# Package 'stagedtrees' 

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Type Package
Title Staged Event Trees

## Version 2.2.1

Description Creates and fits staged event tree probability models, which are probabilistic graphical models capable of representing asymmetric conditional independence statements for categorical variables.
Includes functions to create, plot and fit staged
event trees from data, as well as many efficient structure
learning algorithms.
References:
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Barclay L. M., Hutton J. L. and Smith J. Q. (2013)
[doi:10.1016/j.ijar.2013.05.006](doi:10.1016/j.ijar.2013.05.006).
Smith J. Q. and Anderson P. E. (2008)
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## $R$ topics documented:

as.character.parentslist ..... 3
Asym ..... 4
as_adj_matrix ..... 4
as_bn ..... 5
as_parentslist ..... 5
as_sevt. ..... 6
barplot.sevt ..... 8
ceg ..... 9
ceg2adjmat ..... 9
cid ..... 10
compare_stages ..... 11
confint.sevt ..... 13
full_indep ..... 14
generate_linear_dataset ..... 16
generate_random_dataset ..... 17
generate_xor_dataset ..... 17
get_stage ..... 18
inclusions_stages ..... 19
join_stages ..... 19
join_unobserved ..... 20
logLik.sevt ..... 21
Ir_test ..... 22
PhDArticles ..... 23
plot.ceg ..... 24
plot.sevt ..... 25
Pokemon ..... 27
predict.sevt ..... 28
print.sevt ..... 29
prob ..... 30
rename_stage ..... 31
sample_from ..... 32
search_best ..... 32
search_greedy ..... 33
sevt ..... 34
sevt_add ..... 36
sevt_fit ..... 37
stagedtrees ..... 38
stages ..... 39
stages_bhc ..... 40
stages_bhcr ..... 41
stages_bj ..... 42
stages_fbhc ..... 43
stages_hc ..... 44
stages_hclust ..... 45
stages_kmeans ..... 46
stndnaming ..... 47
subtree ..... 48
summary.sevt ..... 49
text.sevt ..... 49
Index ..... 51

```
as.character.parentslist
    Print a parentslist object
```


## Description

Nice print of a parentslist object

## Usage

\#\# S3 method for class 'parentslist'
as.character (x, only_parents = FALSE, ...)
\#\# S3 method for class 'parentslist'
print(x, ...)

## Arguments

$x \quad$ an object of class parentslist.
only_parents logical, if the basic DAG encoding is to be returned.
... additional arguments for compatibility.

## Value

as.character. parentslist returns a string encoding the associated directed graph and eventually the context specific independences. The encoding is similar to the one returned by modelstring in package bnlearn and package deal. In particular, parents of a variable can be enclosed in:

- ( ) if a partial (conditional) independence is present.
- \{ \} if a context specific independence is present.
- <> if no context specific and partial (conditional) independences are present, but at least a local independence is detected.

If a parent is not enclosed in parenthesis the dependence is full.
If only_parents = TRUE, the simple DAG encoding as in bnlearn is returned.

## Examples

```
    model <- stages_hclust(full(Titanic), k = 2)
    pl <- as_parentslist(model)
    pl
    as.character(pl)
    as.character(pl, only_parents = TRUE)
```

    Asym
    Asym dataset
    
## Description

Artificial dataset with observations from four variables having a non-symmetrical conditional independence structure.

## Usage

Asym

## Format

A data frame with 1000 observations of 4 binary variables.

## Source

The data has been generated by Federico Carli <carli@dima. unige>.
as_adj_matrix Convert to an adjacency matrix

## Description

Convert to an adjacency matrix

## Usage

as_adj_matrix(x)
\#\# S3 method for class 'parentslist'
as_adj_matrix(x)

## Arguments

x
an R object

## Value

the equivalent adjacency matrix
as_bn Convert to a bnlearn object

## Description

Convert a staged tree object into an object of class bn from the bnlearn package.

## Usage

as_bn(x)
\#\# S3 method for class 'parentslist'
as_bn(x)
\#\# S3 method for class 'sevt'
as_bn(x)

## Arguments

x
an R object of class sevt or parentslist.

## Value

an object of class bn from package bnlearn.

```
as_parentslist Obtain the equivalent DAG as list of parents
```


## Description

Convert to the equivalent representation as list of parents.

## Usage

```
as_parentslist(x, ...)
## S3 method for class 'bn'
as_parentslist(x, order = NULL, ...)
## S3 method for class 'bn.fit'
as_parentslist(x, order = NULL, ...)
## S3 method for class 'sevt'
as_parentslist(x, ...)
```


## Arguments

x
... additional parameters.
order
an R object.
order of the variables, usually a topological order.

## Details

The output of this function is an object of class parentslist which is one of the possible encoding for a directed graph. This is mainly an internal class and its specification can be changed in the future. For example, now it may also include information on the sample space of the variables and the context/partial/local independences.
In as_parentslist.sevt, if a context-specific or a local-partial independence is detected a message is printed and the minimal super-model is returned.

## Value

An object of class parentslist for which a print method exists. Basically a list with one entries for each variable with fields:

- parents The parents of the variable.
- context Where context independences are detected.
- partial Where partial independences are detected.
- local Where no context/partial independences are detected, but local independences are present.
- values values for the variable.


## See Also

print. parentslist and as.character. parentslist for the parenthesis-encoding of the DAG structure and the asymmetric independences.

## Examples

```
model <- stages_hclust(full(Titanic), k = 2)
pl <- as_parentslist(model)
pl$Age
```

```
as_sevt
```

Coerce to sevt

## Description

Convert to an equivalent object of class sevt.

## Usage

```
as_sevt(x, ...)
## S3 method for class 'bn.fit'
as_sevt(x, order = NULL, ...)
## S3 method for class 'bn'
as_sevt(x, order = NULL, values = NULL, ...)
## S3 method for class 'parentslist'
as_sevt(x, order = NULL, values = NULL, ...)
```


## Arguments

$x \quad$ an R object.
... additional parameters to be used by specific methods.
order order of the variables.
values the values for each variable, the sample space.

## Details

In as_sevt.bn.fit the order argument, if provided, must be a topological order of the bn.fit object (no check is performed). If the order is not provided a topological order will be used (the one returned by bnlearn: : node. ordering).

In as_sevt.parentslist the order argument, if provided, must be a topological order of the corresponding DAG (no check is performed). If the order is not provided names $(x)$ is used.

The values parameter is used to specify the sample space of each variable. For a parentslist object created with as_parentslist from an object of class sevt, it is, usually, not needed to specify the values parameter, since the sample space is saved in the parentslist object.

## Value

the equivalent object of class sevt.

## Examples

```
model <- stages_hclust(full(Titanic), k = 2)
plot(model)
pl <- as_parentslist(model)
model2 <- as_sevt(pl)
plot(model2) ## this is a super-model of the first staged tree
## we can check it with
inclusions_stages(model, model2)
```


## Description

Create a bar plot visualizing probabilities associated to the different stages of a variable in a staged event tree.

## Usage

```
## S3 method for class 'sevt'
barplot(
        height,
        var,
        ignore = height$name_unobserved,
        beside = TRUE,
        horiz = FALSE,
        legend.text = FALSE,
        col = NULL,
        xlab = ifelse(horiz, "probability", NA),
        ylab = ifelse(!horiz, "probability", NA),
    )
```


## Arguments

height an object of class sevt.
var name of a variable in object.
ignore vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in object\$name_unobserved.
beside a logical value. See barplot.
horiz a logical value. See barplot.
legend.text logical.
col color mapping for the stages, see col argument in plot. sevt.
$x l a b \quad a \quad$ label for the x axis.
$y l a b \quad a \quad$ label for the $y$ axis.
... additional arguments passed to barplot.

## Value

As barplot: A numeric vector (or matrix, when beside = TRUE), giving the coordinates of all the bar midpoints drawn, useful for adding to the graph.

## Examples

```
model <- stages_fbhc(full(PhDArticles, lambda = 1))
```

    barplot(model, "Kids", beside = TRUE)
    ceg Chain event graph (CEG)
    
## Description

Build the CEG representation from an object of class sevt.

## Usage

ceg(object)

## Arguments

object an object of class sevt.

## Details

An object of class ceg is a staged event tree object with additional information on the positions.

## Value

an object of class ceg.

## Examples

DD <- generate_xor_dataset(3, 100)
model <- stages_bhc(full(DD))
model.ceg <- ceg(model)
model.ceg\$positions

Ceg to adjmat of graph

## Description

Obtain the adjacency matrix corresponding to a CEG.

## Usage

ceg2adjmat(x)

## Arguments

x an object of class ceg.

## Details

This utility function can be used to prepare the adjacency matrix to plot the CEG using a graph package (e.g. igraph).

## Value

the adj matrix

## Examples

model <- stages_fbhc(full(PhDArticles))
model.ceg <- ceg(model)
ceg2adjmat(model.ceg)
cid Context specific interventional discrepancy

## Description

Compute the context specific interventional discrepeancy of a staged tree with respect to a reference staged tree.

## Usage

cid(object1, object2, FUN = mean)

## Arguments

object1 an object of class sevt.
object2 an object of class sevt.
FUN a function that is used to aggregate CID for each variable. The default mean will obtain the CID as defined in Leonelli and Varando (2021).

## Value

A list with components:

- wrong a stages-like structure which record where object2 wrongly infer the interventional distance with respect to object1.
- cid the value of the computed CID.


## References

Leonelli M., Varando G. Context-Specific Causal Discovery for Categorical Data Using Staged Trees https://arxiv.org/abs/2106.04416

## Examples

```
model1 <- stages_bhc(full(Titanic))
model2 <- stages_bhc(full(Titanic,
order = c("Survived", "Sex", "Age", "Class")))
cid(model1, model2)$cid
cid(model1, model2)$wrong
```

compare_stages Compare two staged event tree

## Description

Compare two staged event trees, return the differences of the stages structure and plot the difference tree. Three different methods to compute the difference tree are available (see Details).

## Usage

```
compare_stages(
    object1,
    object2,
    method = "naive",
    return_tree = FALSE,
    plot = FALSE,
    ..
)
hamming_stages(object1, object2, return_tree = FALSE)
diff_stages(object1, object2)
```


## Arguments

| object1 | an object of class sevt. |
| :--- | :--- |
| object2 | an object of class sevt. |
| method | character, method to compare staged event trees. One of: "naive", "hamming" <br> or "stages". |
| return_tree | logical, if TRUE the difference tree is returned. <br> plot |
| $\ldots$ | logical. |
| $\ldots$ | additional parameters to be passed to plot. sevt. |

## Details

compare_stages tests if the stage structure of two sevt objects is the same. Three methods are available:

- naive first applies stndnaming to both objects and then simply compares the resulting stage names.
- hamming uses the hamming_stages function that finds a minimal subset of nodes which stages must be changed to obtain the same structure.
- stages uses the diff_stages function that compares stages to check whether the same stage structure is present in both models.

Setting return_tree $=$ TRUE will return the stages difference obtained with the selected method. The stages difference is a list of numerical vectors with same lengths and structure as stages (object1) or stages(object2), where values are 1 if the corresponding node has different (with respect to the selected method) associated stage, and 0 otherwise.

With plot = TRUE the plot of the difference tree is displayed.
If return_tree $=$ FALSE and plot $=$ FALSE the logical output is the same for the three methods and thus the naive method should be used since it is computationally faster.
hamming_stages finds a minimal set of nodes for which the associated stages should be changed to obtain equivalent structures. To do that, a maximum-weight bipartite matching problem between the stages of the two staged trees is solved using the Hungarian method implemented in the solve_LSAP function of the clue package. hamming_stages requires the package clue.

## Value

compare_stages: if return_tree = FALSE, logical: TRUE if the two models are exactly equal, otherwise FALSE. Else if return_tree = TRUE, the differences between the two trees, according to the selected method.
hamming_stages: if return_tree = FALSE, integer, the minimum number of situations where the stage should be changed to obtain the same models. If return_tree $=$ TRUE a stages-like structure showing which situations should be modified to obtain the same models.
diff_stages: a stages-like structure marking the situations belonging to stages which are not the exactly equal.

## Examples

```
data("Asym")
mod1 <- stages_bhc(full(Asym, lambda = 1))
mod2 <- stages_fbhc(full(Asym, lambda = 1))
compare_stages(mod1, mod2)
##########
m0 <- full(PhDArticles[, 1:4], lambda = 0)
m1 <- stages_bhc(m0)
m2 <- stages_bj(m0, distance = "totvar", thr = 0.25)
diff_stages(m1, m2)
```


## Description

Confint method for class sevt.

## Usage

```
## S3 method for class 'sevt'
    confint(
        object,
        parm,
        level = 0.95,
        method = c("wald", "waldcc", "wilson", "goodman", "quesenberry-hurst"),
        ignore = object$name_unobserved,
    ...
    )
```


## Arguments

| object | an object of class sevt. |
| :--- | :--- |
| parm | a specification of which parameters are to be given confidence intervals, either <br> a vector of numbers or a vector of names. If missing, all parameters are consid- <br> ered. |
| level | the confidence level required. |
| method | a character string specifing which method to use: wald", "waldcc", "goodman", <br> "quesenberry-hurst" or "wilson". |
| ignore | vector of stages which will be ignored, by default the name of the unobserved <br> stages stored in object\$name_unobserved. |
| $\ldots$ | additional argument(s) for compatibility with confint methods. |

## Details

Compute confidence intervals for staged event trees. Currently five methods are available:

- wald, waldcc: Wald method and with continuity correction.
- wilson, quesenberry-hurst and goodman.


## Value

A matrix with columns giving lower and upper confidence limits for each parameter. These will be labelled as $(1-\mathrm{level}) / 2$ and $1-(1-\mathrm{level}) / 2$ in $\%$ (by default $2.5 \%$ and $97.5 \%$ ).

## Author(s)

The function is partially inspired by code in the MultinomCI function from the DescTools package, implemented by Andri Signorelli and Pablo J. Villacorta Iglesias.

## References

Goodman, L. A. (1965) On Simultaneous Confidence Intervals for Multinomial Proportions Technometrics, 7, 247-254.
Wald, A. Tests of statistical hypotheses concerning several parameters when the number of observations is large, Trans. Am. Math. Soc. 54 (1943) 426-482.
Wilson, E. B. Probable inference, the law of succession and statistical inference, J.Am. Stat. Assoc. 22 (1927) 209-212.

Quesenberry, C., \& Hurst, D. (1964). Large Sample Simultaneous Confidence Intervals for Multinomial Proportions. Technometrics, 6(2), 191-195

## Examples

```
m1 <- stages_bj(full(PhDArticles), distance = "kullback", thr = 0.01)
confint(m1, "Prestige", level = 0.90)
confint(m1, "Married", method = "goodman")
confint(m1, c("Married", "Kids"))
```

full_indep Full and independent staged event tree

## Description

Build fitted staged event tree from data.

```
Usage
    full(
        data,
        order = NULL,
        join_unobserved = TRUE,
        lambda = 0,
        name_unobserved = "UNOBSERVED"
    )
    ## S3 method for class 'table'
    full(
        data,
        order = names(dimnames(data)),
        join_unobserved = TRUE,
        lambda = 0,
        name_unobserved = "UNOBSERVED"
```

```
full_indep
)
## S3 method for class 'data.frame'
full(
    data,
    order = colnames(data),
    join_unobserved = TRUE,
    lambda = 0,
    name_unobserved = "UNOBSERVED"
)
indep(
    data,
    order = NULL,
    join_unobserved = TRUE,
    lambda = 0,
    name_unobserved = "UNOBSERVED"
)
## S3 method for class 'table'
indep(
    data,
    order = names(dimnames(data)),
    join_unobserved = TRUE,
    lambda = 0,
    name_unobserved = "UNOBSERVED"
)
## S3 method for class 'data.frame'
indep(
        data,
        order = colnames(data),
        join_unobserved = TRUE,
        lambda = 0,
        name_unobserved = "UNOBSERVED"
)
```


## Arguments

data data to create the model, data.frame or table.
order character vector, order of variables.
join_unobserved
logical, if situations with zero observations should be joined (default TRUE).
lambda smoothing coefficient (default 0).
name_unobserved
name to pass to join_unobserved.

## Details

Functions to create full or independent staged tree models from data. The full (or saturated) staged tree is the model where every situation is in a different stage, and thus the model has the maximum number of parameters. Conversely, the independent staged tree (indep) assigns all the situations related to the same variable to the same stage, thus it is equivalent to the independence factorization.

## Examples

```
## full model
DD <- generate_xor_dataset(4, 100)
model_full <- full(DD, lambda = 1)
## independence model (data.frame)
DD <- generate_xor_dataset(4, 100)
model <- indep(DD, lambda = 1)
model
```

generate_linear_dataset

## Generate a random binary dataset for classification

## Description

Randomly generate a simple classification problem.

## Usage

```
generate_linear_dataset(
    n = 2,
    N = 10000,
    eps = 1.2,
    gamma = runif(1, min = -n, max = n),
    alpha = runif(n, min = -n, max = n)
)
```


## Arguments

| n | number of variables. |
| :--- | :--- |
| N | number of observations. |
| eps | noise. |
| gamma | numeric. |
| alpha | numeric vector of length n. |

## Value

A data.frame with $n$ independent random variables and one class variable $C$ computed as sign(sum( $x$ * alpha) + runif(1, -eps, eps) + gamma).

## Examples

DD <- generate_linear_dataset( $\mathrm{n}=5$, 1000)
generate_random_dataset
Generate a random binary dataset

## Description

Randomly generate a data.frame of independent binary variables.

## Usage

generate_random_dataset( $\mathrm{n}=2, \mathrm{~N}=10000$ )

## Arguments

$\mathrm{n} \quad$ number of variables.
N number of observations.

## Value

A data.frame with n independent random variables.

## Examples

DD <- generate_random_dataset $(n=5,1000)$
generate_xor_dataset Generate a xor dataset

## Description

Generate a xor dataset

## Usage

generate_xor_dataset( $\mathrm{n}=2, \mathrm{~N}=100$, eps $=1.2$ )

## Arguments

| $n$ | number of variables. |
| :--- | :--- |
| $N$ | number of observations. |
| eps | error. |

## Value

The xor dataset with $n+1$ variables, where the first one is the class variable $C$ computed as a noisy xor.

## Examples

```
DD <- generate_xor_dataset(n = 5, N = 1000, eps = 1.2)
```

```
get_stage Get stage or path
```


## Description

Utility functions to obtain stages from paths and paths from stages.

## Usage

```
get_stage(object, path)
get_path(object, var, stage)
```


## Arguments

| object <br> path | an object of class sevt. <br> character vector, the path from root or a two dimensional array where each row <br> is a path from root. |
| :--- | :--- |
| var | character, one of the variable in the staged tree. |
| stage | character vector, the name of the stages for which the paths should be returned. |

## Value

get_stage returns the stage name(s) for given path(s).
get_path returns a data.frame containing the paths corresponding to the given stage(s).

## Examples

```
model <- stages_fbhc(full(PhDArticles))
get_stage(model, c("0", "male"))
paths <- expand.grid(model$tree[2:1])[, 2:1]
get_stage(model, paths)
get_path(model, "Kids", "5")
get_path(model, "Gender", "2")
get_path(model, "Kids", c("5", "6"))
```

```
    inclusions_stages Inclusions of stages
```


## Description

Display the relationship between two staged tree models over the same variables.

## Usage

inclusions_stages(object1, object2)

## Arguments

object1 an object of class sevt.
object2 an object of class sevt.

## Details

Computes the relations between the stages structures of the two models.
The relations between stages of the same variable are stored in a data frame with three columns where each row represent a relation between a stage of the first model ( s 1 ) and a stage of the second model (s2). The relation can be one of the following: inclusion (s1 < s2 or s1>s2; equal ( $s 1=s 2$ ); not-equal (s1 ! = s2).

## Value

a list with inclusion relations between stage structures for each variable in the models.

## Examples

```
mod1 <- stages_bhc(full(PhDArticles[, 1:5], lambda = 1))
mod2 <- stages_fbhc(full(PhDArticles[, 1:5], lambda = 1))
inclusions_stages(mod1, mod2)
```

join_stages Join stages

## Description

Join two stages in a staged event tree object, updating probabilities and log-likelihood accordingly.

## Usage

```
join_stages(object, v, s1, s2)
```


## Arguments

| object | an object of class sevt. |
| :--- | :--- |
| $v$ | variable. |
| s1 | first stage. |
| s2 | second stage. |

## Details

This function joins two stages associated to the same variable, updating probabilities and loglikelihood if the object was fitted.

## Value

the staged event tree where s1 and s2 are joined.

## Examples

```
model <- full(PhDArticles, lambda = 0)
model <- stages_fbhc(model)
model$stages$Kids
model <- join_stages(model, "Kids", "5", "6")
model$stages$Kids
```

join_unobserved Join situations with no observations

## Description

Join situations with no observations

## Usage

```
join_unobserved(
    object,
    fit = TRUE,
    trace = 0,
    name = "UNOBSERVED",
    scope = sevt_varnames(object)[-1],
    lambda = object$lambda
)
```


## Arguments

object
fit if TRUE update model's probabilities.
trace if $>0$ print information to console.
name character, name for the new stage storing unobserved situations.
scope character vector, list of variables in object.
lambda smoothing parameter for the fitting.

## Details

It takes as input a (fitted) staged event tree object and it joins, in the same stage, all the situations with zero recorded observations. Since such joining does not change the log-likelihood of the model, it is a useful (time-wise) pre-processing prior to others model selection algorithms.
Unobserved situations can be joined directly in full or indep, by setting join_unobserved= TRUE.

## Value

a staged event tree with at most one stage per variable with no observations. If, as default, fit=TRUE the model will be re-fitted, if fit=FALSE probabilities in the output model are not estimated.

## Examples

```
DD <- generate_xor_dataset(n = 5, N = 10)
model_full <- full(DD, lambda = 1, join_unobserved = FALSE)
model <- join_unobserved(model_full)
logLik(model_full)
logLik(model)
BIC(model_full, model)
```

logLik.sevt Log-Likelihood of a staged event tree

## Description

Compute, or extract the log-likelihood of a staged event tree.

## Usage

\#\# S3 method for class 'sevt'
logLik(object, ...)

## Arguments

object an fitted object of class sevt. additional parameters (compatibility).

## Value

An object of class logLik.

## Examples

```
data("PhDArticles")
mod <- indep(PhDArticles)
logLik(mod)
```

lr_test Likelihood Ratio Test for staged trees models

## Description

Function to perform likelihood ratio test between two or multiple staged event tree models.

## Usage

lr_test(object, ...)

## Arguments

object an object of class sevt.
... further objects of class sevt. Must specify super-models of object. See below for details.

## Details

If a single object of class sevt is passed as argument, it computes the likelihood-ratio test with respect to the independence model. If multiple objects are passed, likelihood-ratio tests between the first object and the followings are computed. In the latter casem the function checks automatically if the first model is nested in the additional ones, via inclusions_stages, and throws an error if not.

## Value

An object of class anova which contains the log-likelihood, degrees of freedom, difference in degrees of freedom, likelihood ratio statistics and corresponding p values.

## Examples

```
data(PhDArticles)
order <- c("Gender", "Kids", "Married", "Articles")
phd.mod1 <- stages_hc(indep(PhDArticles, order))
phd.mod2 <- stages_hc(full(PhDArticles, order))
## compare two nested models
lr_test(phd.mod1, phd.mod2)
```

```
## compare a single model vs the independence model
lr_test(phd.mod1)
```

PhDArticles PhD Students Publications

## Description

Number of publications of 915 PhD biochemistry students during the 1950's and 1960's.

## Usage

PhDArticles

## Format

A data frame with 915 rows and 6 variables:

Articles Number of articles during the last 3 years of PhD: either 0, 1-2 or $>2$.
Gender male or female.
Kids yes if the student has at least one kid 5 or younger, no otherwise.
Married yes or no.
Mentor Number of publications of the student's mentor: low between 0 and 3, medium between 4 and 10 , high otherwise.

Prestige low if the student is at a low-prestige university, high otherwise.

## Source

The data has been modified from the Rchoice package.

## References

Long, J. S. (1990). The origins of sex differences in science. Social Forces, 68(4), 1297-1316.

```
plot.ceg igraph's plotting for CEG
```


## Description

igraph's plotting for CEG

## Usage

\#\# S3 method for class 'ceg'
plot(x, col = NULL, ignore = x\$name_unobserved, layout = NULL, ...)

## Arguments

x
an object of class ceg.
col colors specification see plot.sevt.
ignore vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in $\times \$$ name_unobserved.
layout an igraph layout.
... additional arguments passed to plot.igraph.

## Details

This function is a simple wrapper around igraph's plot.igraph. The ceg object is converted to an igraph object by firstly obtaining the adjacency matrix representation with ceg2adjmat. If not specified, the default layout used is a rotated layout.reingold.tilford.

We use palette() as palette for the igraph plotting, while plot.igraph uses as default a different palette. This is to allow matching stages colors between plot. ceg and plot.sevt.

## Examples

```
## Not run:
    model <- stages_bhc(full(Titanic))
    model.ceg <- ceg(model)
    plot(model.ceg, edge.arrow.size = 0.1, vertex.label.dist = -2)
## End(Not run)
```

plot.sevt
Plot method for staged event trees

## Description

Plot method for staged event tree objects. It allows easy plotting of staged event trees with some options (see Examples).

## Usage

```
\#\# S3 method for class 'sevt'
plot
        x ,
        \(y=10\),
        limit = y,
        \(x \lim =c(0,1)\),
        ylim \(=c(0,1)\),
        main = NULL,
        sub \(=\) NULL,
        asp = 1,
        cex_label_nodes = 0,
        cex_label_edges = 1,
        cex_nodes = 2,
        cex_tree_y = 0.9,
        col = NULL,
        col_edges = "black",
        var_names = TRUE,
        ignore = x\$name_unobserved,
        pch_nodes \(=16\),
        lwd_nodes = 1,
        lwd_edges = 1,
        )
    make_stages_col(x, col = NULL, ignore = x\$name_unobserved, limit = NULL)
```


## Arguments

x
$y \quad$ alias for limit for compatibility with plot.
limit maximum number of variables plotted.
$x \lim \quad$ the $x$ limits $(x 1, x 2)$ of the plot.
ylim the $y$ limits of the plot.
main an overall title for the plot.
sub an object of class sevt.
a sub title for the plot.
sub

```
asp the y/x aspect ratio.
cex_label_nodes
the magnification to be used for the node labels. If set to 0 (as default) node labels are not showed.
cex_label_edges
the magnification for the edge labels. If set to 0 edge labels are not displayed.
cex_nodes the magnification for the nodes of the tree.
cex_tree_y the magnification for the tree in the vertical direction. Default is 0.9 to leave some space for the variable names.
col color mapping for stages, one of the following: NULL (color will be assigned based on the current palette); a named (variables) list of named (stages) vectors of colors; the character "stages", in which case the stage names will be used as colors; a function that takes as input a vector of stages and output the corresponding colors. Check the provided examples. The function make_stages_col is used internally and make_stages_col ( \(x\), NULL) or make_stages_col ( \(x\), "stages") can be used as a starting point for colors tweaking.
col_edges color for the edges.
var_names logical, if variable names should be added to the plot, otherwise variable names can be added manually using text. sevt.
ignore vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in \(\times \$\) name_unobserved.
pch_nodes either an integer specifying a symbol or a single character to be used as the default in plotting nodes shapes see points.
lwd_nodes the line width for edges, a positive number, defaulting to 1 .
lwd_edges the line width for nodes, a positive number, defaulting to 1 .
additional graphical parameters to be passed to points, lines, title, text and plot.window.
```


## Examples

```
data("PhDArticles")
mod <- stages_bj(full(PhDArticles, join_unobserved = TRUE))
### simple plotting
plot(mod)
### labels in nodes
plot(mod, cex_label_nodes = 1, cex_nodes = 0)
### reduce nodes size
plot(mod, cex_nodes = 0.5)
### change line width and nodes style
plot(mod, lwd_edges = 3, pch_nodes = 5)
### changing palette
```

```
plot(mod, col = function(s) heat.colors(length(s)))
### or changing global palette
palette(hcl.colors(10, "Harmonic"))
plot(mod)
palette("default") ##
### forcing plotting of unobserved stages
plot(mod, ignore = NULL)
### use function to specify colors
plot(mod, col = function(stages){
    hcl.colors(n = length(stages))
})
### manually give stages colors
### as an example we will assign colors only to the stages of two variables
### Gender (one stage named "1") and Mentor (six stages)
col <- list(Gender = c("1" = "blue"),
    Mentor = c("UNOBSERVED" = "grey",
    "2" = "red",
    "3" = "purple",
    "10" = "pink",
    "18" = "green",
    "22" = "brown"))
### by setting ignore = NULL we will plot also the UNOBSERVED stage for Mentor
plot(mod, col = col, ignore = NULL)
```

Pokemon Pokemon Go Users

## Description

Demographic information of a population of possible Pokemon Go users.

## Usage

Pokemon

## Format

A data frame with 999 rows and 5 variables:
Use $Y$ if the individual used the app, $N$ otherwise
Age $>30$ if the individual is older than 30, $<=30$ otherwise
Degree Yes if the individual completed a Higher Education degree, No otherwise
Gender Male or Female
Activity Yes if the individual was physically active (i.e. had a walk longer than 30 mins, went for a run or had a bike ride to get some exercise) in the past week before the experiment, No otherwise

## Source

https://osf.io/xy5g6/

## References

Gabbiadini, Alessandro, Christina Sagioglou, and Tobias Greitemeyer. "Does Pokémon Go lead to a more physically active life style?." Computers in Human Behavior 84 (2018): 258-263.

```
predict.sevt Predict method for staged event tree
```


## Description

Predict class values from a staged event tree model.

## Usage

```
    ## S3 method for class 'sevt'
```

    predict (object, newdata \(=\) NULL, class \(=\) NULL, prob \(=\) FALSE, log = FALSE,.. )
    
## Arguments

object an object of class sevt with fitted probabilities.
newdata the newdata to perform predictions
class character, the name of the variable to use as the class variable, if NULL the first element names(object\$tree) will be used.
prob logical, if TRUE the probabilities of class are returned
log logical, if TRUE log-probabilities are returned
... additional parameters, see details

## Details

Predict the most probable a posterior value for the class variable given all the other variables in the model. Ties are broken at random and if, for a given vector of predictor variables, all conditional probabilities are 0, NA is returned.
if prob = TRUE, a matrix with number of rows equals to the number of rows in the newdata and number of columns as the number of levels of the class variable is returned. if log = TRUE, logprobabilities are returned.
if prob = FALSE, a vector of length as the number of rows in the newdata with the level with higher estimated probability for each new observations is returned.

## Value

A vector of predictions or the corresponding matrix of probabilities.

## Examples

```
    DD <- generate_xor_dataset(n = 4, 600)
    order <- c("C", "X1", "X2", "X3", "X4")
    train <- DD[1:500, order]
    test <- DD[501:600, order]
    model <- full(train)
    model <- stages_bhc(model)
    pr <- predict(model, newdata = test, class = "C")
    table(pr, test$C)
    # class values:
    predict(model, newdata = test, class = "C")
    # probabilities:
    predict(model, newdata = test, class = "C", prob = TRUE)
    # log-probabilities:
    predict(model, newdata = test, class = "C", prob = TRUE, log = TRUE)
```

    print.sevt Print a staged event tree
    
## Description

Print a staged event tree

## Usage

```
## S3 method for class 'sevt'
print(x, ...)
```


## Arguments

| x | an object of class sevt. |
| :--- | :--- |
| $\ldots$ | additional parameters (compatibility). |

## Details

The order of the variables in the staged tree is printed (from root). In addition the number of levels of each variable is shown in square brackets. If available the log-likelihood of the model is printed.

## Value

An invisible copy of $x$.

## Examples

```
DD <- generate_xor_dataset(5, 100)
model <- full(DD, lambda = 1)
print(model)
```


## Description

Compute (marginal and/or conditional) probabilities of elementary events with respect to the probability encoded in a staged event tree.

## Usage

prob(object, x, conditional_on = NULL, log = FALSE, na0 = TRUE)

## Arguments

object an object of class sevt with probabilities.
$x \quad$ the vector or data.frame of observations.
conditional_on named vector, the conditioning event.
log logical, if TRUE log-probabilities are returned.
na0 logical, if NA should be converted to 0 .

## Details

Computes probabilities related to a vector or a data.frame of observations.
Optionally, conditional probabilities can be obtained by specifying the conditioning event in conditional_on. This can be done either with a single named vector or with a data.frame object with the same number of rows of $x$. In the former, the same conditioning is used for all the computed probabilities (if $x$ has multiple rows); while with the latter different conditioning events (but on the same variables) can be specified for each row of $x$.

## Value

the probabilities to observe each observation in $x$, possibly conditional on the event(s) in conditional_on.

## Examples

```
data(Titanic)
model <- full(Titanic, lambda = 1)
samples <- expand.grid(model$tree[c(1, 4)])
pr <- prob(model, samples)
## probabilities sum up to one
sum(pr)
## print observations with probabilities
print(cbind(samples, probability = pr))
## compute one probability
prob(model, c(Class = "1st", Survived = "Yes"))
```

```
    ## compute conditional probability
    prob(model, c(Survived = "Yes"), conditional_on = c(Class = "1st"))
    ## compute conditional probabilities with different conditioning set
    prob(model, data.frame(Age = rep("Adult", 8)),
        conditional_on = expand.grid(model$tree[2:1]))
    ## the above should be the same as
    summary(model)$stages.info$Age
```

    rename_stage Rename stage(s) in staged event tree
    
## Description

Change the name of a stage in a staged event tree.

## Usage

rename_stage(object, var, stage, new)

## Arguments

| object | an object of class sevt. |
| :--- | :--- |
| var | name of a variable in object. |
| stage | name of the stage to be renamed. |
| new | new name for the stage. |

## Details

No internal checks are performed and as side effect stages can be joined, if e.g. new is equal to the name of a stage for variable var.

## Value

a staged event tree object where stages stage have been renamed to new.
sample_from Sample from a staged event tree

## Description

Generate a random sample from the distribution encoded in a staged event tree object.

## Usage

sample_from(object, nsim $=1$, seed $=$ NULL)

## Arguments

object an object of class sevt with fitted probabilities.
nsim number of observations to sample.
seed an object specifying if and how the random number generator should be initialized ('seeded'). Either NULL or an integer that will be used in a call to set.seed.

## Details

It samples nsim observations according to the transition probabilities (object\$prob) in the model.

## Value

A data frame containing nsim observations from the variables in object.

## Examples

```
model <- stages_fbhc(full(PhDArticles, lambda = 1))
sample_from(model, 10)
```

```
search_best Optimal Order Search
```


## Description

Find the optimal staged event tree with a dynamic programming approach.

```
Usage
    search_best(
        data,
        alg = stages_bhc,
        search_criterion = BIC,
        lambda = 0,
        join_unobserved = TRUE,
    )
```


## Arguments

```
    data either a data.frame or a table containing the data.
    alg a function that performs stages structure estimation. Similar to stages_bhc or
        stages_hclust. The function alg must accept the argument scope.
    search_criterion
        the criterion minimized in the order search.
    lambda numerical value passed to full.
    join_unobserved
        logical, passed to full.
    ... additional arguments, passed to alg.
```


## Details

This function is an implementation of the dynamic programming approach of Silander and Leong (2013). If the search_criterion is decomposable the returned model attains the best value among all possible orders.

## Value

The estimated staged event tree model.

## References

Silander T., Leong TY. A Dynamic Programming Algorithm for Learning Chain Event Graphs. In: Fürnkranz J., Hüllermeier E., Higuchi T. (eds) Discovery Science. DS 2013. Lecture Notes in Computer Science, vol 8140. Springer, Berlin, Heidelberg. 2013.

Cowell R and Smith J. Causal discovery through MAP selection of stratified chain event graphs. Electronic Journal of Statistics, 8(1):965-997, 2014.

## Examples

```
## default search using BIC score
model <- search_best(Titanic, alg = stages_kmeans)
## use df as search_criterion
model1 <- search_best(Titanic, alg = stages_bhc,
    search_criterion = function(m) attr(logLik(m), "df"))
```

search_greedy Greedy Order Search

## Description

Search the optimal staged event tree with a greedy heuristic.

## Usage

```
    search_greedy(
        data,
        alg = stages_bhc,
        search_criterion = BIC,
        lambda = 0,
        join_unobserved = TRUE,
    )
```


## Arguments

## data

either a data.frame or a table containing the data.
alg
a function that performs stages structure estimation. Similar to stages_bhc or stages_hclust. The function alg must accept the argument scope.
search_criterion the criterion minimized in the order search.
lambda numerical value passed to full.
join_unobserved logical, passed to full.
... additional arguments, passed to alg.

## Details

The greedy approach implemented in this function iteratively adds variables to the staged tree that better improve the search_criterion.

## Value

The estimated staged event tree model.

## Examples

```
model <- search_greedy(Titanic, alg = stages_fbhc)
print(model)
```

$\qquad$
sevt Staged event tree (sevt) class

## Description

Structure and usage of S3 class sevt, used to store a staged event tree.

## Usage

```
sevt(x, full = FALSE, order = NULL)
## S3 method for class 'table'
sevt(x, full = FALSE, order = names(dimnames(x)))
## S3 method for class 'data.frame'
sevt(x, full = FALSE, order = colnames(x))
## S3 method for class 'list'
sevt(x, full = FALSE, order = names(x))
```


## Arguments

$x \quad$ a list, a data frame or table object.
full logical, if TRUE the full model is created otherwise the independence model.
order character vector, order of the variables to build the tree, by default the order of the variables in $x$.

## Details

A staged event tree object is a list with components:

- tree (required): A named list with one component for each variable in the model, a character vector with the names of the levels for that variable. The order of the variables in tree is the order of the event tree.
- stages (required): A named list with one component for each variable but the first, a character vector storing the stages for the situations related to path ending in that variable.
- ctables: A named list with one component for each variable, the flat contingency table of that variable given the previous variables.
- lambda: The smoothing parameter used to compute probabilities.
- name_unobserved: The stage name for unobserved situations.
- prob: The conditional probability tables for every variable and stage. Stored in a named list with one component for each variable, a list with one component for each stage.
- ll: The log-likelihood of the estimated model. If present, logLik. sevt will return this value instead of computing the log-likelihood.

The tree structure is never defined explicitly, instead it is implicitly defined by the list tree containing the order of the variables and the names of their levels. This is sufficient to define a complete symmetric tree where an internal node at a depth related to a variable $v$ has a number of children equal to the cardinality of the levels of $v$. The stages information is instead stored as a list of vectors, where each vector is indexed as the internal nodes of the tree at a given depth.
To define a staged tree from data (data frame or table) the user can call either full or indep which both construct the staged tree object, attach the data in ctables and compute probabilities. After, one of the available model selection algorithm can be used, see for example stages_hc, stages_bhc or stages_hclust. If, mainly for development, only the staged tree structure is needed (without data or probabilities) the basic sevt constructor can be used.

## Value

A staged event tree object, an object of class sevt.

## Examples

```
######### from table
model.titanic <- sevt(Titanic, full = TRUE)
######### from data frame
DD <- generate_random_dataset(n = 4, 1000)
model.indep <- sevt(DD)
model.full <- sevt(DD, full = TRUE)
######### from list
model <- sevt(list(
    X = c("good", "bad"),
    Y = c("high", "low")
))
```

sevt_add

Add a variable to a staged event tree

## Description

Return an updated staged event tree with one additional variable at the end of the tree.

## Usage

sevt_add(object, var, data, join_unobserved = TRUE)

## Arguments

object an object of class sevt.
var character, the name of the new variable to be added.
data either a data. frame or a table containing the data from the variables in object plus var.
join_unobserved
logical, passed to full.

## Details

This function update a staged event tree object with an additional variable. The stages structure of the new variable is initialized as in the saturated model.

## Value

An object of class sevt representing a staged event tree model with var added as last variable.

## Examples

```
    model <- full(Titanic, order = c("Age", "Class"))
    print(model)
    model <- sevt_add(model, "Survived", Titanic)
    print(model)
```

    sevt_fit
        Fit a staged event tree
    
## Description

Estimate transition probabilities in a staged event tree from data. Probabilities are estimated with the relative frequencies plus, eventually, an additive (Laplace) smoothing.

## Usage

sevt_fit(object, data $=$ NULL, lambda = object\$lambda)

## Arguments

object an object of class sevt.
data data.frame or contingency table with observations of the variables in object.
lambda smoothing parameter or pseudocount.

## Details

The data in form of contingency tables and the log-likelihood of the model is stored in the returned staged event tree.

## Value

A fitted staged event tree, that is an object of class sevt with ctables, prob and 11 components.

## Examples

```
#########
model <- sevt(list(
    X = c("good", "bad"),
    Y = c("high", "low")
))
D <- data.frame(
    X = c("good", "good", "bad"),
    Y = c("high", "low", "low")
)
model.fit <- sevt_fit(model, data = D, lambda = 1)
```


## Description

Algorithms to create, learn, fit and explore staged event tree models. Functions to compute probabilities, make predictions from the fitted models and to plot, analyze and manipulate staged event trees.

## Details

A staged event tree is a representation of a particular factorization of a joint probability over a product space. In particular, given a vector of categorical random variables $X 1, X 2, \ldots$, a staged event tree represents the factorization $P(X 1, X 2, X 3, \ldots)=P(X 1) P(X 2 \mid X 1) P(X 3 \mid X 1, X 2) \ldots$. Additionally, the stages structure indicates which conditional probabilities are equal.

Model selection algorithms:

- full model full
- independence model indep
- Hill-Climbing stages_hc
- Backward Hill-Climbing stages_bhc
- Fast Backward Hill-Climbing stages_fbhc
- Backward Hill-Climbing Random stages_bher
- Backward joining stages_bj
- Hierarchical Clustering stages_hclust
- K-Means Clustering stages_kmeans
- Optimal order search search_best
- Greedy order search search_greedy

Probabilities, log-likelihood and predictions:

- Marginal/Conditional probabilities prob
- Log-Likelihood logLik. sevt
- Predict method predict.sevt
- Confidence intervals confint.sevt

Plot, explore and compare:

- Plot plot.sevt
- Compare compare_stages
- Stages inclusion inclusions_stages
- Stages info summary.sevt
- List of parents as_parentslist
- Barplot construction barplot.sevt
- Likelihood-ratio test lr_test
- Context-specific interventional distance cid

Modify models:

- Join and isolate unobserved situations join_unobserved
- Join two stages join_stages
- Rename a stage rename_stage


## References

Collazo R. A., Görgen C. and Smith J. Q. Chain event graphs. CRC Press, 2018.
Görgen C., Bigatti A., Riccomagno E. and Smith J. Q. Discovery of statistical equivalence classes using computer algebra. International Journal of Approximate Reasoning, vol. 95, pp. 167-184, 2018.

Barclay L. M., Hutton J. L. and Smith J. Q. Refining a Bayesian network using a chain event graph. International Journal of Approximate Reasoning, vol. 54, pp. 1300-1309, 2013.
Smith J. Q. and Anderson P. E. Conditional independence and chain event graphs. Artificial Intelligence, vol. 172, pp. 42-68, 2008.
Thwaites P. A., Smith, J. Q. A new method for tackling asymmetric decision problems. International Journal of Approximate Reasoning, vol. 88, pp. 624-639, 2017.

## Examples

```
data("PhDArticles")
mf <- full(PhDArticles, join_unobserved = TRUE)
mod <- stages_fbhc(mf)
plot(mod)
```

stages Stages of a variable

## Description

Obtain the stages of a given variable in a staged event tree object.

## Usage

stages(object, var = NULL)

## Arguments

object an object of class sevt.
var name of one variable in object.

## Value

If var is specified, it returns a character vector with stage names for the given variable (that is object\$stages[[var]]. Otherwise, If var is not specified, stages returns a list of character vectors containing the stages associated to each variable in the model (that is object\$stages).

```
    stages_bhc Backward hill-climbing
```


## Description

Greedy search of staged event trees with iterative joining of stages.

## Usage

```
stages_bhc(
    object,
    score = function(x) { return(-BIC(x)) },
    max_iter = Inf,
    scope = NULL,
    ignore = object$name_unobserved,
    trace = 0
)
```


## Arguments

object an object of class sevt with fitted probabilities and data, as returned by full or sevt_fit.
score the score function to be maximized.
max_iter the maximum number of iterations per variable.
scope names of variables that should be considered for the optimization.
ignore vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in object\$name_unobserved.
trace if $>0$ increasingly amount of info is printed (via message).

## Details

For each variable the algorithm tries to join stages and moves to the best model that increases the score. When no increase is possible it moves to the next variable.

## Value

The final staged event tree obtained.

## Examples

```
DD <- generate_xor_dataset(n = 4, N = 100)
model <- stages_bhc(full(DD), trace = 2)
summary(model)
```


## stages_bhcr Backward random hill-climbing

## Description

Randomly try to join stages. This is a pretty-useless function, used for comparisons.

## Usage

```
    stages_bhcr(
        object,
        score = function(x) { return(-BIC(x)) },
        max_iter = 100,
        trace = 0
    )
```


## Arguments

object an object of class sevt.
score the score function to be maximized.
max_iter the maximum number of iteration.
trace if $>0$ increasingly amount of info is printed (via message).

## Details

At each iteration a variable and two of its stages are randomly selected. If joining the stages increases the score, the model is updated. The procedure is repeated until the number of iterations reaches max_iter.

## Value

an object of class sevt.

## Examples

```
DD <- generate_xor_dataset(n = 4, N = 100)
model <- stages_bhcr(full(DD), trace = 2)
summary(model)
```

```
stages_bj Backward joining of stages
```


## Description

Join stages from more complex to simpler models using a distance and a threshold value.

## Usage

```
stages_bj(
    object = NULL,
    distance = "kullback",
    thr = 0.1,
    scope = NULL,
    ignore = object$name_unobserved,
    trace = 0
)
```


## Arguments

object an object of class sevt with fitted probabilities and data, as returned by full or sevt_fit.
distance character, see details.
thr the threshold for joining stages
scope names of variables that should be considered for the optimization.
ignore vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in object\$name_unobserved.
trace if $>0$ increasingly amount of info is printed (via message).

## Details

For each variable in the model stages are joined iteratively. At each iteration the two stages with minimum distance are selected and joined if their distance is less than thr.
Available distances are: manhattan (manhattan), euclidean (euclidean), Renyi divergence (reny), Kullback-Liebler (kullback), total-variation (totvar), squared Hellinger (hellinger), Bhattacharyya (bhatt), Chan-Darwiche (chandarw). See also probdist.

## Value

The final staged event tree obtained.

## Examples

```
DD <- generate_xor_dataset(n = 5, N = 1000)
model <- stages_bj(full(DD, lambda = 1), trace = 2)
summary(model)
```

```
stages_fbhc Fast backward hill-climbing
```


## Description

Greedy search of staged event trees with iterative joining of stages.

## Usage

```
stages_fbhc(
    object = NULL,
    score = function(x) { return(-BIC(x)) },
    max_iter = Inf,
    scope = NULL,
    ignore = object$name_unobserved,
    trace = 0
    )
```


## Arguments

object an object of class sevt with fitted probabilities and data, as returned by full or sevt_fit.
score the score function to be maximized.
max_iter the maximum number of iteration.
scope names of variables that should be considered for the optimization.
ignore vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in object\$name_unobserved.
trace if $>0$ increasingly amount of info is printed (via message).

## Details

For each variable the algorithm tries to join stages and moves to the first model that increases the score. When no increase is possible it moves to the next variable.

## Value

The final staged event tree obtained.

## Examples

```
DD <- generate_xor_dataset(n = 5, N = 100)
model <- stages_fbhc(full(DD), trace = 2)
summary(model)
```


## Description

Greedy search of staged event trees with iterative moving of nodes between stages.

## Usage

stages_hc(
object,
score $=$ function $(x)\{\quad \operatorname{return}(-B I C(x))\}$,
max_iter = Inf,
scope $=$ NULL,
ignore = object\$name_unobserved,
trace $=0$
)

## Arguments

object an object of class sevt with fitted probabilities and data, as returned by full or sevt_fit.
score the score function to be maximized.
max_iter the maximum number of iterations per variable.
scope names of variables that should be considered for the optimization
ignore vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in object\$name_unobserved.
trace if $>0$ increasingly amount of info is printed (via message).

## Details

For each variable node-moves that best increases the score are performed until no increase is possible. A node-move is either changing the stage associate to a node or move the node to a new stage.
The ignore argument can be used to specify stages that should not be affected during the search, that is left untouched. This is useful for preserving structural zeroes and to speed-up computations.

## Value

The final staged event tree obtained.

## Examples

```
start <- indep(PhDArticles[,1:5], join_unobserved = TRUE)
model <- stages_hc(start)
```

stages_hclust Learn a staged tree with hierarchical clustering

## Description

Build a stage event tree with $k$ stages for each variable by clustering stage probabilities with hierarchical clustering.

## Usage

```
    stages_hclust(
        object,
        distance = "totvar",
        k = length(object$tree[[1]]),
        method = "complete",
        ignore = object$name_unobserved,
        limit = length(object$tree),
        scope = NULL
    )
```


## Arguments

object an object of class sevt with fitted probabilities and data, as returned by full or sevt_fit.
distance character, the distance measure to be used, either a possible method for dist or one of the following: "totvar", "hellinger".
$\mathrm{k} \quad$ integer or (named) vector: number of clusters, that is stages per variable. Values will be recycled if needed.
method the agglomeration method to be used in hclust.
ignore vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in object\$name_unobserved.
limit the maximum number of variables to consider.
scope names of the variables to consider.

## Details

hclust_sevt performs hierarchical clustering of the initial stage probabilities in object and it aggregates them into the specified number of stages $(k)$. A different number of stages for the different variables in the model can be specified by supplying a (named) vector via the argument $k$.

## Value

A staged event tree object.

## Examples

```
data("Titanic")
model <- stages_hclust(full(Titanic, join_unobserved = TRUE, lambda = 1), k = 2)
summary(model)
```

stages_kmeans Learn a staged tree with $k$-means clustering

## Description

Build a stage event tree with k stages for each variable by clustering (transformed) probabilities with k-means.

## Usage

```
stages_kmeans(
    object,
    k = length(object$tree[[1]]),
    algorithm = "Hartigan-Wong",
    transform = sqrt,
    ignore = object$name_unobserved,
    limit = length(object$tree),
    scope = NULL,
    nstart = 1
)
```


## Arguments

object an object of class sevt with fitted probabilities and data, as returned by full or sevt_fit.
$\mathrm{k} \quad$ integer or (named) vector: number of clusters, that is stages per variable. Values will be recycled if needed.
algorithm character: as in kmeans.
transform function applied to the probabilities before clustering.
ignore vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in object\$name_unobserved.
limit the maximum number of variables to consider.
scope names of the variables to consider.
nstart as in kmeans

## Details

kmenas_sevt performs k-means clustering to aggregate the stage probabilities of the initial staged tree object. Different values for k can be specified by supplying a (named) vector to k . kmeans from the stats package is used internally and arguments algorithm and nstart refer to the same arguments as kmeans.

## Value

A staged event tree.

## Examples

```
data("Titanic")
model <- stages_kmeans(full(Titanic, join_unobserved = TRUE, lambda = 1), k = 2)
summary(model)
```

```
stndnaming Standard renaming of stages
```


## Description

Rename all stages in a staged event tree.

## Usage

```
stndnaming(
    object,
    uniq = FALSE,
    prefix = FALSE,
    ignore = object$name_unobserved
)
```


## Arguments

object an object of class sevt.
uniq logical, if stage numbers should be unique over all tree.
prefix logical, if stage names should be prefixed with variable name.
ignore vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in object\$name_unobserved.

## Value

a staged event tree object with stages named with consecutive integers.

## Examples

```
model <- stages_fbhc(full(PhDArticles, join_unobserved = TRUE))
model$stages
model1 <- stndnaming(model)
model1$stages
### unique stage names in all tree
model2 <- stndnaming(model, uniq = TRUE)
model2$stages
```

```
    ### prefix stage names with variable name
    model3 <- stndnaming(model, prefix = TRUE)
    model3$stages
    ### manuallty select stage names left untouched
    model4 <- stndnaming(model, ignore = c("2", "6"), prefix = TRUE)
    model4$stages
```

    subtree Extract subtree
    
## Description

Extract subtree

## Usage

subtree(object, path)

## Arguments

object an object of class sevt.
path the path from root after which extract the subtree.

## Details

Returns the subtree of the staged event tree, starting from path.

## Value

A staged event tree object corresponding to the subtree.

## Examples

```
DD <- generate_random_dataset(4, 100)
model <- sevt(DD, full = TRUE)
plot(model)
model1 <- subtree(model, path = c("-1", "1"))
plot(model1)
```


## Description

Summary method for class sevt.

## Usage

\#\# S3 method for class 'sevt'
summary (object, ...)
\#\# S3 method for class 'summary.sevt'
print( $x, \max =10, \ldots$ )

## Arguments

object an object of class sevt.
... arguments for compatibility.
$x \quad$ an object of class summary. sevt.
$\max \quad$ the maximum number of variables for which information is printed.

## Details

Print model information and summary of stages.

## Value

An object of class summary. sevt for which a print method exist.

## Examples

```
model <- stages_fbhc(full(PhDArticles, lambda = 1))
summary(model)
```

text.sevt

Add text to a staged event tree plot

## Description

Add text to a staged event tree plot

## Usage

\#\# S3 method for class 'sevt'
$\operatorname{text}(x, y=y \lim [1], \operatorname{limit}=10, x \lim =c(0,1), y \lim =c(0,1), \ldots)$

## Arguments

x
y
limit
xlim
ylim

An object of class sevt.
the position of the labels.
maximum number of variables plotted.
graphical parameter.
graphical parameter.
additional parameters passed to text.

## Index

* datasets

Asym, 4
PhDArticles, 23
Pokemon, 27
as.character. parentslist, 3, 6
as_adj_matrix, 4
as_bn, 5
as_parentslist, 5, 7, 38
as_sevt, 6
Asym, 4
barplot, 8
barplot.sevt, 8,39
ceg, 9, 10, 24
ceg2adjmat, 9, 24
cid, 10, 39
compare_stages, 11, 38
confint.sevt, 13, 38
diff_stages (compare_stages), 11
dist, 45
full, 21, 33-36, 38
full (full_indep), 14
full_indep, 14
generate_linear_dataset, 16
generate_random_dataset, 17
generate_xor_dataset, 17
get_path (get_stage), 18
get_stage, 18
hamming_stages (compare_stages), 11
hclust, 45
inclusions_stages, 19, 22, 38
indep, 21, 35, 38
indep (full_indep), 14
join_stages, 19, 39
join_unobserved, 15, 20, 39
kmeans, 46
logLik, 22
logLik.sevt, 21, 35, 38
lr_test, 22, 39
make_stages_col (plot.sevt), 25
PhDArticles, 23
plot.ceg, 24
plot.sevt, 8, 11, 24, 25, 38
points, 26
Pokemon, 27
predict.sevt, 28, 38
print. parentslist, 6
print. parentslist
(as.character. parentslist), 3
print.sevt, 29
print. summary.sevt (summary.sevt), 49
prob, 30, 38
probdist, 42
rename_stage, 31, 39
sample_from, 32
search_best, 32, 38
search_greedy, 33, 38
sevt, $6,7,9,10,22,34,35$
sevt_add, 36
sevt_fit, 37
stagedtrees, 38
stages, 39
stages_bhc, 33-35, 38, 40
stages_bhcr, 38, 41
stages_bj, 38, 42
stages_fbhc, 38, 43
stages_hc, 35, 38, 44
stages_hclust, 33-35, 38, 45
stages_kmeans, 38, 46
stndnaming, 12, 47
subtree, 48
summary.sevt, 38, 49
text, 50
text.sevt, 26, 49

