add_df_to_invWish = 5)
```

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tau2tau

Set process completion times equal

## Description

Setting multiple process completion times (taus) equal. This means all process times of negative outcomes will be set equal and all process times of positive outcomes will be set equal. Only two process times (one for the negative and one for the positive outcome) of the named processes will be estimated. The equality can be removed by just naming only one process name.

## Usage

```
tau2tau(model, names, keep_zeros = FALSE)
set_taus_equal(model, names, keep_zeros = FALSE)
```

#### Arguments

model

A list of the class rtmpt\_model.

names

Character vector giving the names of the processes for which the process completion times should be equal. If length(names) = 1 then the corresponding process completion times (for negative and positive outcomes) will be estimates (i.e., they will be set to NA)

keep\_zeros

Can be one of the following

- logical value: FALSE (default) means none of the zeros for names in the model will be kept; The times of the reference process (i.e., first of names in alphabetical order) will be set to NA (i.e., will be estimated) and the others will be set to the name of the reference process (i.e., will be set to equal the reference process times). TRUE means the zero(s) of the reference process times (if specified) is used for the same outcome of all other processes.
- numeric value: index for names. If 1, the zero(s) of the first process in names (in original order defined by the user) is used for the same outcome of all other processes in names. If 2, the zero(s) of the second process is used. And so on.

## Value

A list of the class rtmpt\_model.

#### Note

If you use theta2theta() and tau2tau() with the same process names you might just change the EQN or MDL file accordingly by using the same process name for all processes which should have equal process times and probabilities.

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## Author(s)

Raphael Hartmann

## See Also

delta2delta, theta2const, tau2zero and theta2theta

## **Examples**

```
# Detect-Guess variant of the Two-High Threshold model.
# The encoding and motor execution times are assumed to be equal for each category.
# The process completion times for both detection processes ("do" and "dn") will be
mdl_2HTM <- "
# targets
do+(1-do)*g
(1-do)*(1-g)
# lures
(1-dn)*g
dn+(1-dn)*(1-g)
# do: detect old; dn: detect new; g: guess
model <- to_rtmpt_model(mdl_file = mdl_2HTM)</pre>
## make do = dn
new_model <- tau2tau(model = model, names = c("do", "dn"))</pre>
new_model
## make do = dn
new_model <- set_taus_equal(model = model, names = c("do", "dn"))</pre>
new_model
```

tau2zero

Set process completion times to zero

## **Description**

Setting process completion times (taus) to zero or change it back to be estimated.

## Usage

```
tau2zero(model, names, outcomes, values = 0)
set_tau_zero(model, names, outcomes, values = 0)
```

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## **Arguments**

values

model A list of the class rtmpt\_model.

names Character vector with process names.

outcomes Character vector of length length(names) indicating for which process out-

come the process completion time should be zero or changed back to be esti-

mated. Allowed characters are:

• "minus": the negative outcome of the process.

• "plus": the positive outcome of the process.

Numerical vector of length one or length(names). You have the following options for the elements of the numeric vector:

• 0: suppress the process time/rate, i.e., set the process completion time (tau) with the specified output to zero.

• NA: estimate the process time (tau)

## Value

A list of the class rtmpt\_model.

#### Author(s)

Raphael Hartmann

## See Also

delta2delta, theta2const, theta2theta and tau2tau

## **Examples**

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theta2const

Set process probabilities to constants

## Description

Setting process probabilities (thetas) to constants or change it back to be estimated.

## Usage

```
theta2const(model, names, constants = NA)
set_theta_const(model, names, constants = NA)
```

## Arguments

model An object of the class rtmpt\_model.

Character vector with process names.

constants Numerical vector of length one or length(names). You have the following

options for the elements of the numeric vector:

- 0 < constants < 1: set the named probability to a constant value between zero and one
- NA: estimate the named probability

#### Value

An object of the class rtmpt\_model.

## Author(s)

Raphael Hartmann

#### See Also

delta2delta, tau2zero, theta2theta and tau2tau

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## **Examples**

```
# Detect-Guess variant of the Two-High Threshold model.
# The encoding and motor execution times are assumed to be equal for each category.
\# The process probability for guessing (g) will be set to 0.5.
mdl_2HTM <- "
# targets
do+(1-do)*g
(1-do)*(1-g)
# lures
(1-dn)*g
dn+(1-dn)*(1-g)
# do: detect old; dn: detect new; g: guess
model <- to_rtmpt_model(mdl_file = mdl_2HTM)</pre>
## setting g to a constant (0.5):
new_model < -theta2const(model = model, names = c("g"), constants = c(0.5))
new_model
## setting g to a constant (0.5):
new_model < -set_theta_const(model = model, names = c("g"), constants = c(0.5))
new_model
```

theta2theta

Set process probabilities equal

## **Description**

Setting multiple process probabilities (thetas) equal. One of the process probabilities will be estimated and the other named process(es) will be set to equal the former. The equality can be removed by only using one name of a process.

## Usage

```
theta2theta(model, names, keep_consts = FALSE)
set_thetas_equal(model, names, keep_consts = FALSE)
```

## **Arguments**

model

A list of the class rtmpt\_model.

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names

Character vector giving the names of the processes for which the process probabilities should be equal. If length(names) = 1 then the corresponding process probability will be estimates (i.e., it will be set to NA)

keep\_consts

Can be one of the following

- logical value: FALSE (default) means none of the constants for names in the model will be kept; The probability of the reference process (i.e., first of names in alphabetical order) will be set to NA (i.e., will be estimated) and the others will be set to the name of the reference process (i.e., will be set to equal the reference process probability). TRUE means the constant of the reference process probability (if specified) is used for all other processes.
- numeric value: index for names. If 1, the constant of the first process in names (in original order defined by the user) is used for all other probabilities of the processes in names. If 2, the constant of the second process is used. And so on.

#### Value

A list of the class rtmpt\_model.

#### Note

If you use theta2theta() and tau2tau() with the same process names you might just change the EQN or MDL file accordingly by using the same process name for all processes which should have equal process times and probabilities.

## Author(s)

Raphael Hartmann

## See Also

delta2delta, theta2const, tau2zero and tau2tau

## **Examples**

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```
# do: detect old; dn: detect new; g: guess
"
model <- to_rtmpt_model(mdl_file = mdl_2HTM)
## make do = dn
new_model <- theta2theta(model = model, names = c("do", "dn"))
new_model
## make do = dn
new_model <- set_thetas_equal(model = model, names = c("do", "dn"))
new_model</pre>
```

to\_rtmpt\_data

Transform data to be used in RT-MPT model fitting

## **Description**

Transform data, such that it can be used in fit\_rtmpt. This implies changing each value/label in "subj", "group", "tree", and "cat" to numbers such that it starts from zero (e.g. data\$tree = c(1,1,3,3,2,2,...) will be changed to data\$tree = c(0,0,2,2,1,1,...)) and the columns will be ordered in the right way. "rt" must be provided in milliseconds. If it has decimal places it will be rounded to a whole number. fit\_rtmpt will automatically call this function if its input is not already an rtmpt\_data list, but it is advised to use it anyway because it provides information about the transformations of the data.

## Usage

```
to_rtmpt_data(raw_data, model)
```

## **Arguments**

raw\_data data.frame or path to data containing columns "subj", "group", "tree", "cat",

and "rt". If not provided in this order it will be reordered and unused variables

and it. If not provided in this order it will be reordered and unused

will be moved to the end of the new data frame.

model A list of the class rtmpt\_model.

#### Value

A list of the class rtmpt\_data containing transformed data and information about the transformation that has been done.

## Author(s)

Raphael Hartmann

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## **Examples**

```
# Detect-Guess variant of the Two-High Threshold model.
# The encoding and motor execution times are assumed to be equal for each response.
eqn_2HTM <- "
# CORE MPT EQN
# tree ; cat ; mpt
target ; hit ; do
target; hit; (1-do)*g
target; miss; (1-do)*(1-g)
 lure ; f_a ; (1-dn)*g
 lure ; c_r ; dn
 lure; c_r; (1-dn)*(1-g)
model <- to_rtmpt_model(eqn_file = eqn_2HTM)</pre>
data_file <- system.file("extdata/labeled_data.txt", package="rtmpt")</pre>
data <- read.table(file = data_file, header = TRUE)</pre>
data_list <- to_rtmpt_data(raw_data = data, model = model)</pre>
data_list
```

to\_rtmpt\_model

Create a model list to fit an RT-MPT

## Description

Create a model list of the class rtmpt\_model by providing either eqn\_file or mdl\_file. If both are provided mdl\_file will be used.

#### Usage

```
to_rtmpt_model(eqn_file = NULL, mdl_file = NULL)
```

## **Arguments**

egn\_file

Character string as shown in example 2 or path to the text file that specifies the (RT-)MPT model with standard .eqn syntax (Heck et al., 2018; Hu, 1999). E.g. studied; hit; (1-do)\*g for a correct guess in the detect-guess 2HT model.

mdl\_file

Character string as shown in example 1 or path to the text file that specifies the (RT-)MPT model and gives on each line the equation of one category using + to separate branches and \* to separate processes (Singmann and Kellen, 2013). E.g. do+(1-do)\*g for the category "hit" in the detect-guess 2HT model.

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#### Value

A list of the class rtmpt\_model.

#### Note

Within a branch of a (RT-)MPT model it is not allowed to have the same process two or more times.

#### Author(s)

Raphael Hartmann

#### References

Heck, D. W., Arnold, N. R., & Arnold, D. (2018). TreeBUGS: An R package for hierarchical multinomial-processing-tree modeling. *Behavior Research Methods*, 50(1), 264-284.

Hu, X. (1999). Multinomial processing tree models: An implementation. *Behavior Research Methods, Instruments, & Computers, 31(4)*, 689-695.

Singmann, H., & Kellen, D. (2013). MPTinR: Analysis of multinomial processing tree models in R. Behavior Research Methods, 45(2), 560-575.

#### See Also

delta2delta, theta2const, tau2zero, theta2theta, and tau2tau for functions to change the model

## **Examples**

```
# Detect-Guess variant of the Two-High Threshold model
  with constant guessing and
  suppressed process completion times for both failed detections.
# The encoding and motor execution times are assumed to be different for each response.
## 1. using the mdl syntax
mdl_2HTM <- "
# targets
do+(1-do)*g
           ; 0
(1-do)*(1-g)
           ; 1
# lures
(1-dn)*g
dn+(1-dn)*(1-g); 1
# do: detect old; dn: detect new; g: guess
# OPTIONAL MPT CONSTRAINTS
# set probabilities to constants:
const_prob: g=0.5
```

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```
# suppress process times:
suppress_process: dn-, do-
model <- to_rtmpt_model(mdl_file = mdl_2HTM)</pre>
model
## 2. using the eqn syntax
eqn_2HTM <- "
# CORE MPT EQN
# tree ; cat ; mpt
    0; 0; do
    0; 0; (1-do)*g
0; 1; (1-do)*(1-g)
    1; 2; (1-dn)*g
    1; 3; dn
    1; 3; (1-dn)*(1-g)
# OPTIONAL MPT CONSTRAINTS
# set probabilities to constants:
const_prob: g=0.5
# suppress process times:
suppress_process: dn-, do-
# tree; cat; MAP
resp: 0; 0; 0
resp: 0; 1; 1
resp: 1; 2; 0
      1; 3; 1
resp:
# different motor execution times for old and new responses.
model <- to_rtmpt_model(eqn_file = eqn_2HTM)</pre>
model
```

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